

Do all problems and show your work. Credit is not given for answers only. Don't spend too much time on any one problem. Use separate sheets of paper and don't cram your work into the spaces below. As in the notes,  $z_F$  and  $z'_F$  are the object and image distances measured from the front and rear focal points. The distances  $z$  and  $z'$  are the object and image distances measured from the front and rear principal plane. Questions 1-5 are worth 8 points each. Questions 6-8 are worth 20 points each.

Thin lens or general system $\phi = \frac{1}{f}$	Focal Lengths $f'_R = n'f \quad f_F = -nf$
Single surface $\phi = \frac{n' - n}{R}$	Total power of two elements $\phi = \phi_1 + \phi_2 - \left(\frac{t'_1}{n'_1}\right)\phi_1\phi_2$
Front Principal Plane $\delta = \frac{d}{n} = \frac{\phi_2}{\phi} \left(\frac{t'_1}{n'_1}\right)$	Rear Principal Plane $\delta' = \frac{d'}{n'} = -\frac{\phi_1}{\phi} \left(\frac{t'_1}{n'_1}\right)$
Front Focal Distance $FFD = f_F + d$	Back Focal Distance $BFD = f'_R + d'$
Gaussian Imaging Eq. $\frac{n'}{z'} - \frac{n}{z} = \frac{1}{f}$	Newtonian Imaging Eq. $z_F z'_F = f_F f'_R$
Transverse Magnification $m = \frac{h'}{h} = \frac{nz'}{n'z} = -\frac{z'_F}{f'_R} = -\frac{f_F}{z_F} = \frac{nu}{n'u'}$	Longitudinal Magnification (small shift) $\bar{m} = \frac{n'}{n} m^2$
Nodal Points $z_{PN} = z'_{PN} = f_F + f'_R = (n' - n)f$	Mirrors Thickness and indices switch sign after reflection
Paraxial Refraction (Reflection) Equation $n'_j u'_j = n_j u_j - y_j \phi_j$	Paraxial Transfer Equation $y_{j+1} = y_j + n'_j u'_j \frac{t'_j}{n'_j}$

- The object space index is  $n = 1$  and the image space index is  $n' = 1$ . Given an object distance  $z_F = -60mm$  and a lens of focal length  $f = -40mm$ , what is the image distance  $z'_F$  and the magnification  $m$ ? What are the front and rear focal lengths  $f_F$  and  $f'_R$ ?
- The object space index is  $n = 1.5$  and the image space index is  $n' = 1$ . Given an image distance  $z'_F = 20mm$  and a lens of focal length  $f = 40mm$ , what is the object distance  $z_F$  and the magnification  $m$ ? What are the front and rear focal lengths  $f_F$  and  $f'_R$ ?
- The object space index is  $n = 1.333$  and the image space index is  $n' = 1$ . Given a magnification  $m = -3$  and a lens of focal length  $f = -40mm$ , what is the object distance  $z_F$  and the image distance  $z'_F$ ? What are the front and rear focal lengths  $f_F$  and  $f'_R$ ?

4. The object space index is  $n = 1$  and the image space index is  $n' = 1$ . Given an object distance  $z_F = -40\text{mm}$  and a lens of focal length  $f = -80\text{mm}$ , what is the image distance  $z'_F$  and the magnification  $m$ ? What are the front and rear focal lengths  $f_F$  and  $f'_R$ ?
5. The object space index is  $n = 1.5$  and the image space index is  $n' = 1$ . Given an image distance  $z'_F = 80\text{mm}$  and a lens of focal length  $f = 60\text{mm}$ , what is the object distance  $z_F$  and the magnification  $m$ ? What are the front and rear focal lengths  $f_F$  and  $f'_R$ ?
6. A Cooke triplet consists of three thin lenses in air. The effective focal lengths of the lenses are  $f_1 = 44.4\text{ mm}$ ,  $f_2 = -22\text{ mm}$  and  $f_3 = 44.4\text{ mm}$ . The lenses are separated by  $t'_1 = t'_2 = 15.3\text{ mm}$ . Do the following:
- Sketch the lens and label the lens vertices,  $V_1$ ,  $V_2$  and  $V_3$ . Show the location of the principal planes for each of the three thin lenses.
  - Find the powers of each individual thin lens.
  - Using Gaussian reduction, calculate the overall power of the system and the locations of the principal planes?
7. A Cassegrain telescope has two reflective mirrors. The first mirror has a radius of curvature of  $R_1 = -1000\text{ mm}$ . The second mirror lies to the left of the first mirror such that  $t'_1 = -400\text{ mm}$ . The radius of curvature of the second mirror is  $R_2 = -250\text{ mm}$ .
- Sketch the telescope and label the vertices,  $V_1$ ,  $V_2$ .
  - Using Gaussian reduction, find the overall focal length of the telescope.
  - Where are the principal planes located with respect to the vertices  $V_1$  and  $V_2$ ?
8. A thick lens has air ( $n_1 = 1$ ) on the object side and water ( $n'_2 = 1.33$ ) on the image side. The lens is 20 mm thick and has a refractive index of  $n'_1 = 1.5$ . The radii of curvature of the lens are  $R_1 = 50\text{ mm}$  and  $R_2 = -40\text{ mm}$ , respective.
- Sketch the telescope and label the vertices,  $V_1$  and  $V_2$ .
  - Using Gaussian reduction, find the overall focal length of the lens.
  - Where are the principal planes located with respect to the vertices  $V_1$  and  $V_2$ ?
  - Where are the nodal points located?