

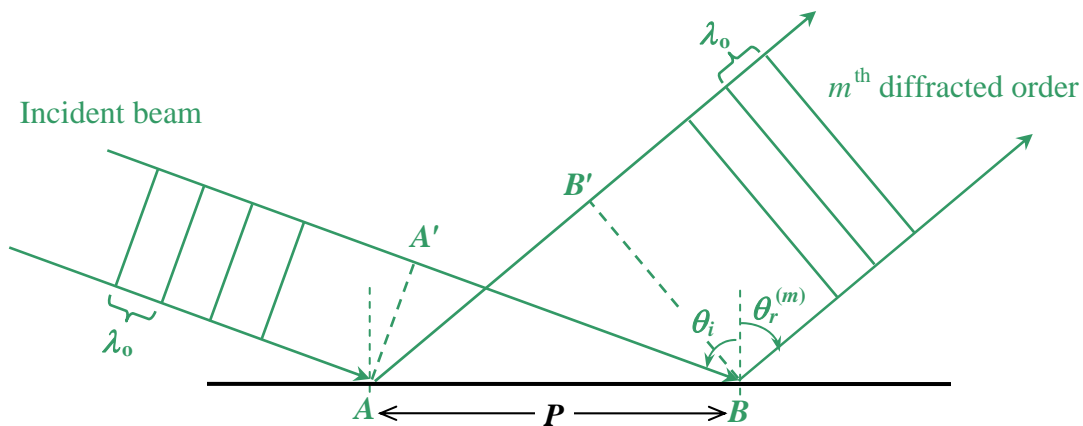
## MEASURING THE WAVELENGTH OF LIGHT USING A RULER

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A simple and dramatic measurement that's an exercise in trigonometry.

Figure 1 shows the arrangement that might be called a grazing incidence diffraction grating. It is easy to see many orders of interference. The hard part is quantifying how near to grazing incidence.

The ruler should have a scale that is either raised or indented and at least as fine as 1 mm. We used a machinist's vernier caliper scale. The light source was a green laser pointer.



**Figure 1.** The incident plane-wave arrives on the grating surface at an angle  $\theta_i$ . The  $m^{\text{th}}$  diffracted order leaves the grating at an angle  $\theta_r^{(m)}$ . The grating period  $P$  is the distance between points  $A$  and  $B$ . The line  $AA'$  is perpendicular to the incident rays; the distance between  $A'$  and  $B$ , which is given by  $P \sin \theta_i$ , is the extra path-length covered by the upper incident ray relative to the lower incident ray. Similarly,  $BB'$  is perpendicular to the  $m^{\text{th}}$  order diffracted rays; the distance between  $A$  and  $B'$ , which is given by  $P \sin \theta_r^{(m)}$ , is the extra path-length covered by the upper diffracted ray relative to the lower diffracted ray. The difference between  $AB'$  and  $A'B$  must be an integer-multiple of the wavelength  $\lambda_0$ , that is,

$$P \sin \theta_r^{(m)} - P \sin \theta_i = m \lambda_0.$$

This is the grating equation for the  $m^{\text{th}}$  diffracted order. In the experiment with the ruler,  $P = 0.635 \text{ mm}$ ,  $\theta_i = 88.5^\circ$ ,  $\theta_r^{(m)} = 87.2^\circ$ , and  $m = -1$ , yielding  $\lambda_0 = 0.54 \mu\text{m}$ .

It is a pleasure to acknowledge publication of a similar analysis by a great teacher, Arthur L. Schawlow.

“Measuring the Wavelength of Light with a Ruler,” *American Journal of Physics*, Volume 33, Issue 11, pp 922-923 (1965).