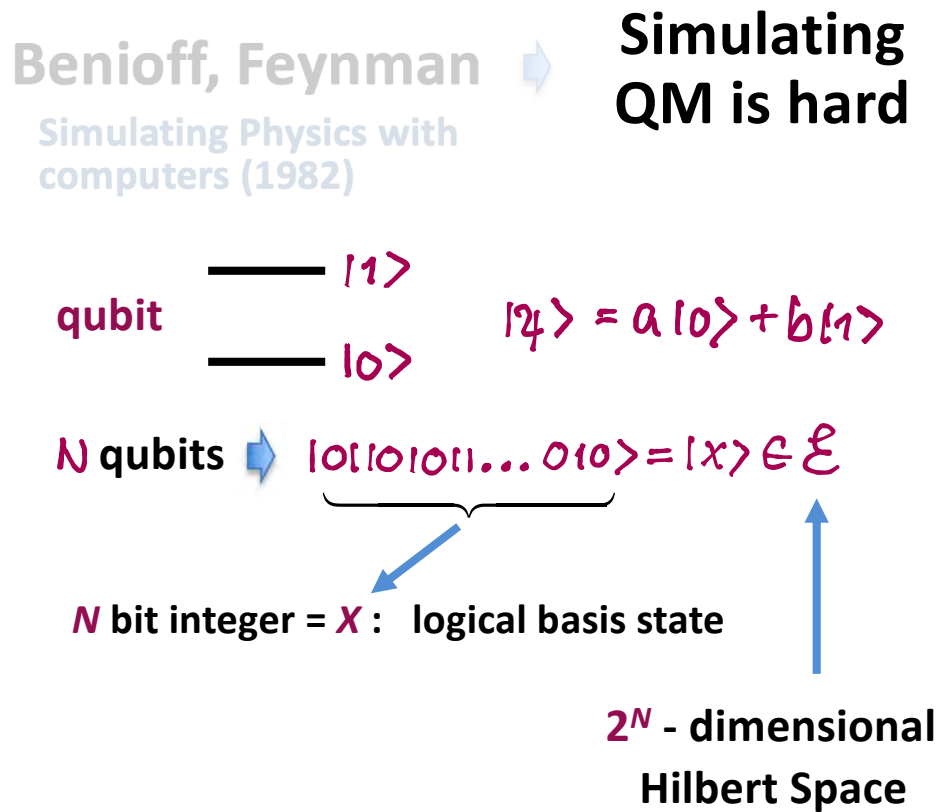


# Introduction and Overview (Preskills Notes)

## Quantum Complexity



General State:

$$|\psi\rangle = \sum_{x=0}^{2^N-1} a_x |x\rangle$$

## Simulating Physics with Computers

Richard P. Feynman

Department of Physics, California Institute of Technology, Pasadena, California 91107

Received May 7, 1981

### 1. INTRODUCTION

On the program it says this is a keynote speech—and I don't know what a keynote speech is. I do not intend in any way to suggest what should be in this meeting as a keynote of the subjects or anything like that. I have my own things to say and to talk about and there's no implication that anybody needs to talk about the same thing or anything like it. So what I want to talk about is what Mike Dertouzos suggested that nobody would talk about. I want to talk about the problem of simulating physics with computers and I mean that in a specific way which I am going to explain. The reason for doing this is something that I learned about from Ed Fredkin, and my entire interest in the subject has been inspired by him. It has to do with learning something about the possibilities of computers, and also something about possibilities in physics. If we suppose that we know all the physical laws perfectly, of course we don't have to pay any attention to computers. It's interesting anyway to entertain oneself with the idea that we've got something to learn about physical laws; and if I take a relaxed view here (after all I'm here and not at home) I'll admit that we don't understand everything.

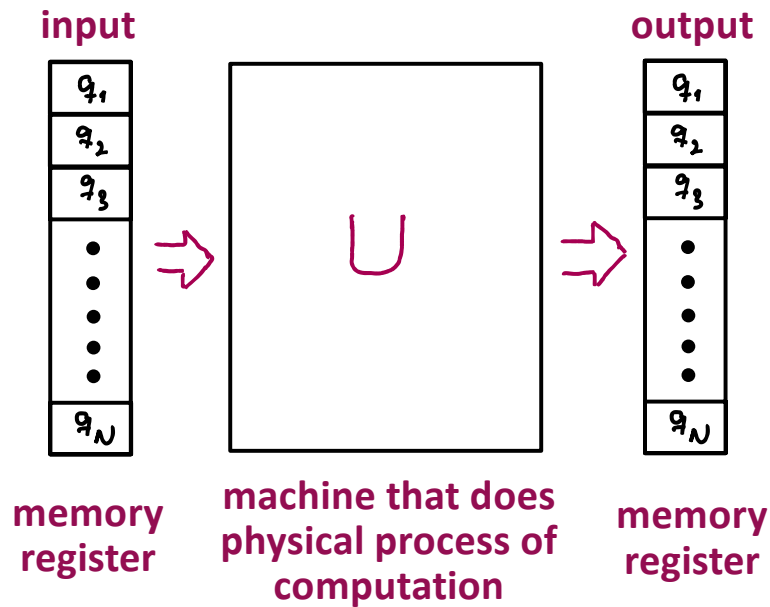
The first question is, What kind of computer are we going to use to simulate physics? Computer theory has been developed to a point where it realizes that it doesn't make any difference; when you get to a *universal computer*, it doesn't matter how it's manufactured, how it's actually made. Therefore my question is, Can physics be simulated by a universal computer? I would like to have the elements of this computer *locally interconnected*, and therefore sort of think about cellular automata as an example (but I don't want to force it). But I do want something involved with the

# Introduction and Overview (Preskills Notes)

OK – Plausible QM can do more

Where does the QC's power come from?

## Visualization of Computation



Classical: Register is in one of the logical states

$$x = \underbrace{q_1 q_2 q_3 \dots q_N}_{\text{binary \#}}$$

Reversible transformation

$$U: x \rightarrow y$$

Quantum: Register can be in any coherent superposition of logical states  $|x\rangle$

Unitary transformation  $U: |x\rangle \rightarrow |y\rangle$

Maps basis to basis  $U: \{|x\rangle\} \rightarrow \{|y\rangle\}$

## Quantum Parallelism

$$\begin{aligned} |\psi_{in}\rangle &\rightarrow \sum_x a_x |x\rangle \rightarrow | \\ &\rightarrow |\psi_{out}\rangle = U|\psi_{in}\rangle = \sum_x a_x |y\rangle = \sum_x b_x |x\rangle \end{aligned}$$

Machine processes  $2^N$  inputs “in parallel” !

Beware: measurement collapses Q. Register into a single basis state at random

We get one random result out of  $2^N$

# Introduction and Overview (Preskills Notes)

Quantum: Register can be in any coherent superposition of logical states  $|x\rangle$

Unitary transformation  $U: |x\rangle \rightarrow |y\rangle$

Maps basis to basis  $U: \{|x\rangle\} \rightarrow \{|y\rangle\}$

## Quantum Parallelism

$$|\psi_{in}\rangle \rightarrow \sum_x a_x |x\rangle \rightarrow$$

Quantum Sampling Problem

$$\rightarrow |\psi_{out}\rangle = U|\psi_{in}\rangle = \sum_x a_x |y\rangle = \sum_x b_x |x\rangle$$

Machine processes  $2^N$  inputs “in parallel” !

Beware: measurement collapses Q. Register into a single basis state at random

We get one random result out of  $2^N$

Quantum Algorithms look for global properties of functions – **symmetry, periodicity, etc.**

- \* Classical -> requires many function evaluations
- \* Quantum -> design **U** so measurement gives answer with high probability
- \*  $\exists$  classes of problems (**sampling problems**) which are classically hard but quantum “easy”

↑  
Google “Quantum Supremacy”

Expert insight into current research

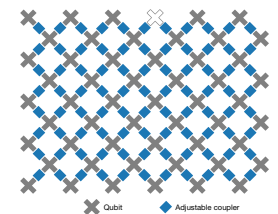
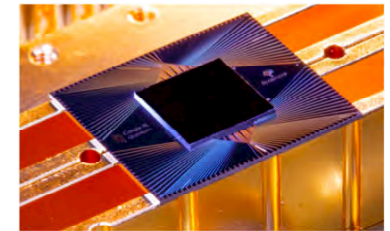
## News & views

Quantum information

### Quantum computing takes flight

William D. Oliver

A programmable quantum computer has been reported to outperform the most powerful conventional computers in a specific task – a milestone in computing comparable in importance to the Wright brothers’ first flights. See p.505



# Introduction and Overview (Preskills Notes)

Quantum Algorithms look for global properties of functions – **symmetry, periodicity, etc.**

\* Classical → requires many function evaluations

\* Quantum → design **U** so measurement gives answer with high probability

\* ∃ classes of problems (**sampling problems**) which are classically hard but quantum “easy”

Google “Quantum Supremacy”

Expert insight into current research

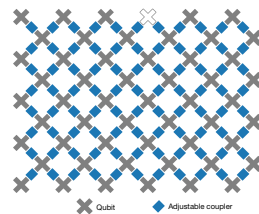
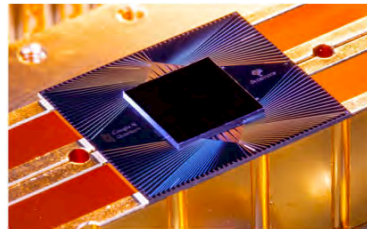
## News & views

Quantum information

## Quantum computing takes flight

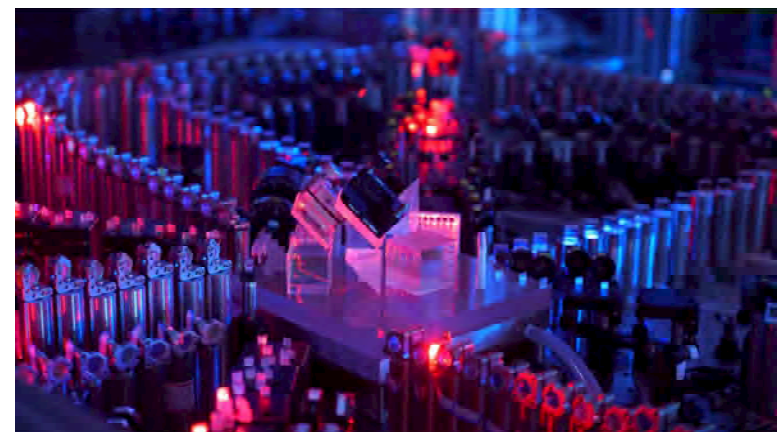
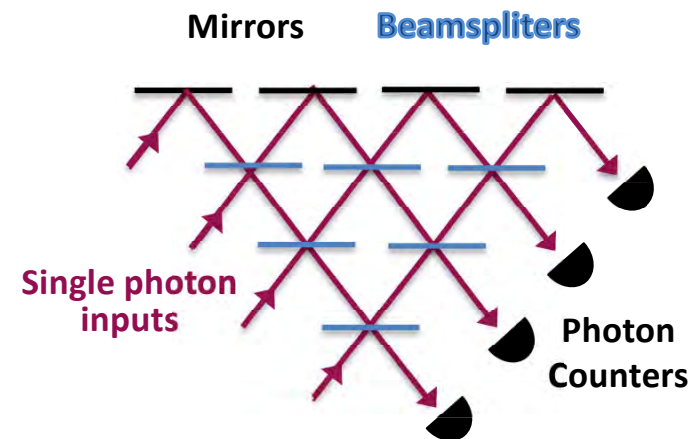
William D. Oliver

A programmable quantum computer has been reported to outperform the most powerful conventional computers in a specific task – a milestone in computing comparable in importance to the Wright brothers’ first flights. See p.505



## Boson Sampling

An example from Optics/Photonics Setup

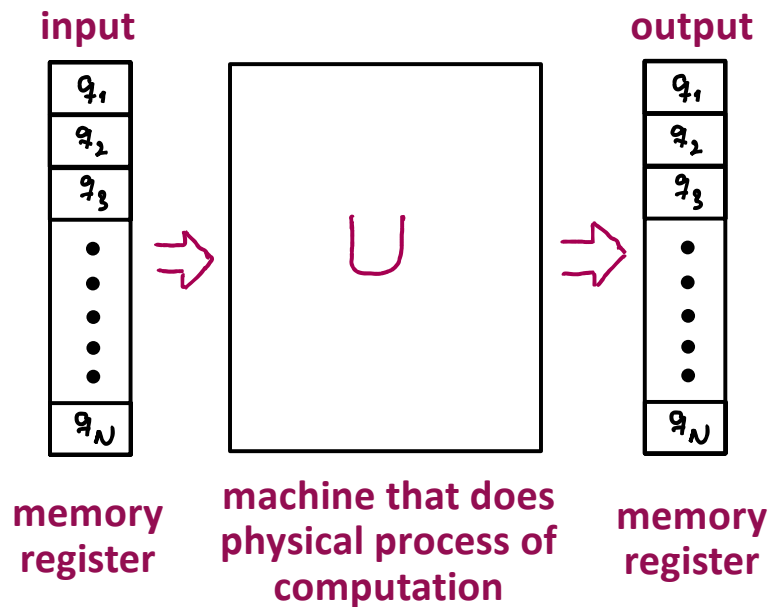


An optical quantum computer developed by a team of Chinese researchers including those from the University of Science and Technology of China. (courtesy of Han-Sen Zhong of the research group)

# Introduction and Overview (Preskills Notes)

## Back to Universal Computation

### Visualization of Computation



Classical: Register is in one of the logical states

$$x = q_1 q_2 q_3 \dots q_N$$

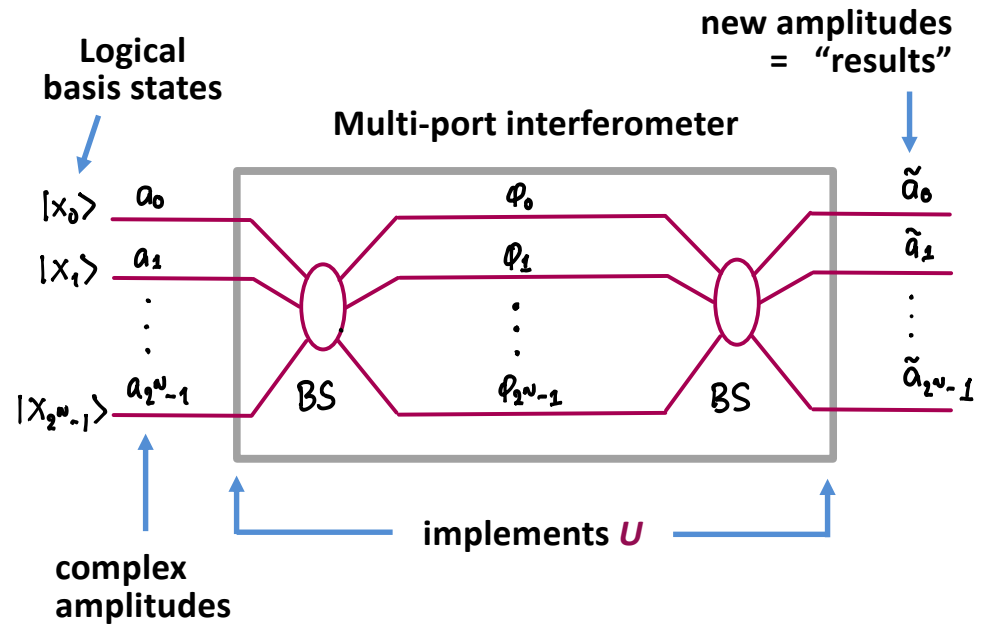
binary #

Reversible transformation

$$U: x \rightarrow y$$

## What might be inside the machine ?

Wave interference w/classical fields ?



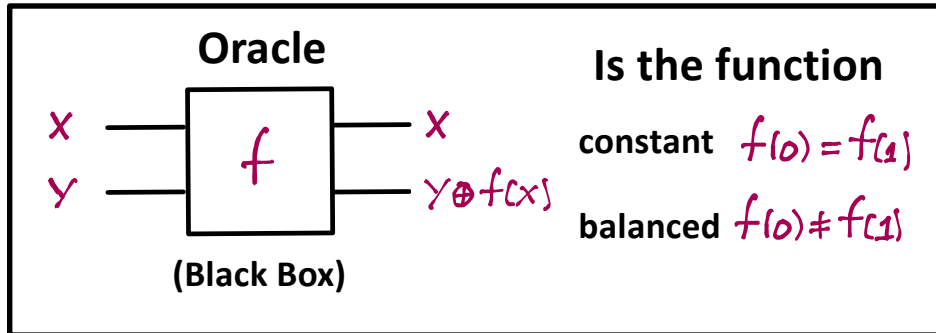
Note:  $N$  - qubit register  $\Rightarrow 2^N$  "paths"

**Beware of Resource Scaling !**

End 08-28-2023

## Quantum Advantage

David Deutsch: Toy problem that shows Quantum Advantage



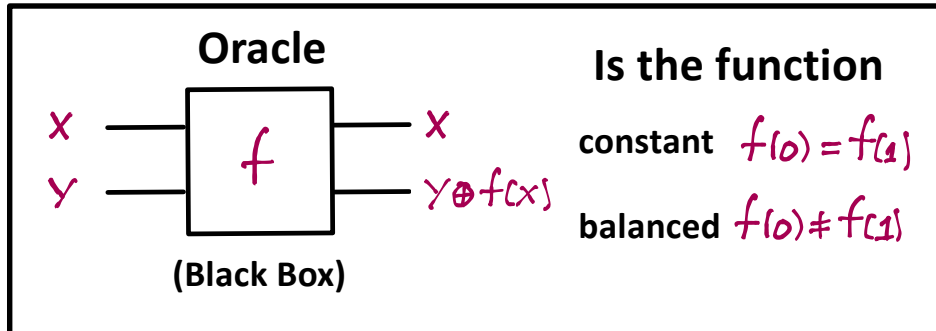
Classical Box: Need 2 queries  $f(0)$  &  $f(1)$

# Introduction and Overview (Preskills Notes)

## Quantum Advantage

David Deutsch:

Toy problem that shows Quantum Advantage



Quantum Box: In 3 steps can show that

$$(1) U_f: |x\rangle|y\rangle \rightarrow |x\rangle|y \oplus f(x)\rangle$$

$$(2) U_f: |x\rangle \frac{1}{\sqrt{2}}(|0\rangle - |1\rangle) \rightarrow |x\rangle \frac{1}{\sqrt{2}}(|f(x)\rangle - |1 \oplus f(x)\rangle)$$

$$= |x\rangle \frac{1}{\sqrt{2}} (-1)^{f(x)} (|0\rangle - |1\rangle)$$

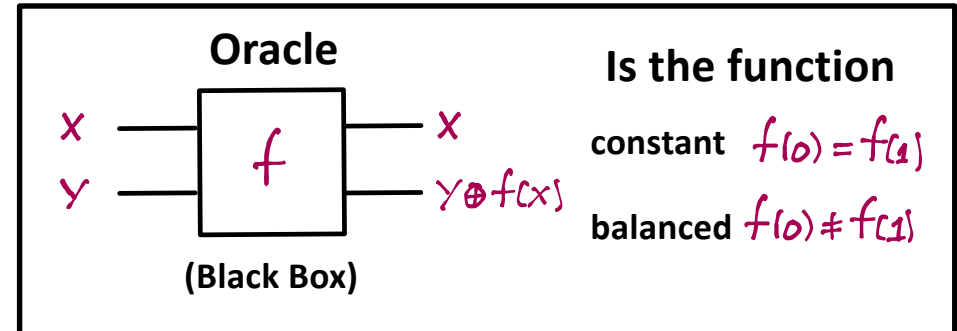
$$(3) U_f: \frac{1}{\sqrt{2}}(|0\rangle + |1\rangle) \frac{1}{\sqrt{2}}(|0\rangle - |1\rangle)$$

$$\rightarrow \frac{1}{2} \left( (-1)^{f(0)} |0\rangle + (-1)^{f(1)} |1\rangle \right) (|0\rangle - |1\rangle)$$

## Quantum Advantage

David Deutsch:

Toy problem that shows Quantum Advantage



Quantum Computation:

Input  $|x\rangle|y\rangle = \frac{1}{\sqrt{2}}(|0\rangle + |1\rangle) \frac{1}{\sqrt{2}}(|0\rangle - |1\rangle)$

$$U_f: \frac{1}{2} \left( (-1)^{f(0)} |0\rangle + (-1)^{f(1)} |1\rangle \right) (|0\rangle - |1\rangle)$$

Measure 1<sup>st</sup> qubit in basis  $| \pm \rangle = \frac{1}{\sqrt{2}} (|0\rangle \pm |1\rangle)$

$\rightarrow |+\rangle$  if constant,  $|-\rangle$  if balanced

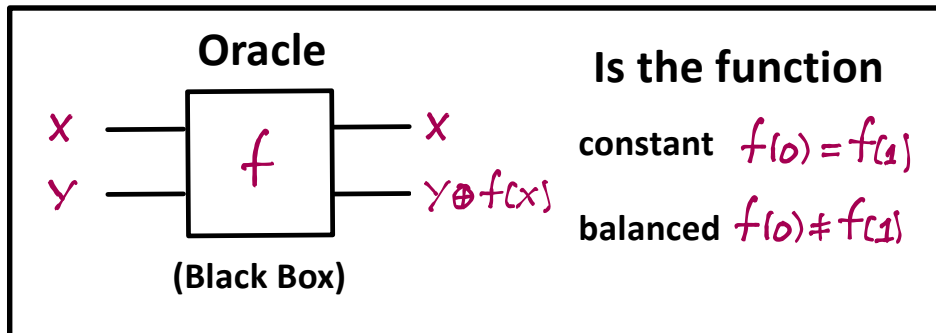
Quantum Speedup: can solve w/1 query

# Introduction and Overview (Preskills Notes)

## Quantum Advantage

David Deutsch:

Toy problem that shows Quantum Advantage



## Quantum Computation:

Input  $|x\rangle|y\rangle = \frac{1}{\sqrt{2}}(|0\rangle + |1\rangle) \frac{1}{\sqrt{2}}(|0\rangle - |1\rangle)$

$$U_f: \frac{1}{2} \left( (-1)^{f(0)} |0\rangle + (-1)^{f(1)} |1\rangle \right) (|0\rangle - |1\rangle)$$

Measure 1<sup>st</sup> qubit in basis  $| \pm \rangle = \frac{1}{\sqrt{2}} (|0\rangle \pm |1\rangle)$

→  $|+\rangle$  if constant,  $|-\rangle$  if balanced

Quantum Speedup: can solve w/1 query

Key aspect of Deutsch's algorithm:  
 We are looking for a global property of the function  $f$

Generally:  $U_f: |x\rangle|0\rangle \rightarrow |x\rangle|f(x)\rangle$

Input  $| \psi_{in} \rangle = \left[ \frac{1}{\sqrt{2}} (|0\rangle + |1\rangle) \right]^{\otimes N} |0\rangle$

$$= \frac{1}{2^{N/2}} \sum_{x=0}^{2^N-1} |x\rangle|0\rangle$$

compute once

Output  $| \psi_{out} \rangle = \frac{1}{2^{N/2}} \sum_{x=0}^{2^N-1} |x\rangle|f(x)\rangle$

Global properties encoded in state, trick is to extract desired information

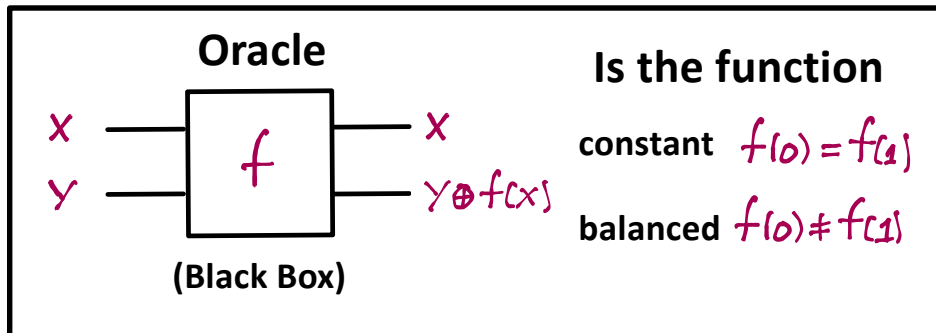


# Introduction and Overview (Preskills Notes)

## Quantum Advantage

David Deutsch:

Toy problem that shows Quantum Advantage



### Quantum Computation:

Input  $|x\rangle|y\rangle = \frac{1}{\sqrt{2}}(|0\rangle + |1\rangle) \frac{1}{\sqrt{2}}(|0\rangle - |1\rangle)$

$$U_f: \frac{1}{2} \left( (-1)^{f(0)} |0\rangle + (-1)^{f(1)} |1\rangle \right) (|0\rangle - |1\rangle)$$

Measure 1<sup>st</sup> qubit in basis  $| \pm \rangle = \frac{1}{\sqrt{2}} (|0\rangle \pm |1\rangle)$

→  $|+\rangle$  if constant,  $|-\rangle$  if balanced

Quantum Speedup: can solve w/1 query

Key aspect of Deutsch's algorithm:  
 We are looking for a global property of the function  $f$

Generally:  $U_f: |x\rangle|0\rangle \rightarrow |x\rangle|f(x)\rangle$

Input  $| \psi_{in} \rangle = \left[ \frac{1}{\sqrt{2}} (|0\rangle + |1\rangle) \right]^{\otimes N} |0\rangle$

$$= \frac{1}{2^{N/2}} \sum_{x=0}^{2^N-1} |x\rangle|0\rangle$$

compute once

Output  $| \psi_{out} \rangle = \frac{1}{2^{N/2}} \sum_{x=0}^{2^N-1} |x\rangle|f(x)\rangle$

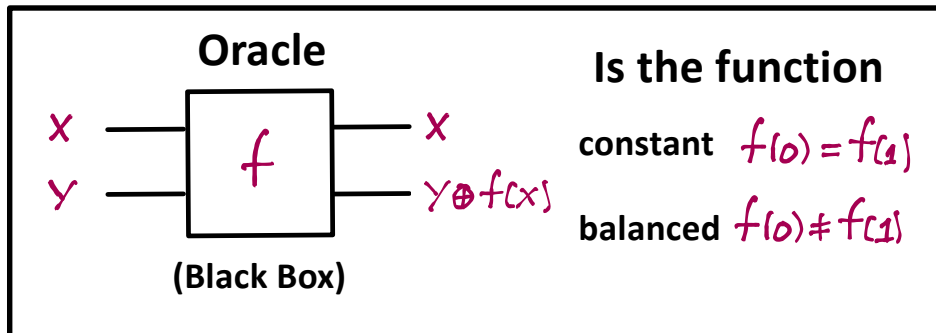
Global properties encoded in state, trick is to extract desired information

# Introduction and Overview (Preskills Notes)

## Quantum Advantage

David Deutsch:

Toy problem that shows Quantum Advantage



## Quantum Computation:

Input  $|x\rangle|y\rangle = \frac{1}{\sqrt{2}}(|0\rangle + |1\rangle) \frac{1}{\sqrt{2}}(|0\rangle - |1\rangle)$

$$U_f: \frac{1}{2} \left( (-1)^{f(0)} |0\rangle + (-1)^{f(1)} |1\rangle \right) (|0\rangle - |1\rangle)$$

Measure 1<sup>st</sup> qubit in basis  $| \pm \rangle = \frac{1}{\sqrt{2}} (|0\rangle \pm |1\rangle)$

→  $|+\rangle$  if constant,  $|-\rangle$  if balanced

Quantum Speedup: can solve w/1 query

Key aspect of Deutsch's algorithm:

We are looking for a global property of the function  $f$

Generally:  $U_f: |x\rangle|0\rangle \rightarrow |x\rangle|f(x)\rangle$

Input  $| \psi_{in} \rangle = \left[ \frac{1}{\sqrt{2}} (|0\rangle + |1\rangle) \right]^{\otimes N} |0\rangle$

$$= \frac{1}{2^{N/2}} \sum_{x=0}^{2^N-1} |x\rangle|0\rangle$$

compute once

Output  $| \psi_{out} \rangle = \frac{1}{2^{N/2}} \sum_{x=0}^{2^N-1} |x\rangle|f(x)\rangle$

Peter Shor: Period finding, QFT, Factoring

# Introduction and Overview (Preskills Notes)

Key aspect of Deutsch's algorithm:  
We are looking for a global property  
of the function  $f$

Generally:  $U_f: |x\rangle|0\rangle \rightarrow |x\rangle|f(x)\rangle$   
*N bit binary number*

Input  $|q_{in}\rangle = \left[ \frac{1}{\sqrt{2}} (|0\rangle + |1\rangle) \right]^{\otimes N} |0\rangle$

$$= \frac{1}{2^{N/2}} \sum_{x=0}^{2^N-1} |x\rangle|0\rangle$$

compute once

Output  $|q_{out}\rangle = \frac{1}{2^{N/2}} \sum_{x=0}^{2^N-1} |x\rangle|f(x)\rangle$

Peter Shor: Period finding,  
QFT, Factoring

Next: Will this work with real-world  
Quantum Hardware ?

Faulty gates, decoherence !

# Introduction and Overview (Preskills Notes)

## Quantum Error Correction

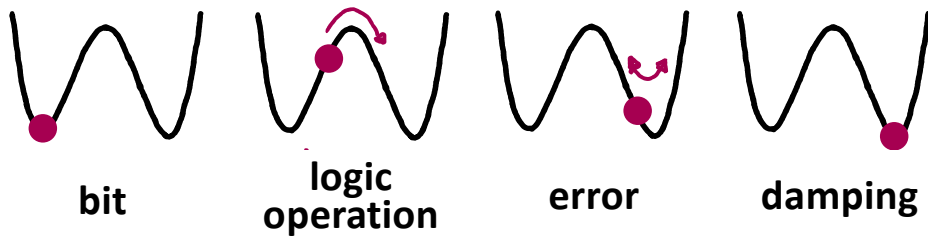
Fundamental Problem



Quantum States are fragile, especially when entangled

Classical Computation ?

Dissipation helps



No dissipation →

Errors build up

Quantum Computation →

- \* Cannot tolerate dissipation
- \* Destroys superposition and entanglement

What to do? **Error Correction!**

## Classical Error Correction:

Simple example: Redundancy protects against bit flips

Encode:  
 $0 \rightarrow (000)$   
 $1 \rightarrow (111)$

Errors:  
 $(000) \rightarrow (100)$   
 $(111) \rightarrow (011)$  correct by majority vote

# Introduction and Overview (Preskills Notes)

## Quantum Computation

- \* Cannot tolerate dissipation
- \* Destroys superposition and entanglement

What to do? **Error Correction!**

## Classical Error Correction:

Simple example: Redundancy protects against bit flips



Encode:  $0 \rightarrow (000)$   
 $1 \rightarrow (111)$

Errors:  $(000) \rightarrow (100)$   
 $(111) \rightarrow (011)$  correct by majority vote

## Von Neumann:

- \* A classical computer w/faulty components can work, given enough redundancy
- \* Classical error correction is well developed and highly sophisticated...

## \* Quantum Errors

- 1) Bit Flip  $|0\rangle \rightarrow |1\rangle$ , phase flip  $|0\rangle \rightarrow |0\rangle$   
 $|1\rangle \rightarrow |0\rangle$ ,  $|1\rangle \rightarrow -|1\rangle$
- 2) Small errors  $a|0\rangle + b|1\rangle$   $a, b$  can change by  $\epsilon$   
errors accumulate
- 3) Measurement disturbs  collapse of quantum states
- 4) No cloning  Cannot protect by making copies

# Introduction and Overview (Preskills Notes)

## Von Neumann:

- \* A classical computer w/faulty components can work, given enough redundancy
- \* Classical error correction is well developed and highly sophisticated...

## \* Quantum Errors

- 1) Bit Flip  $|0\rangle \rightarrow |1\rangle$ , phase flip  $|0\rangle \rightarrow |0\rangle$   
 $|1\rangle \rightarrow |0\rangle$ ,  $|1\rangle \rightarrow -|1\rangle$
- 2) Small errors  $a|0\rangle + b|1\rangle$   $a, b$  can change by  $\epsilon$   
 errors accumulate
- 3) Measurement disturbs  $\Rightarrow$  collapse of quantum states
- 4) No cloning  $\Rightarrow$  Cannot protect by making copies

Example: Peter Shor's code for bit flip error when  $P(\text{error}) \ll 1$

Encode:  $|0\rangle \rightarrow |0\rangle \equiv |000\rangle$  (3 bit code)  
 $|1\rangle \rightarrow |1\rangle \equiv |111\rangle$

$$a|0\rangle + b|1\rangle \rightarrow a|000\rangle + b|111\rangle$$

Single-qubit measurement  $\Rightarrow$

collapse of state, destroys info, no majority voting!

## Collective 2-qubit measurement:

- for  $|x, y, z\rangle$  measure  $y \oplus z$  (never measure individual bits)  
 $x \oplus z$
- if  $|000\rangle, |111\rangle$  these observables = 0
- if one bit-flip, at least one observable = 1
- easy to check that  $(y \oplus z, x \oplus z) =$  binary address of qubit flip

$$|000\rangle \rightarrow |010\rangle \quad (1, 0) = \text{2nd bit}$$

# Introduction and Overview (Preskills Notes)

**Example:** Peter Shor's code for bit flip error when  $P(\text{error}) \ll 1$

**Encode:**  $|0\rangle \rightarrow |\bar{0}\rangle \equiv |000\rangle$  (3 bit code)  
 $|1\rangle \rightarrow |\bar{1}\rangle \equiv |111\rangle$

$$a|0\rangle + b|1\rangle \rightarrow a|000\rangle + b|111\rangle$$

Single-qubit measurement



collapse of state, destroys info, no majority voting!

## Collective 2-qubit measurement:

- for  $|x, y, z\rangle$  measure  $y \oplus z$  (never measure individual bits)  
 $x \oplus z$

- if  $|000\rangle, |111\rangle$  these observables = 0

- if one bit-flip, at least one observable = 1

- easy to check that  $(y \oplus z, x \oplus z) =$  binary address of qubit flip

$$|000\rangle \rightarrow |010\rangle \quad (1, 0) = \text{2nd bit}$$

**Small errors:**  $|000\rangle \rightarrow |000\rangle + \epsilon|100\rangle$   
 $|111\rangle \rightarrow |111\rangle + \epsilon|110\rangle$

**Quantum mechanics to the rescue !**

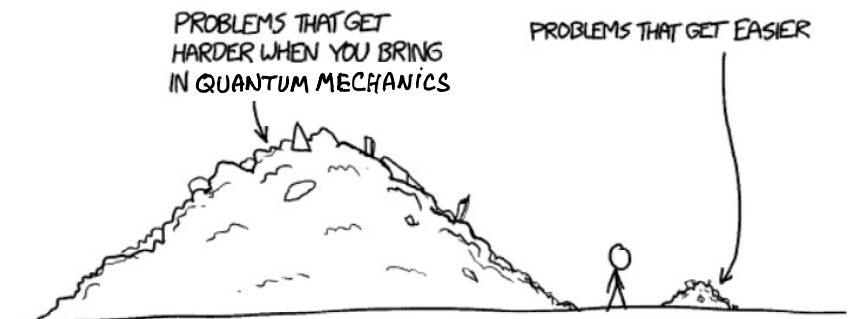
- mostly no error detected

➡ collapse into  $|000\rangle$  resp.  $|111\rangle$

- sometime error detected

➡ collapse into  $|001\rangle$  resp.  $|110\rangle$

➡ full bit flip, correct as such



Source: xkcd.com

# Introduction and Overview (Preskills Notes)

**Example:** Peter Shor's code for bit flip error when  $P(\text{error}) \ll 1$

**Encode:**  $|0\rangle \rightarrow |\bar{0}\rangle \equiv |000\rangle$  (3 bit code)  
 $|1\rangle \rightarrow |\bar{1}\rangle \equiv |111\rangle$

$$a|0\rangle + b|1\rangle \rightarrow a|000\rangle + b|111\rangle$$

Single-qubit measurement



collapse of state,  
destroys info,  
no majority voting!

## Collective 2-qubit measurement:

- for  $|x, y, z\rangle$  measure  $y \oplus z$  (never measure individual bits)  
 $x \oplus z$

- if  $|000\rangle, |111\rangle$  these observables = 0

- if one bit-flip, at least one observable = 1

- easy to check that  $(y \oplus z, x \oplus z) =$  binary address of qubit flip

$$|000\rangle \rightarrow |010\rangle \quad (1, 0) = \text{2nd bit}$$

**Small errors:**  $|000\rangle \rightarrow |000\rangle + \epsilon|100\rangle$   
 $|111\rangle \rightarrow |111\rangle + \epsilon|110\rangle$

**Quantum mechanics to the rescue !**

- mostly no error detected

➡ collapse into  $|000\rangle$  resp.  $|111\rangle$

- sometime error detected

➡ collapse into  $|001\rangle$  resp.  $|110\rangle$

➡ full bit flip, correct as such

## How to implement ?

Quantum circuit + single qubit measurement

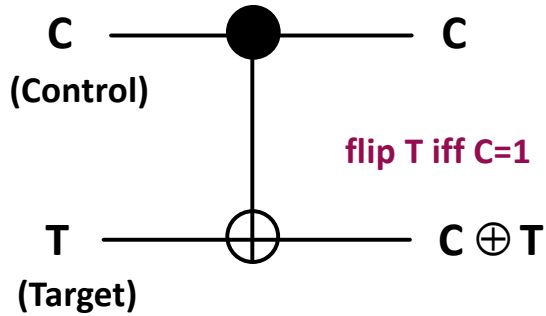
Quantum Gates – work on superpositions,  
and entangled states



# Introduction and Overview (Preskills Notes)

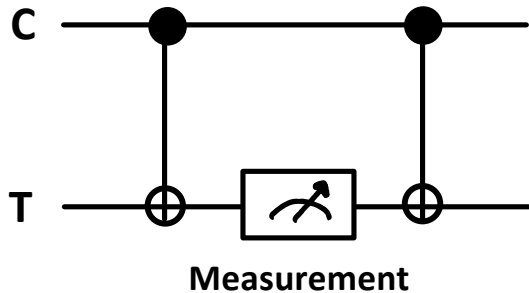
## Controlled-NOT (CNOT)

## Truth Table



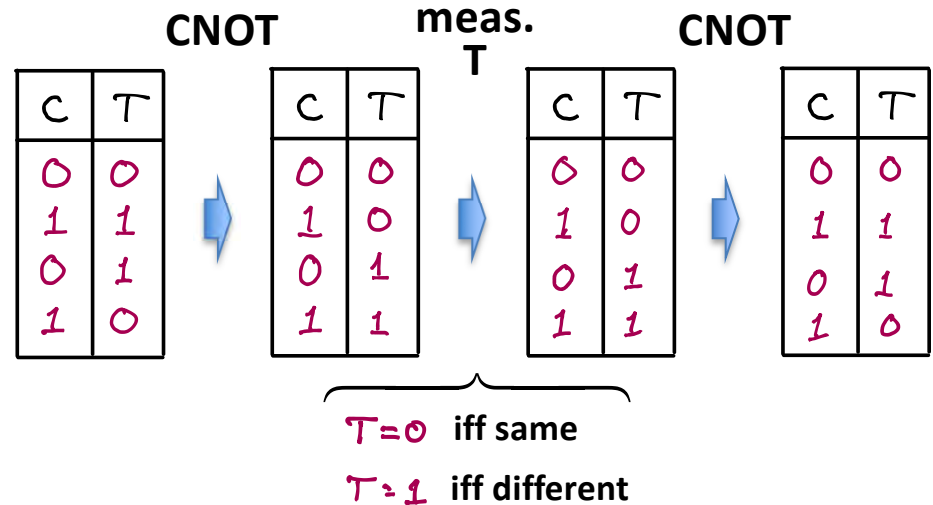
C	T	$C \oplus T$
0	0	0
0	1	1
1	0	1
1	1	0

## Quantum Circuit for joint measurement

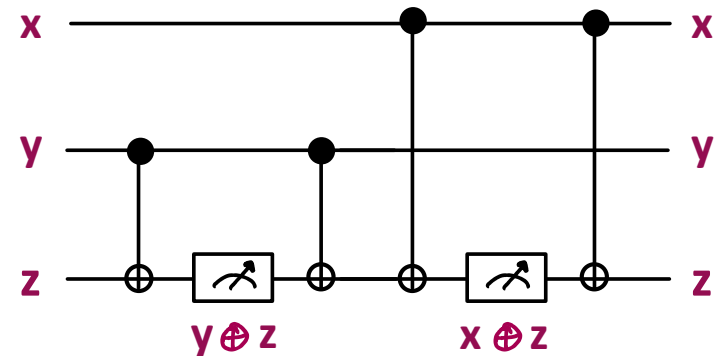


Measurement in  $\{|0\rangle, |1\rangle\}$  basis  
yields  $C \oplus T$

## Circuit maps logical basis states as



## Full circuit to obtain Error Syndrome



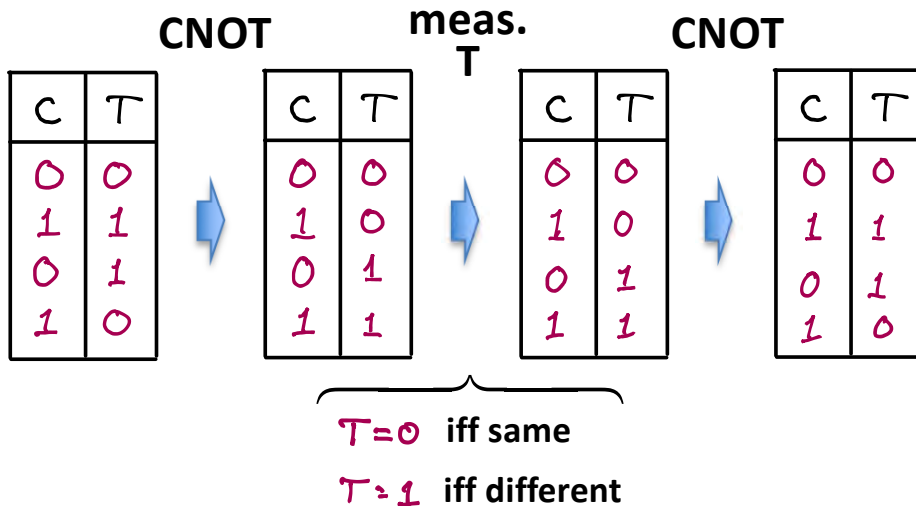
\* iff qubit flip, binary address =  $(y \oplus z, x \oplus z)$

End 09-01-2023

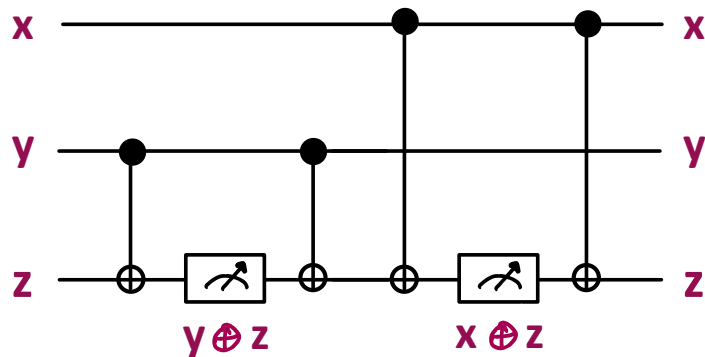
# Introduction and Overview (Preskills Notes)

Begin  
09-06-2023

Circuit maps logical basis states as



Full circuit to obtain Error Syndrome



\* iif qubit flip, binary address =  $(y \oplus z, x \oplus z)$

End 09-01-2023

Quantum Phase Error

$$\begin{aligned} |0\rangle &\rightarrow |0\rangle \\ |1\rangle &\rightarrow -|1\rangle \end{aligned}$$

Encoding

$$\begin{aligned} |0\rangle &\rightarrow |\bar{0}\rangle = \frac{1}{2^{3/2}} (|0\rangle + |1\rangle)^{x'} (|0\rangle + |1\rangle)^{y'} (|0\rangle + |1\rangle)^{z'} \\ |1\rangle &\rightarrow |\bar{1}\rangle = \frac{1}{2^{3/2}} (|0\rangle - |1\rangle)^{x'} (|0\rangle - |1\rangle)^{y'} (|0\rangle - |1\rangle)^{z'} \end{aligned}$$

Relabel

$$\begin{aligned} \frac{1}{\sqrt{2}} (|0\rangle + |1\rangle) &= |0'\rangle \\ \frac{1}{\sqrt{2}} (|0\rangle - |1\rangle) &= |1'\rangle \end{aligned}$$

Measure in basis

$$\{|0'\rangle, |1'\rangle\} \rightarrow y' \oplus z', x' \oplus z'$$

Error Syndrome

\* Iff phase error, binary address =  $(y' \oplus z', x' \oplus z')$

\* Analogous to bit-flip code, just in different basis

# Introduction and Overview (Preskills Notes)

Quantum Phase Error       $|0\rangle \rightarrow |0\rangle$   
    $|1\rangle \rightarrow -|1\rangle$

## Encoding

$$|0\rangle \rightarrow |\bar{0}\rangle = \frac{1}{2^{3/2}} (|0\rangle + |1\rangle)^{x'} (|0\rangle + |1\rangle)^{y'} (|0\rangle + |1\rangle)^{z'}$$
$$|1\rangle \rightarrow |\bar{1}\rangle = \frac{1}{2^{3/2}} (|0\rangle - |1\rangle)^{x'} (|0\rangle - |1\rangle)^{y'} (|0\rangle - |1\rangle)^{z'}$$

Relabel       $\frac{1}{\sqrt{2}} (|0\rangle + |1\rangle) = |0'\rangle$   
                  $\frac{1}{\sqrt{2}} (|0\rangle - |1\rangle) = |1'\rangle$

Measure in basis       $\{|0'\rangle, |1'\rangle\} \rightarrow y' \oplus z', x' \oplus z'$

## Error Syndrome

- \* Iff phase error, binary address =  $(y' \oplus z', x' \oplus z')$
- \* Analogous to bit-flip code, just in different basis

## Shor's 9-bit code

- \* Combines flip/phase error correction
- \* Corrects one flip or phase error

## General principle of error correction

- \* Encode  $p$  logical qubits in  $n$  physical qubits.
- \* Valid Logical States form  $2^p$ -dimensional subspace  $\mathcal{E}_p$  (code space) in  $n$ -qubit ( $2^n$ -dimensional) Hilbert space  $\mathcal{E}_N$
- \* Errors displace system into orthogonal (distinguishable) subspaces.

# Introduction and Overview (Preskills Notes)

## Shor's 9-bit code

- \* Combines flip/phase error correction
- \* Corrects one flip or phase error

## General principle of error correction

- \* Encode  $p$  logical qubits in  $n$  physical qubits.
- \* Valid Logical States form  $2^p$ -dimensional subspace  $\mathcal{E}_p$  (code space) in  $n$ -qubit ( $2^n$ -dimensional) Hilbert space  $\mathcal{E}_N$
- \* Errors displace system into orthogonal (distinguishable) subspaces.

# Introduction and Overview (Preskills Notes)

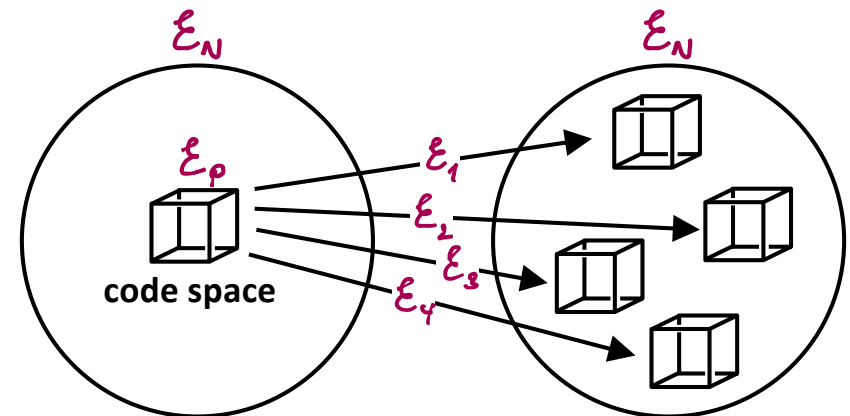
## Shor's 9-bit code

- \* Combines flip/phase error correction
- \* Corrects one flip or phase error

## General principle of error correction

- \* Encode  $p$  logical qubits in  $n$  physical qubits.
- \* Valid Logical States form  $2^p$ -dimensional subspace  $\mathcal{E}_p$  (code space) in  $n$ -qubit ( $2^n$ -dimensional) Hilbert space  $\mathcal{E}_N$
- \* Errors displace system into orthogonal (distinguishable) subspaces.

## Geometric illustration



## What about non-Unitary errors?

e. g., decay

$$|0\rangle \rightarrow |0\rangle$$

$$|1\rangle \rightarrow |0\rangle$$

Problem: Errors not displaced into orthogonal subspaces

Solution: "Quantum jump codes", monitors the environment

## Other kinds of errors?

# Introduction and Overview (Preskills Notes)

# Catnip for Theoretical Physicists & Computer Scientists

Showing 1–50 of 2,143 results

Search v0.5.6 released 2020-02-24 [Feedback?](#)

Query: order: announced\_date\_first; size: 50; include\_cross\_list: True; terms: AND all="Quantum Error Correction"

[Simple Search](#)

[Refine query](#)

[New search](#)

50 results per page. Sort results by Announcement date (oldest first) [Go](#)

1 2 3 4 5

[Next](#)

1. [arXiv:quant-ph/9511003](#) [[pdf](#), [ps](#), [other](#)] [quant-ph](#)  
**Quantum Error Correction by Coding**  
**Authors:** I. L. Chuang, R. Laflamme  
**Abstract:** ...cryptography and quantum computers has given hope to their imminent practical realization. An essential element at the heart of the application of these quantum systems is a **quantum error correction** scheme. We propose a new technique based on the use of coding in order to detect... [More](#)  
**Submitted** 3 November, 1995; **originally announced** November, 1995.  
**Comments:** 11 pages RevTeX + 2 figures in postscript; Please see <http://feynman.stanford.edu/qcomp/> for figures.
2. [arXiv:quant-ph/9512032](#) [[pdf](#), [ps](#), [other](#)] [quant-ph](#) [doi](#) 10.1103/PhysRevA.54.1098  
**Good Quantum Error-Correcting Codes Exist**  
**Authors:** A. R. Calderbank, Peter W. Shor  
**Abstract:** A **quantum**... [More](#)  
**Submitted** 16 April, 1996; **v1** submitted 30 December, 1995; **originally announced** December 1995.  
**Comments:** Latex, 23 pages, 1 figure. Revised April 1996 to give more intuition and an example. Submitted to Phys. Rev. A  
**Journal ref:** Phys. Rev. A, Vol. 54, No. 2, pp. 1098-1106, 1996
3. [arXiv:quant-ph/9601029](#) [[pdf](#), [ps](#), [other](#)] [quant-ph](#) [doi](#) 10.1098/rspa.1996.0136

# Catnip for Theoretical Physicists & Computer Scientists



We gratefully acknowledge support from the Simons Foundation and member institutions.



Search:  All fields

[Help](#) | [Advanced Search](#)

[Login](#)

Showing 1–50 of 2,143 results

Search v0.5.6 released 2020-02-24 [Feedback?](#)

Query: order: -announced\_date\_first; size: 50; include\_cross\_list: True; terms: AND all="Quantum Error Correction"

[Simple Search](#)

[Refine query](#)

[New search](#)

50 results per page. Sort results by Announcement date (newest first)

[1](#) [2](#) [3](#) [4](#) [5](#)

[Next](#)

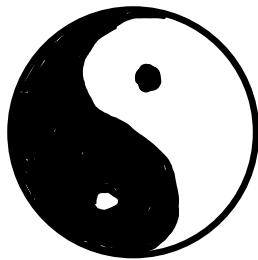
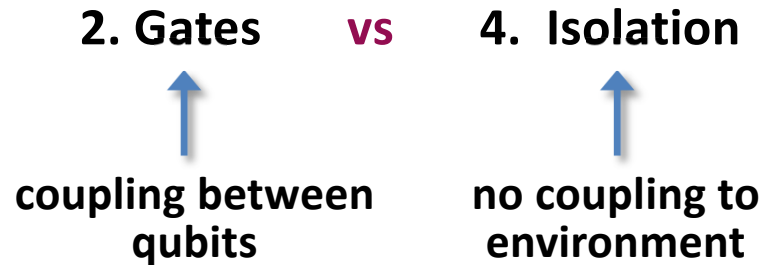
1. [arXiv:2309.00225](#) [pdf] [cond-mat.mes-hall](#) [quant-ph](#)  
**Rapid single-shot parity spin readout in a silicon double quantum dot with fidelity exceeding 99 %**  
**Authors:** Kenta Takeda, Akito Noiri, Takashi Nakajima, Leon C. Camenzind, Takashi Kobayashi, Amir Sammak, Giordano Scappucci, Seigo Tarucha  
**Abstract:** ...(with >99% fidelity) parity spin measurement in a silicon double quantum dot. These results represent a significant step forward toward implementing measurement-based **quantum error correction** in silicon. [More](#)  
**Submitted** 31 August, 2023; **originally announced** September 2023
2. [arXiv:2308.16233](#) [pdf, other] [quant-ph](#)  
**Bounds on Autonomous Quantum Error Correction**  
**Authors:** Oles Shtranko, Yu-jie Liu, Simon Liu, Alexey V. Gorshkov, Victor V. Albert  
**Abstract:** Autonomous quantum memories are a way to passively protect quantum information using engineered dissipation that creates an "always-on" decoder. We analyze Markovian autonomous decoders that can be implemented with a wide range of qubit and bosonic error-correcting codes, and derive several upper bounds and a lower bound on the logical error rate in terms of correction and noise rates. For many b... [More](#)  
**Submitted** 30 August, 2023; **originally announced** August 2023  
**Comments:** 51 pages, 8 figures, 1 table





# Introduction and Overview (Preskills Notes)

## Inherent Contradictions



To build a Quantum Computer

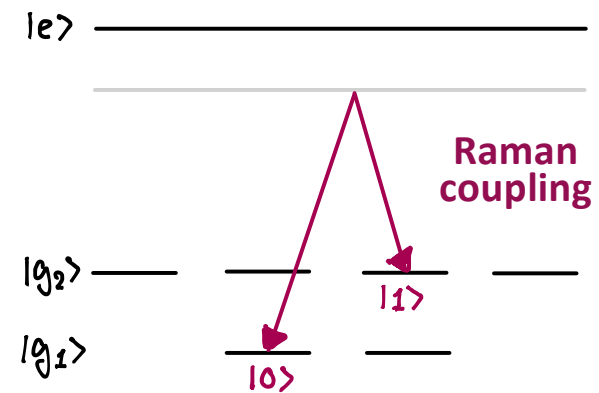


Choose, find or invent a system with acceptable tradeoffs

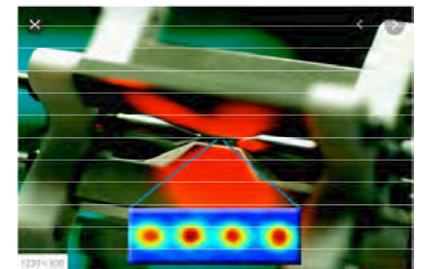
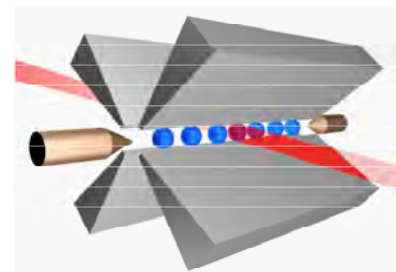
## Ion Trap Quantum Computing

First to demonstrate a Quantum Gate

- \* Qubit is encoded in the electronic ground state of an atomic ion



- \* Early design with a few ions in large trap

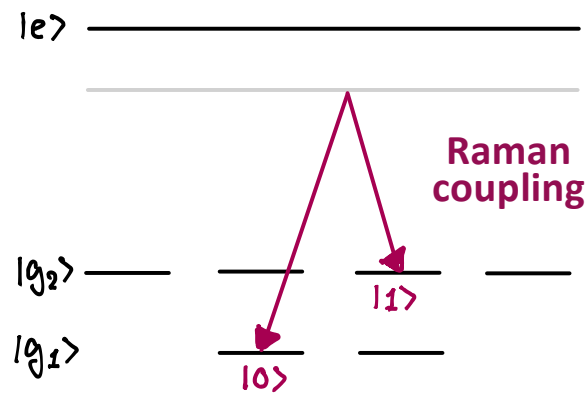


# Introduction and Overview (Preskills Notes)

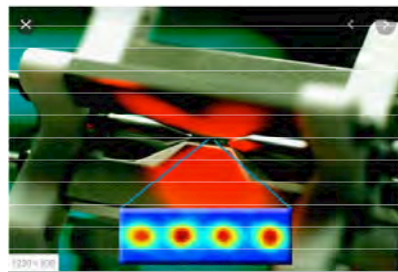
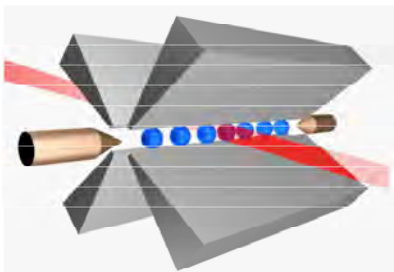
## Ion Trap Quantum Computing

First to demonstrate a Quantum Gate

- \* Qubit is encoded in the electronic ground state of an atomic ion



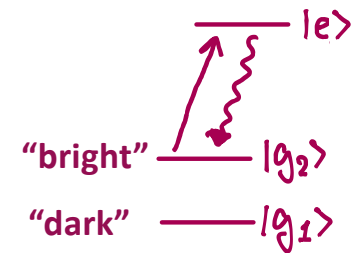
- \* Early design with a few ions in large trap



## Requirements

1. Storage: 10s-100s coherence time
2. Gates: Use collective vibrations as “quantum bus”

3. Readout: Fluorescence



Cirac & Zoller: 5 laser pulses →

CNOT gate between any 2 ions in linear array

Wineland: 3 laser pulses enough for CNOT

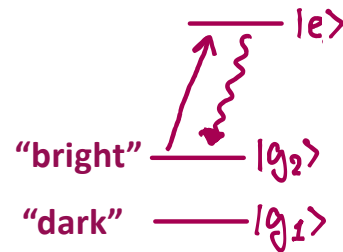
Use this example serves as conceptual template

# Introduction and Overview (Preskills Notes)

## Requirements

1. Storage: 10s-100s coherence time
2. Gates: Use collective vibrations as "quantum bus"

3. Readout: Fluorescence



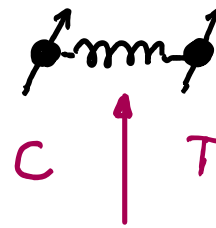
Cirac & Zoller: 5 laser pulses →

CNOT gate between any 2 ions in linear array

Wineland: 3 laser pulses enough for CNOT

Use this example serves as conceptual template

2 – ion trap



convention  
(0 = ↓, 1 = ↑)

center-of-mass mode  
is quantum bus

CNOT input-output map:

$$|\downarrow_C \downarrow_T\rangle \rightarrow |\downarrow_C \downarrow_T\rangle$$

$$|\uparrow_C \downarrow_T\rangle \rightarrow |\uparrow_C \uparrow_T\rangle$$

$$|\downarrow_C \uparrow_T\rangle \rightarrow |\downarrow_C \uparrow_T\rangle$$

$$|\uparrow_C \uparrow_T\rangle \rightarrow |\uparrow_C \downarrow_T\rangle$$

does nothing

swaps  $|\uparrow_C \downarrow_T\rangle, |\uparrow_C \uparrow_T\rangle$

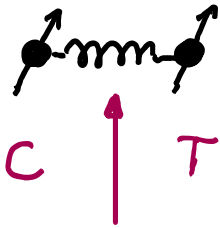
Notation for quantum states:  $|n, \sigma_C^{(z)}, \sigma_T^{(z)}\rangle$

$n$ : vibrational quantum number

$\sigma_C^{(z)}, \sigma_T^{(z)}$ : spin states of C and T ions

# Introduction and Overview (Preskills Notes)

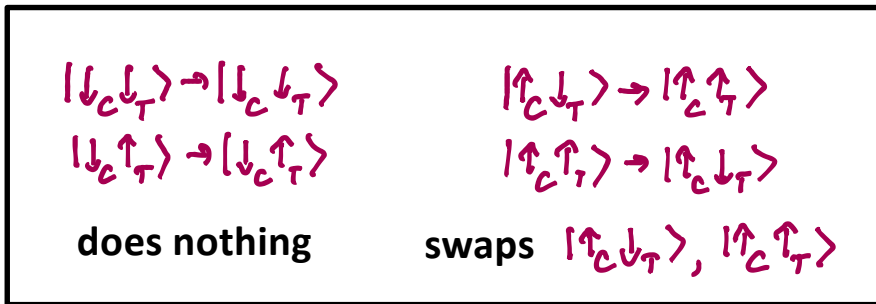
2 – ion trap



center-of-mass mode  
is quantum bus

convention  
(0 = ↓, 1 = ↑)

CNOT input-output map:

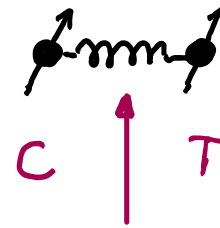


Notation for quantum states:  $|n, \sigma_C^{(z)}, \sigma_T^{(z)}\rangle$

$n$ : vibrational quantum number

$\sigma_C^{(z)}, \sigma_T^{(z)}$ : spin states of C and T ions

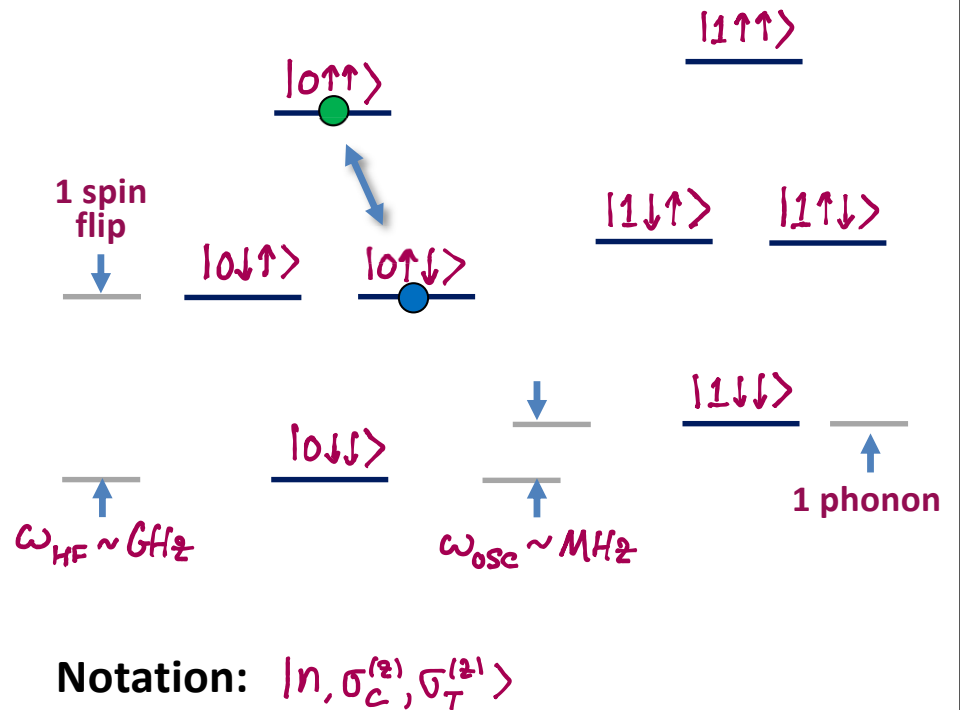
2 – ion trap



center-of-mass mode  
is quantum bus

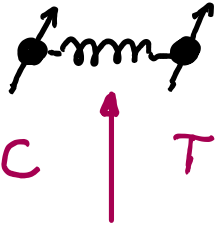
convention  
(0 = ↓, 1 = ↑)

Energy Level diagram:



# Introduction and Overview (Preskills Notes)

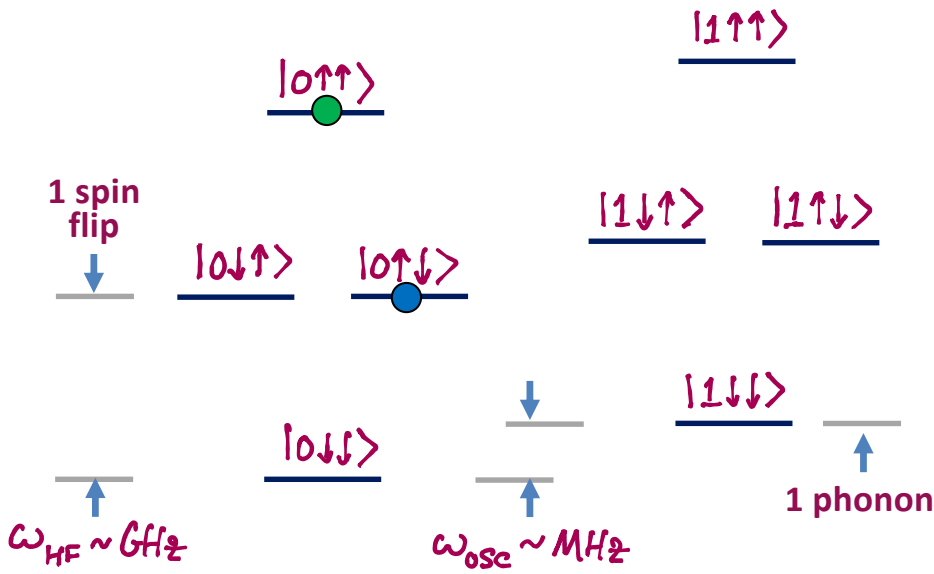
2 – ion trap



center-of-mass mode  
is quantum bus

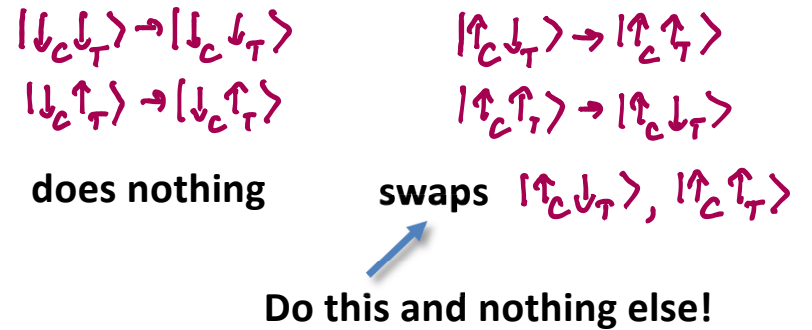
convention  
(0 = ↓, 1 = ↑)

Energy Level diagram:



Notation:  $|n, \sigma_C^{(z)}, \sigma_T^{(z)}\rangle$

CNOT input-output map:



Laser pulse sequence:

- (1)  $\pi$  pulse on C swaps  $|0↑_C X_T\rangle \leftrightarrow |1↓_C X_T\rangle$
- (2)  $\pi$  pulse on T swaps  $|1↓_C ↓_T\rangle \leftrightarrow |1↓_C ↑_T\rangle$
- (3)  $\pi$  pulse on C swaps  $|0↑_C X_T\rangle \leftrightarrow |1↓_C X_T\rangle$

Performs CNOT Gate

Let us go through the process in detail !

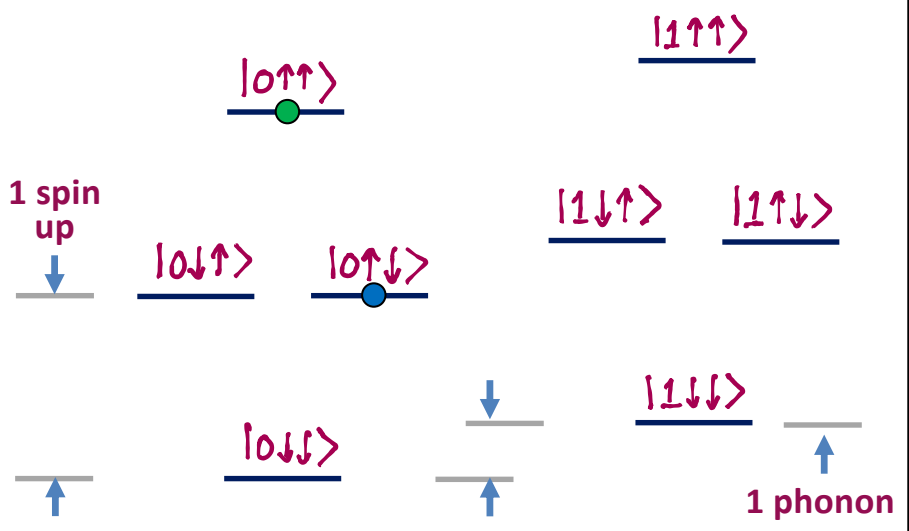
(Note: Clickthrough Panels)

# Introduction and Overview (Preskills Notes)

(1)  $\pi$  pulse on C swaps  $|0\rangle_C |x_T\rangle \leftrightarrow |1\rangle_C |x_T\rangle$

# Introduction and Overview (Preskills Notes)

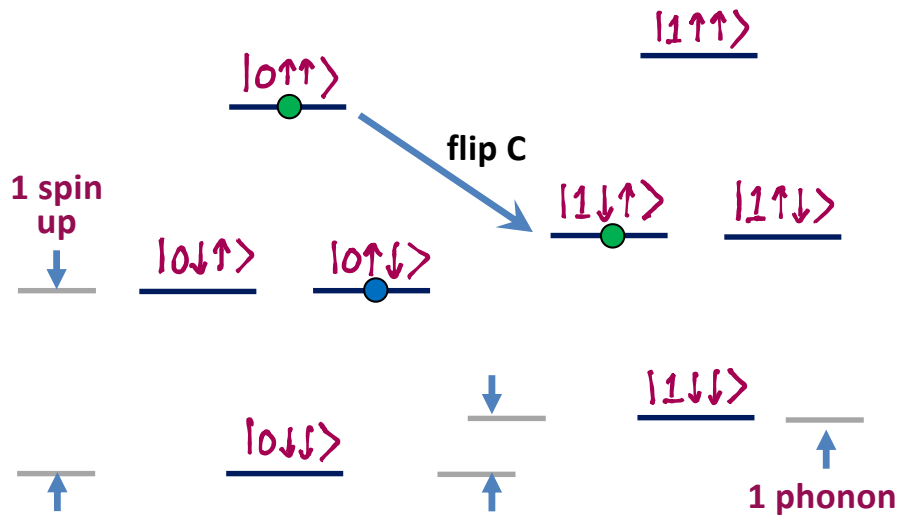
(1)  $\pi$  pulse on C swaps  $|0^{\uparrow}_c x_T\rangle \leftrightarrow |1^{\downarrow}_c x_T\rangle$





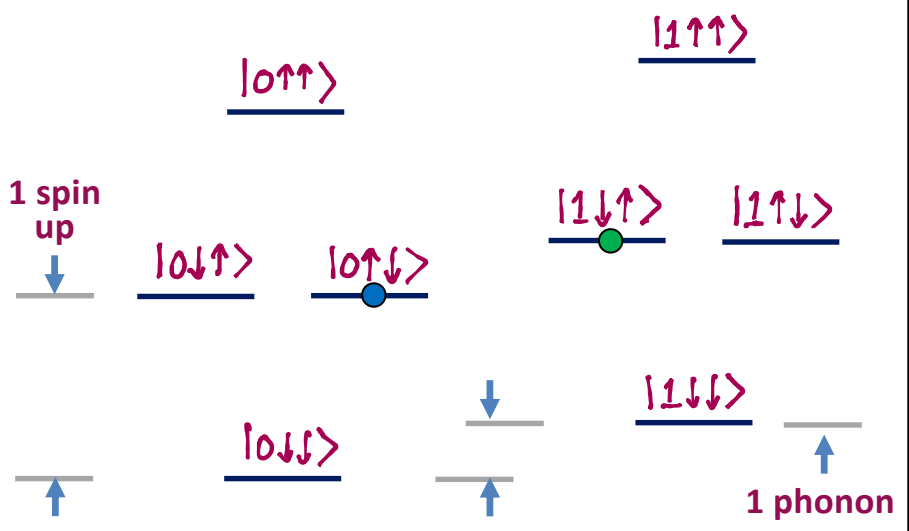
# Introduction and Overview (Preskills Notes)

(1)  $\pi$  pulse on C swaps  $|0^{\uparrow}_C X_T\rangle \leftrightarrow |1^{\downarrow}_C X_T\rangle$



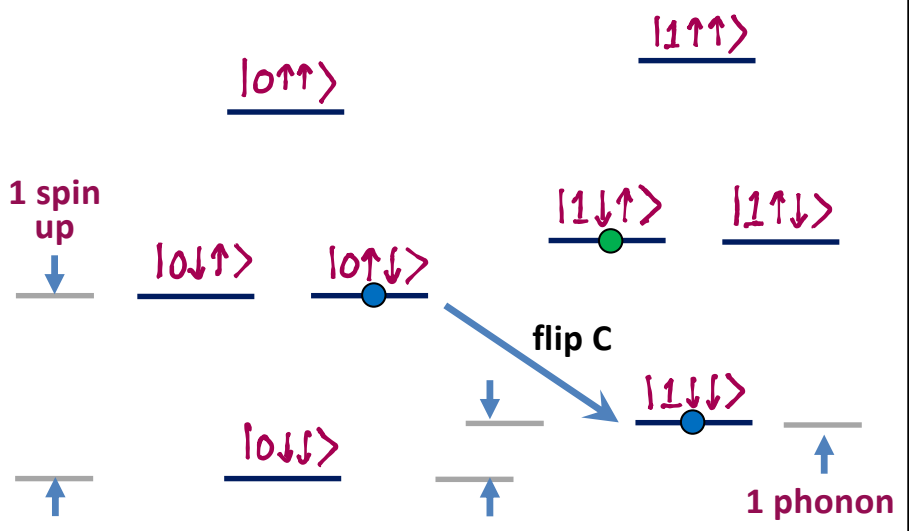
# Introduction and Overview (Preskills Notes)

(1)  $\pi$  pulse on C swaps  $|0^{\uparrow}_c x_T\rangle \leftrightarrow |1^{\downarrow}_c x_T\rangle$



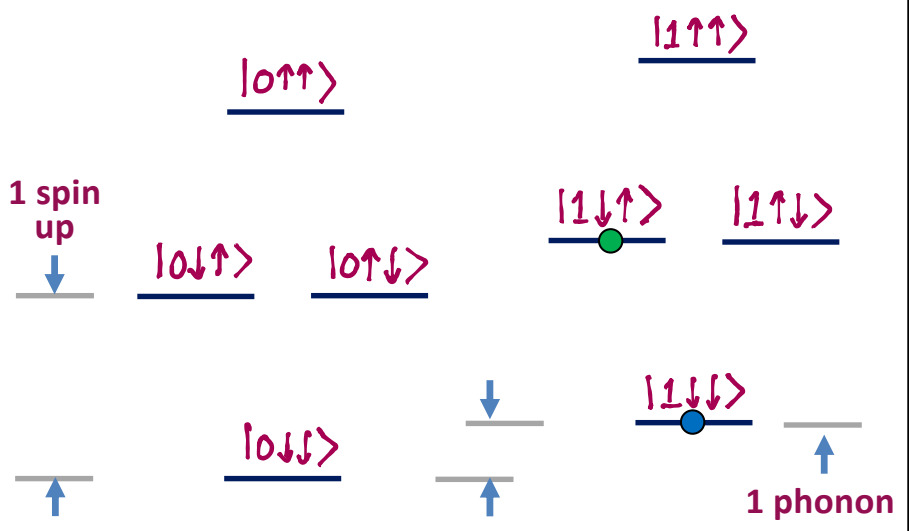
# Introduction and Overview (Preskills Notes)

(1)  $\pi$  pulse on C swaps  $|0^{\uparrow}_C X_T\rangle \leftrightarrow |1^{\downarrow}_C X_T\rangle$



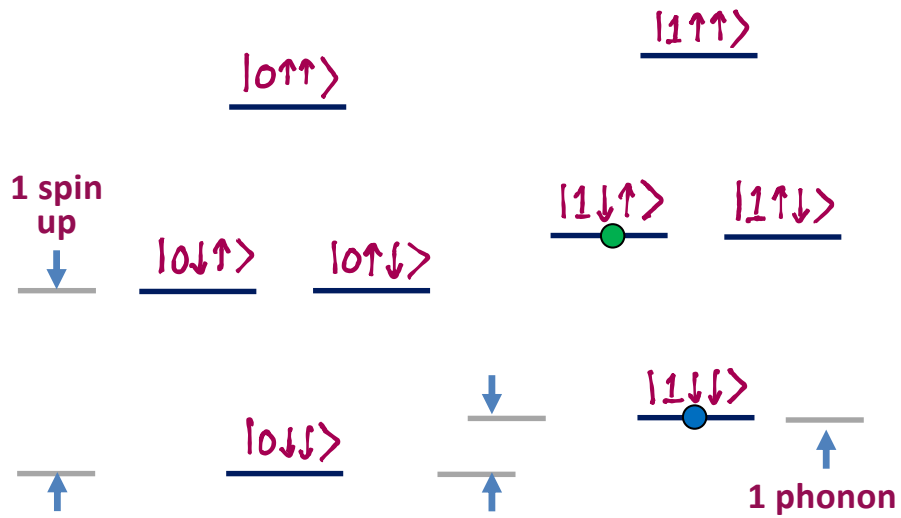
# Introduction and Overview (Preskills Notes)

(1)  $\pi$  pulse on C swaps  $|0^{\uparrow}_c x_T\rangle \leftrightarrow |1^{\downarrow}_c x_T\rangle$

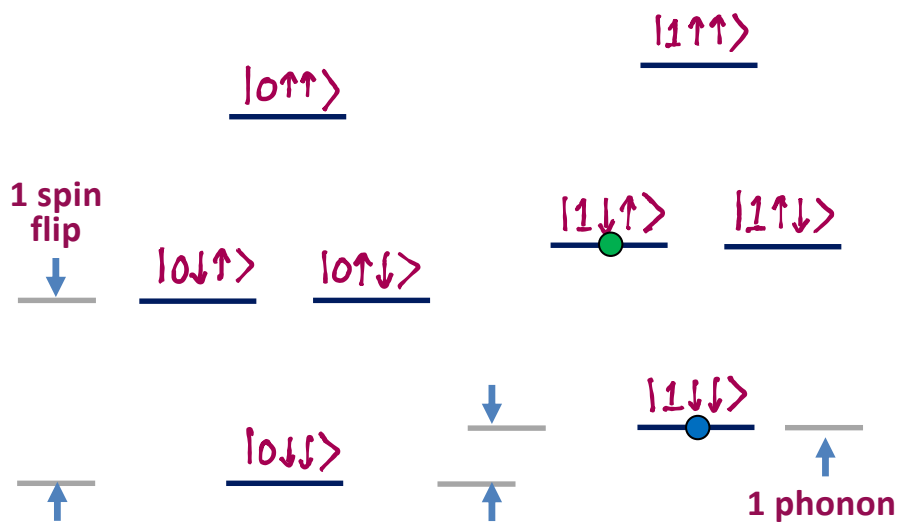


# Introduction and Overview (Preskills Notes)

(1)  $\pi$  pulse on C swaps  $|0\uparrow_c x_T\rangle \leftrightarrow |1\downarrow_c x_T\rangle$

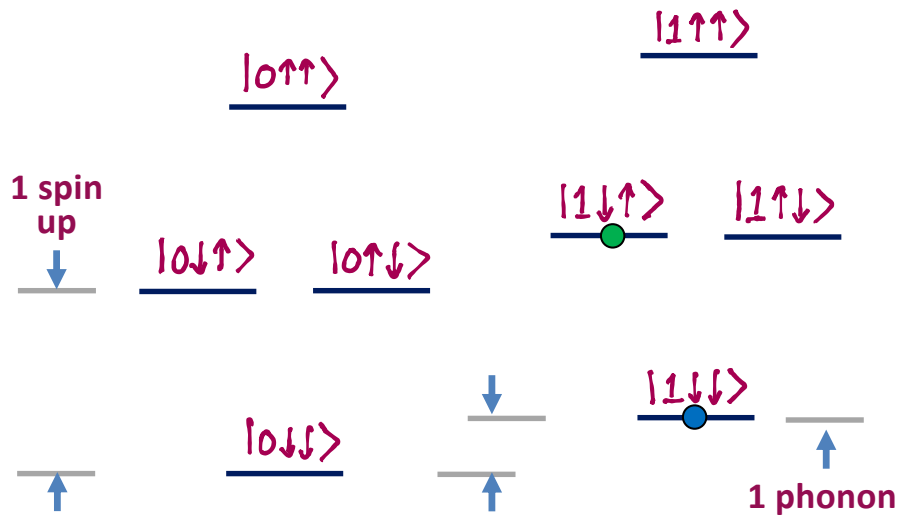


(2)  $\pi$  pulse on T swaps  $|1\downarrow_c \downarrow_T\rangle \leftrightarrow |1\downarrow_c \uparrow_T\rangle$

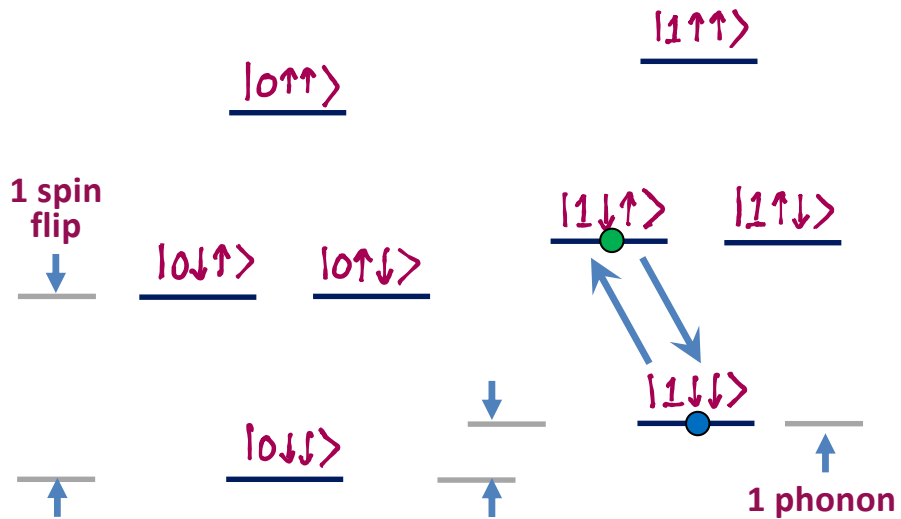


# Introduction and Overview (Preskills Notes)

(1)  $\pi$  pulse on C swaps  $|0\uparrow_c x_T\rangle \leftrightarrow |1\downarrow_c x_T\rangle$

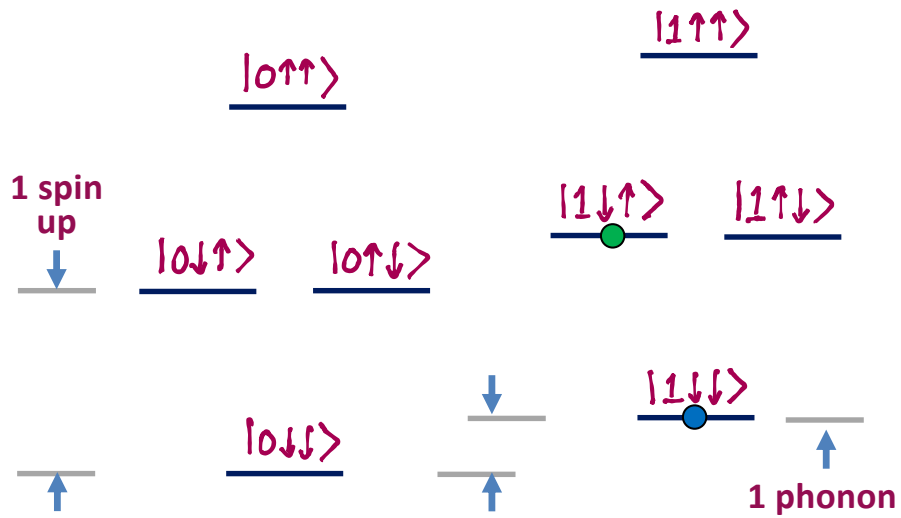


(2)  $\pi$  pulse on T swaps  $|1\downarrow_c \downarrow_T\rangle \leftrightarrow |1\downarrow_c \uparrow_T\rangle$

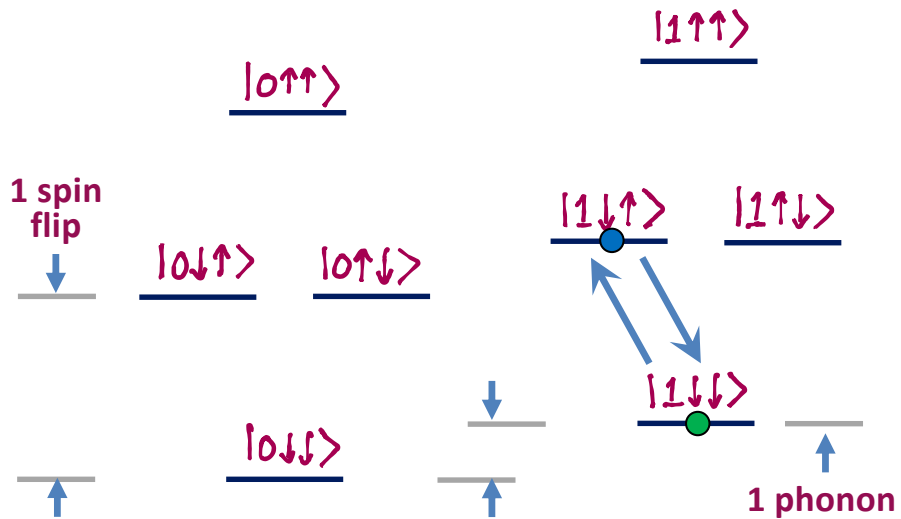


# Introduction and Overview (Preskills Notes)

(1)  $\pi$  pulse on C swaps  $|0\uparrow_c x_T\rangle \leftrightarrow |1\downarrow_c x_T\rangle$

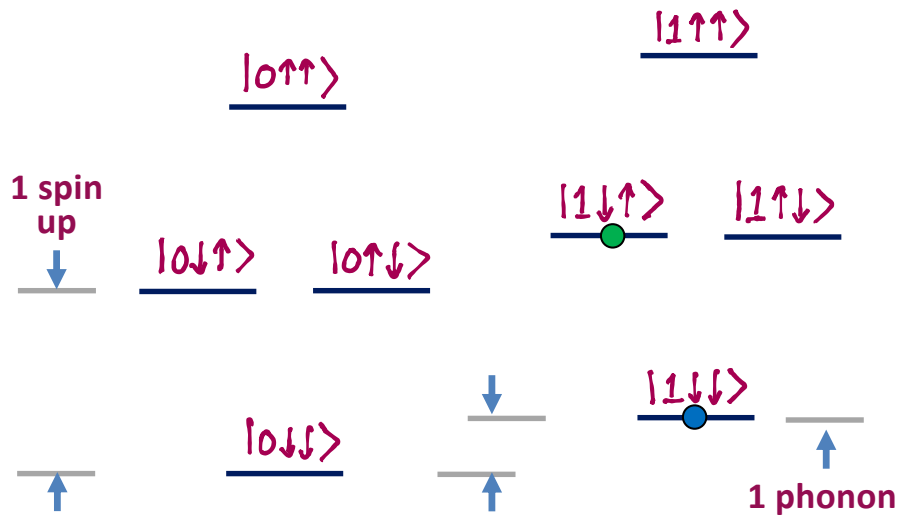


(2)  $\pi$  pulse on T swaps  $|1\downarrow_c \downarrow_T\rangle \leftrightarrow |1\downarrow_c \uparrow_T\rangle$

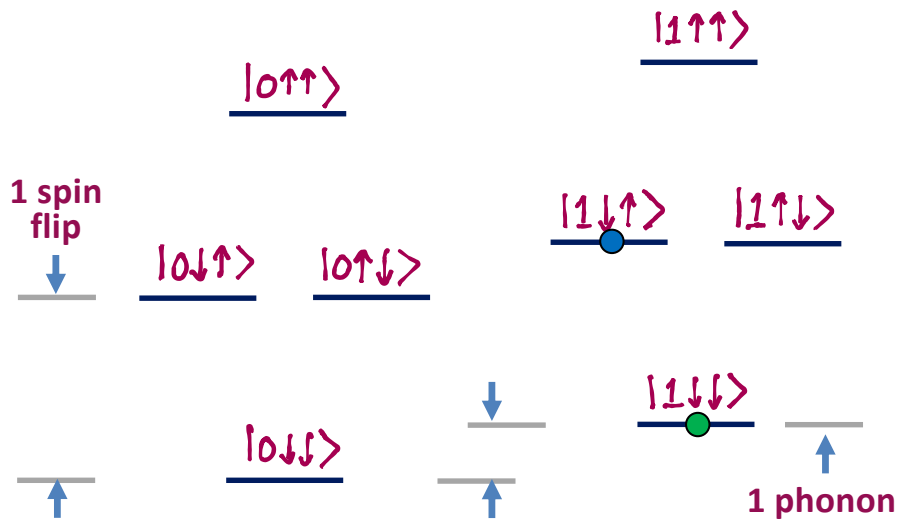


# Introduction and Overview (Preskills Notes)

(1)  $\pi$  pulse on C swaps  $|0\uparrow_c x_T\rangle \leftrightarrow |1\downarrow_c x_T\rangle$



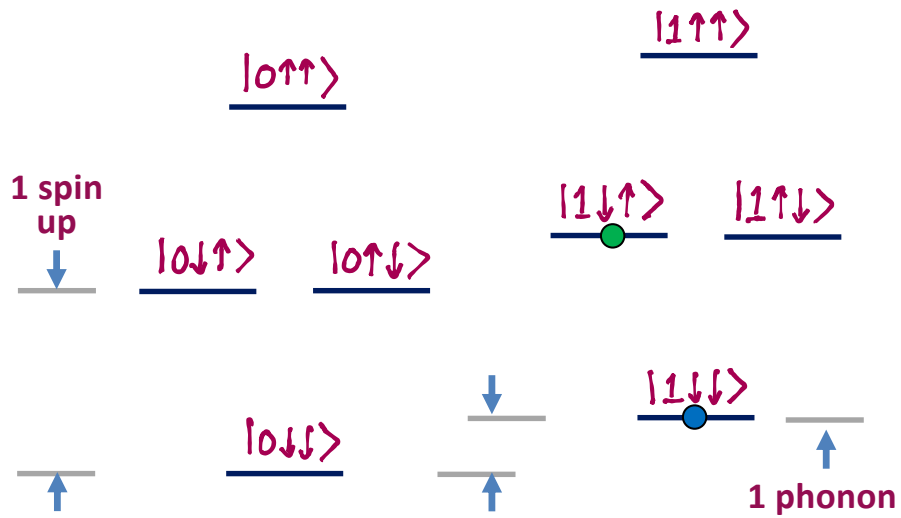
(2)  $\pi$  pulse on T swaps  $|1\downarrow_c \downarrow_T\rangle \leftrightarrow |1\downarrow_c \uparrow_T\rangle$





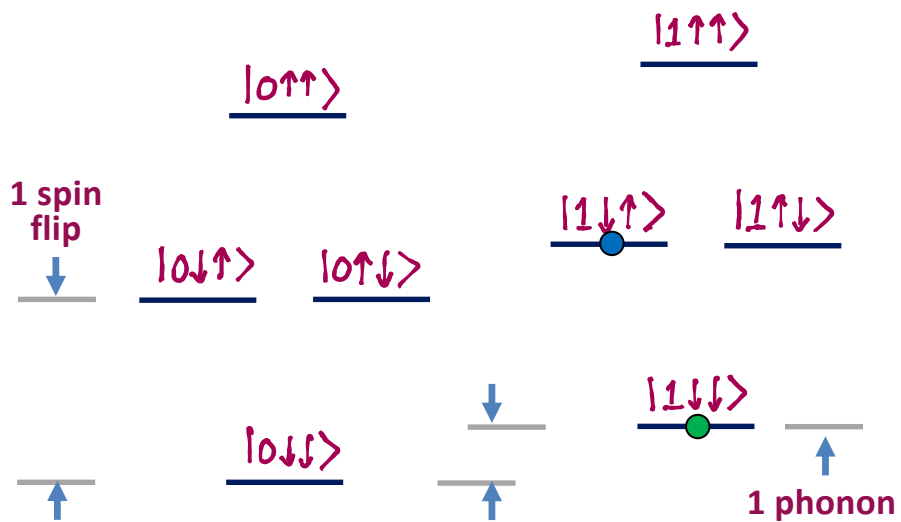
# Introduction and Overview (Preskills Notes)

(1)  $\pi$  pulse on C swaps  $|0\uparrow_c x_T\rangle \leftrightarrow |1\downarrow_c x_T\rangle$

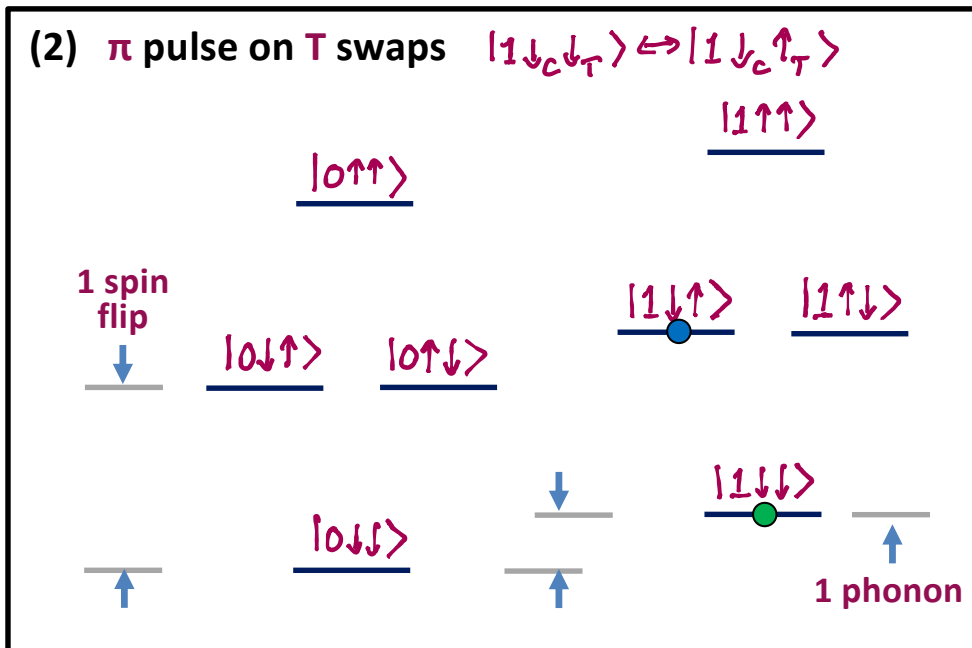
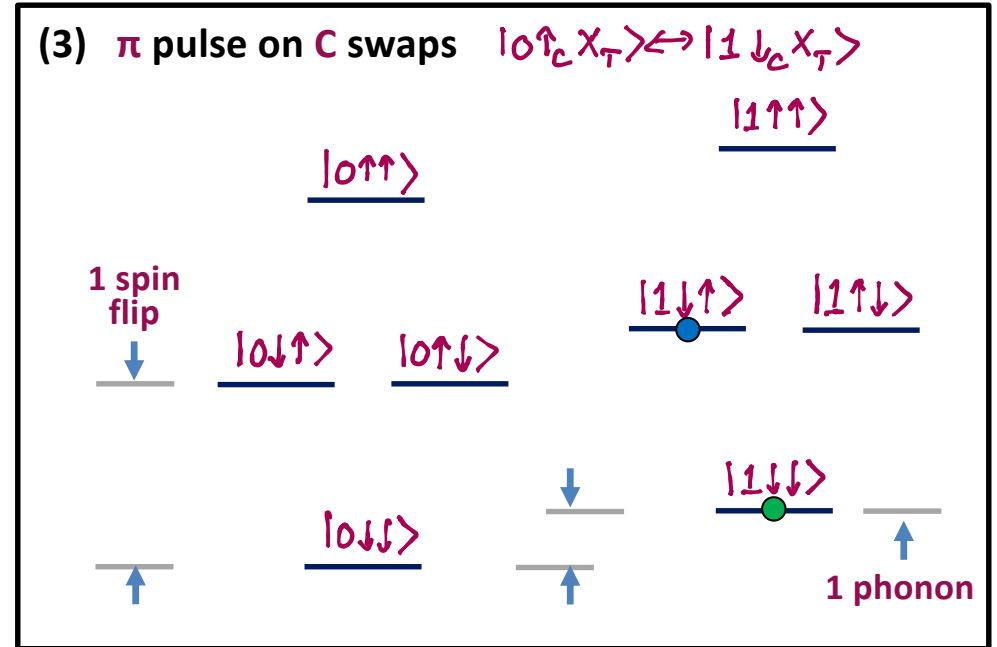
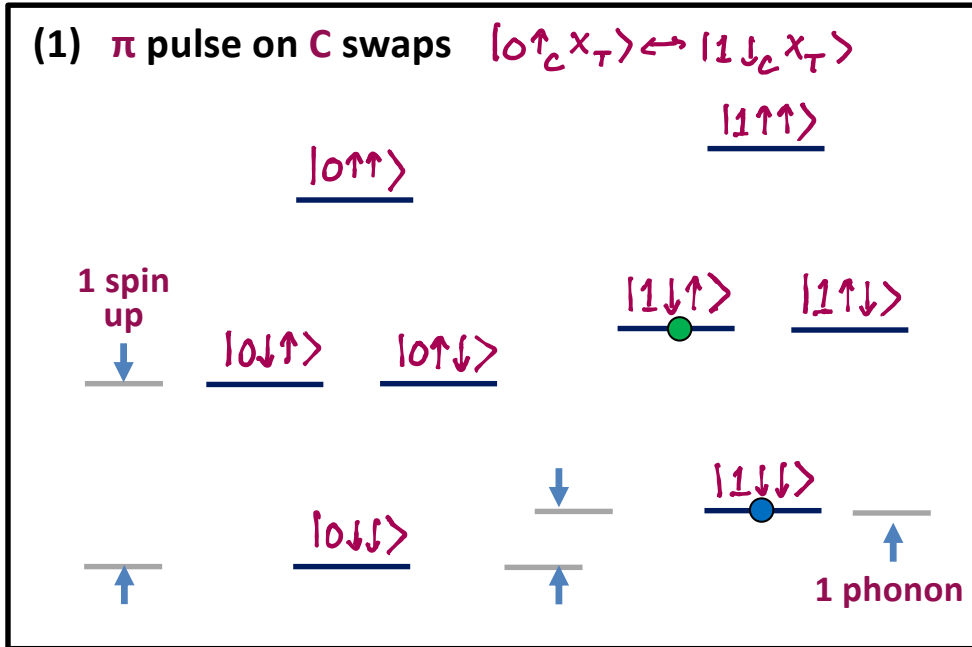


(3)  $\pi$  pulse on C swaps  $|0\uparrow_c x_T\rangle \leftrightarrow |1\downarrow_c x_T\rangle$

(2)  $\pi$  pulse on T swaps  $|1\downarrow_c \downarrow_T\rangle \leftrightarrow |1\downarrow_c \uparrow_T\rangle$

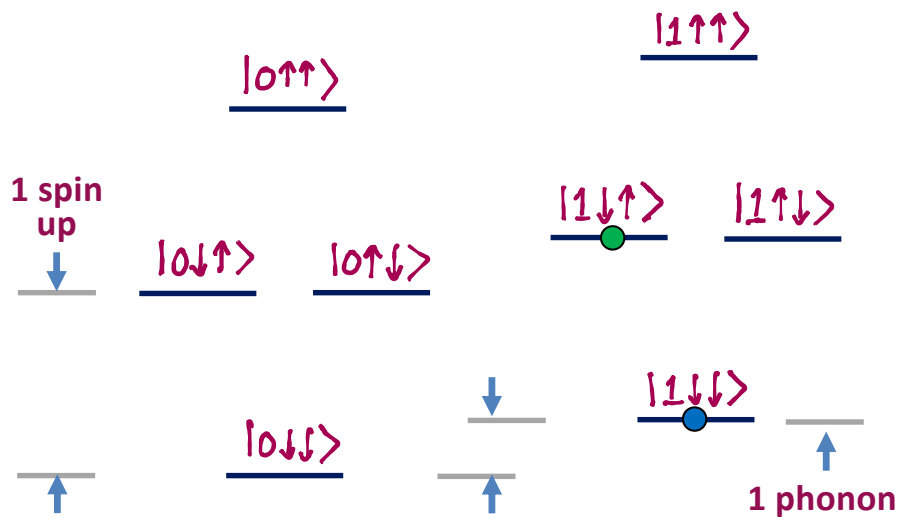


# Introduction and Overview (Preskills Notes)

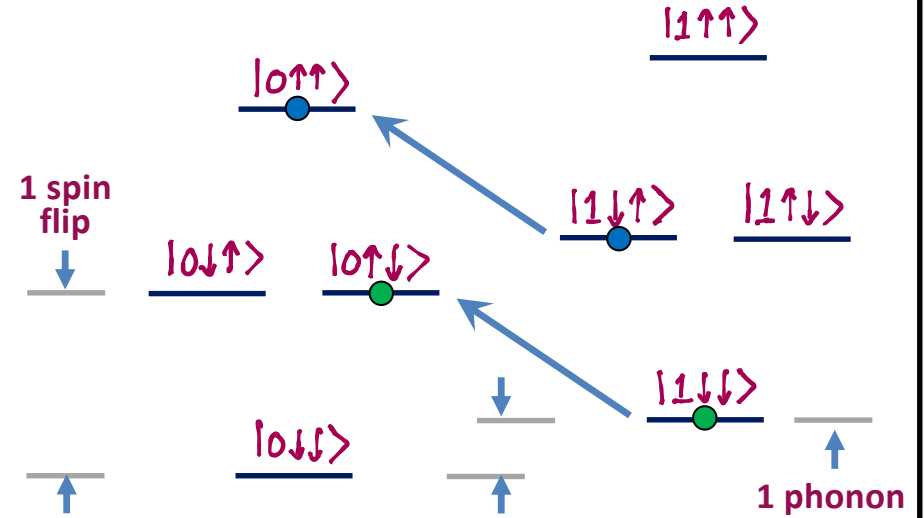


# Introduction and Overview (Preskills Notes)

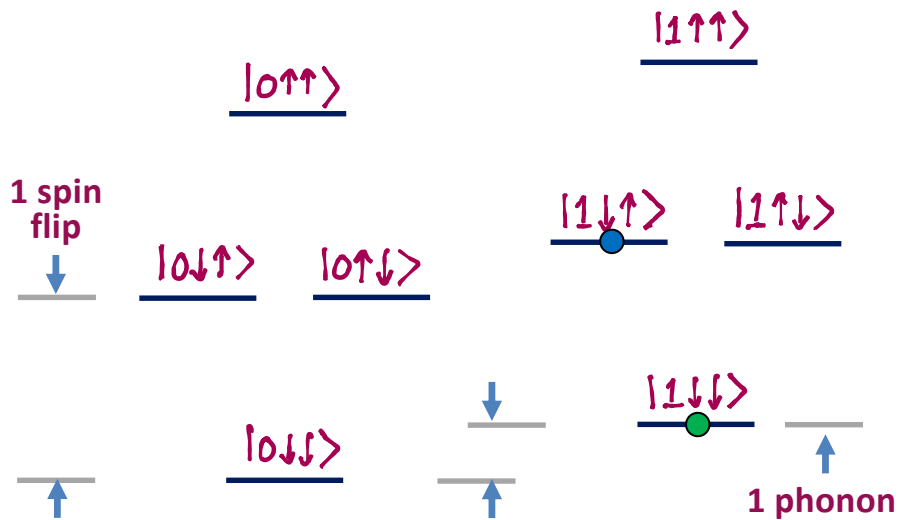
(1)  $\pi$  pulse on C swaps  $|0\uparrow_c x_T\rangle \leftrightarrow |1\downarrow_c x_T\rangle$



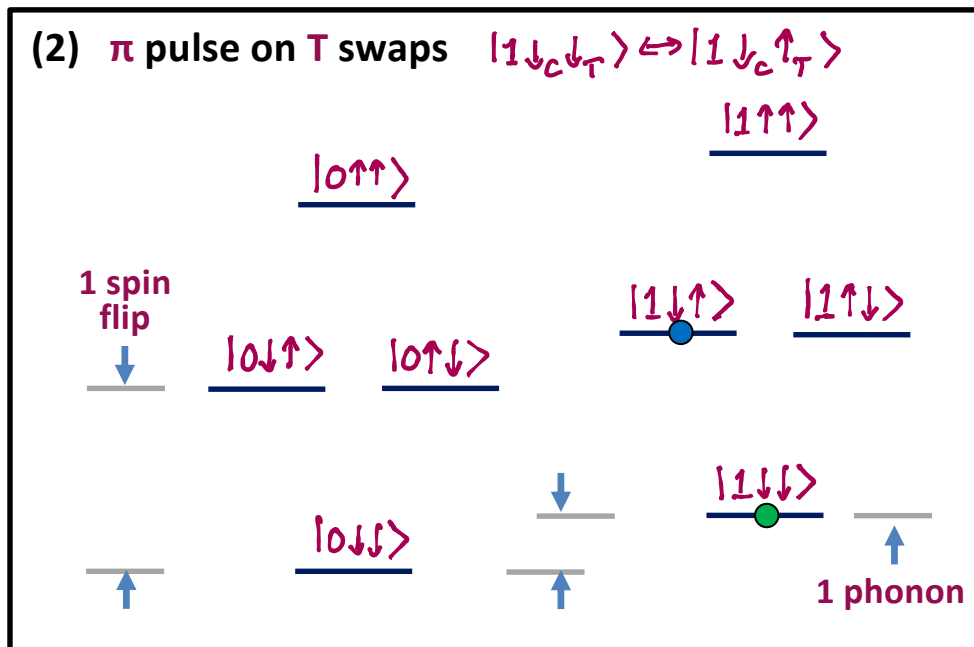
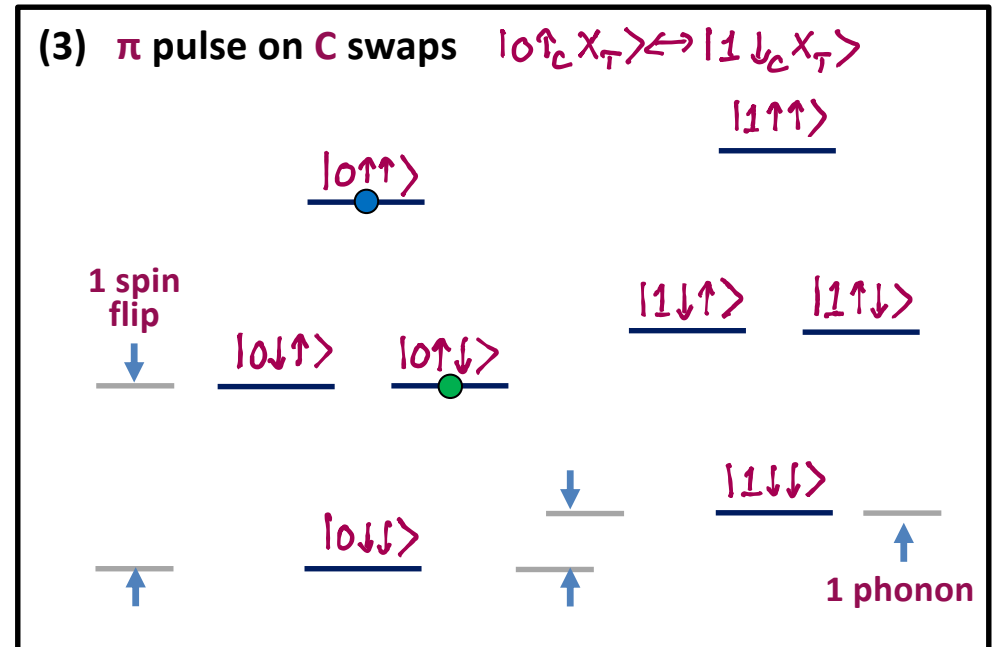
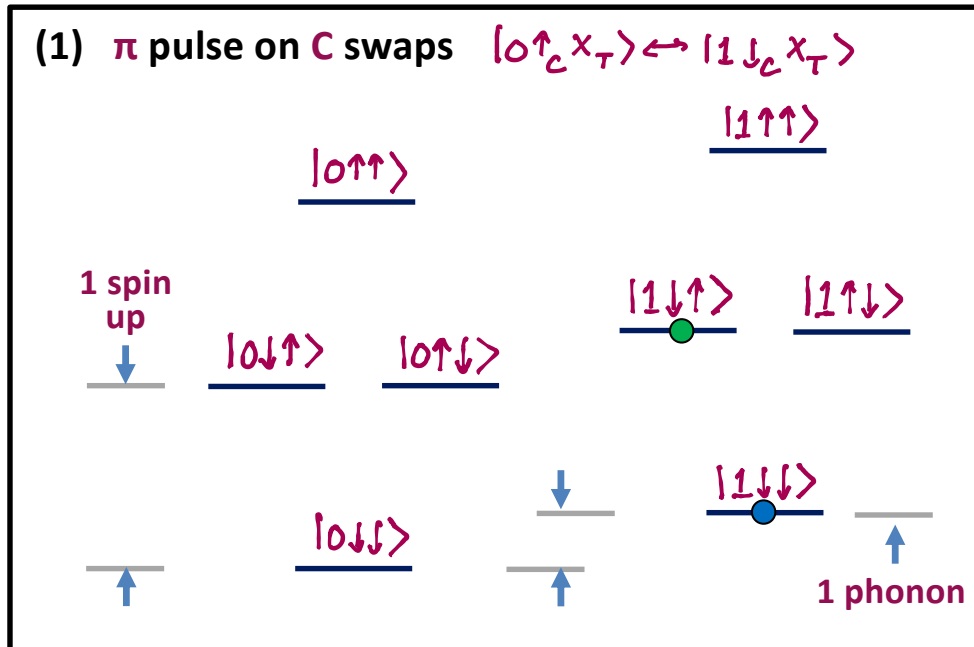
(3)  $\pi$  pulse on C swaps  $|0\uparrow_c x_T\rangle \leftrightarrow |1\downarrow_c x_T\rangle$



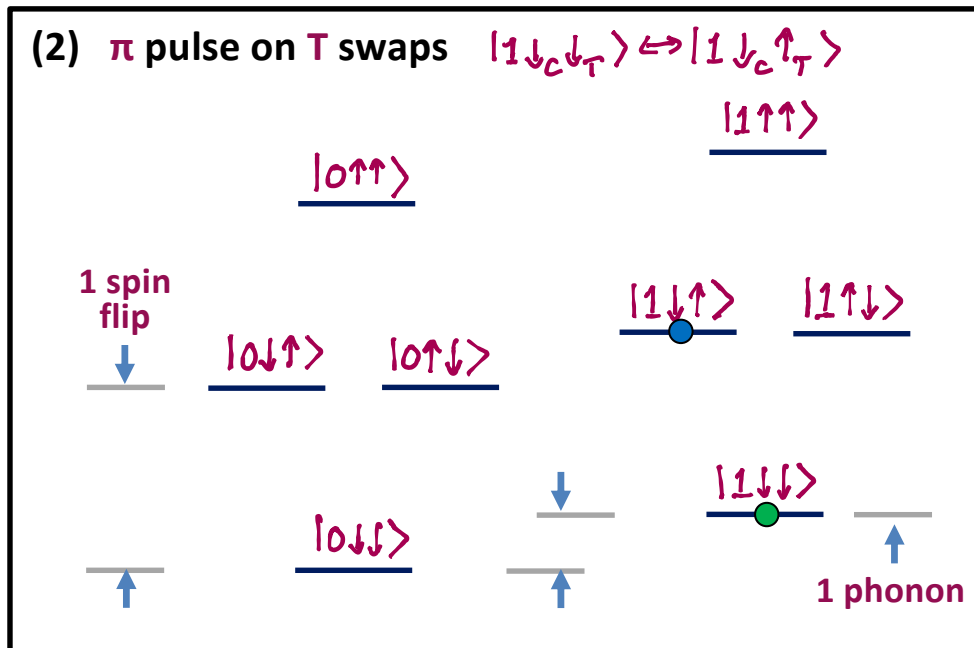
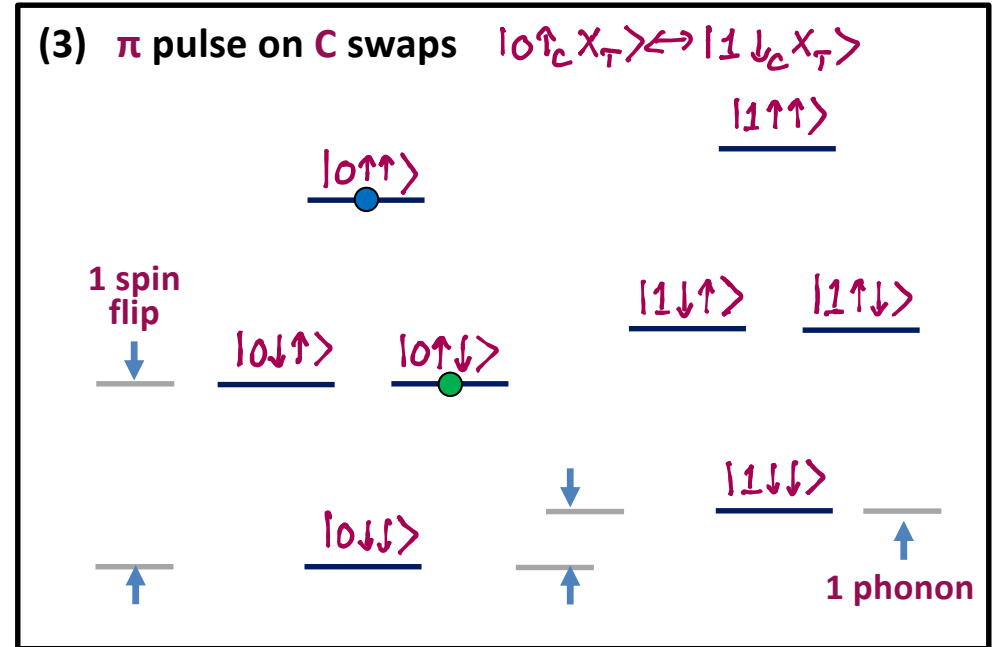
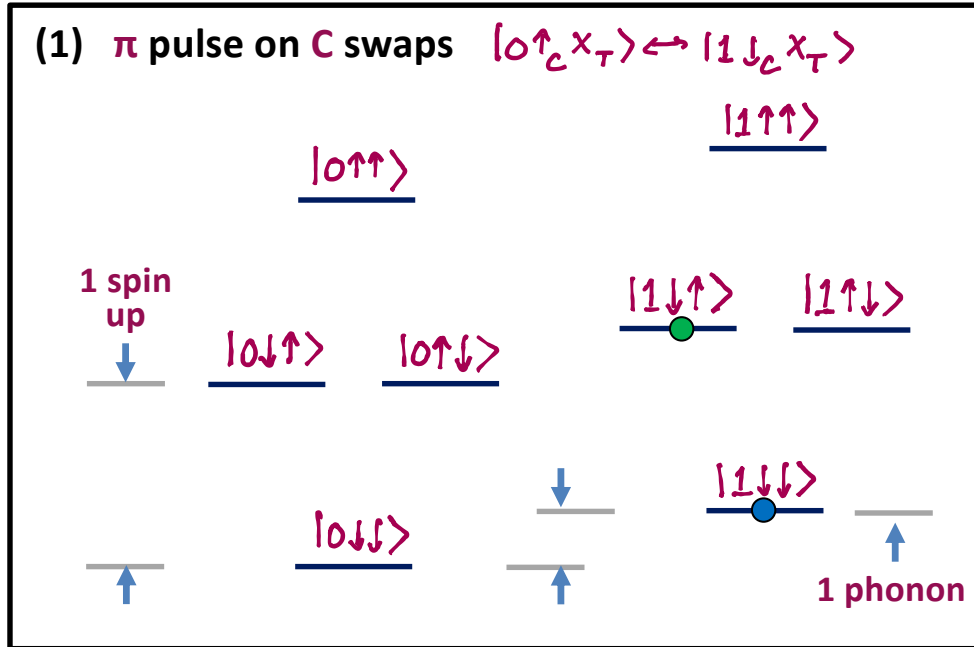
(2)  $\pi$  pulse on T swaps  $|1\downarrow_c \downarrow_T\rangle \leftrightarrow |1\downarrow_c \uparrow_T\rangle$



# Introduction and Overview (Preskills Notes)

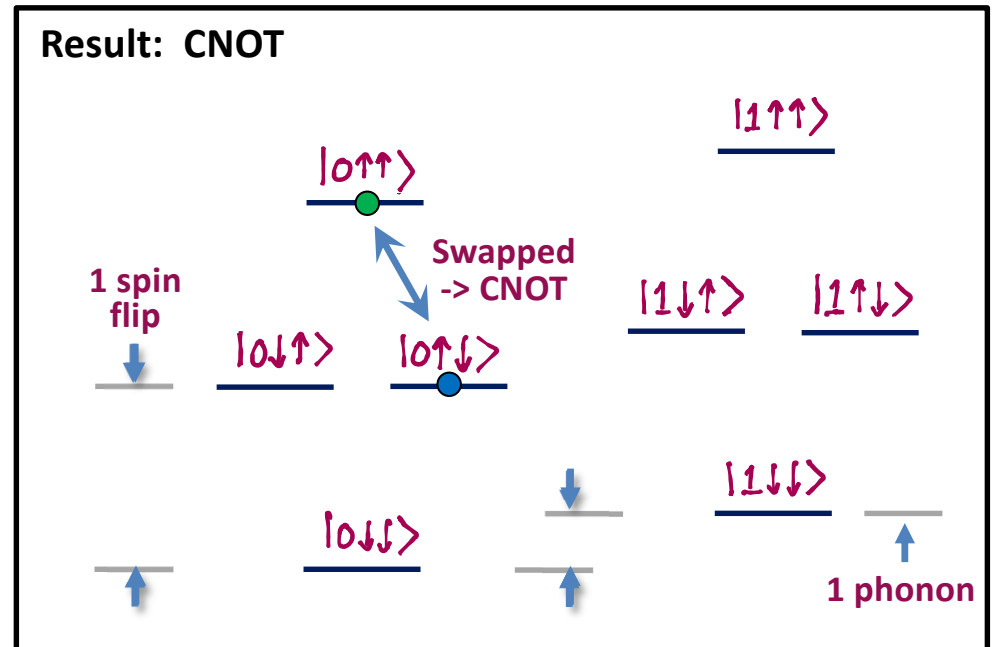
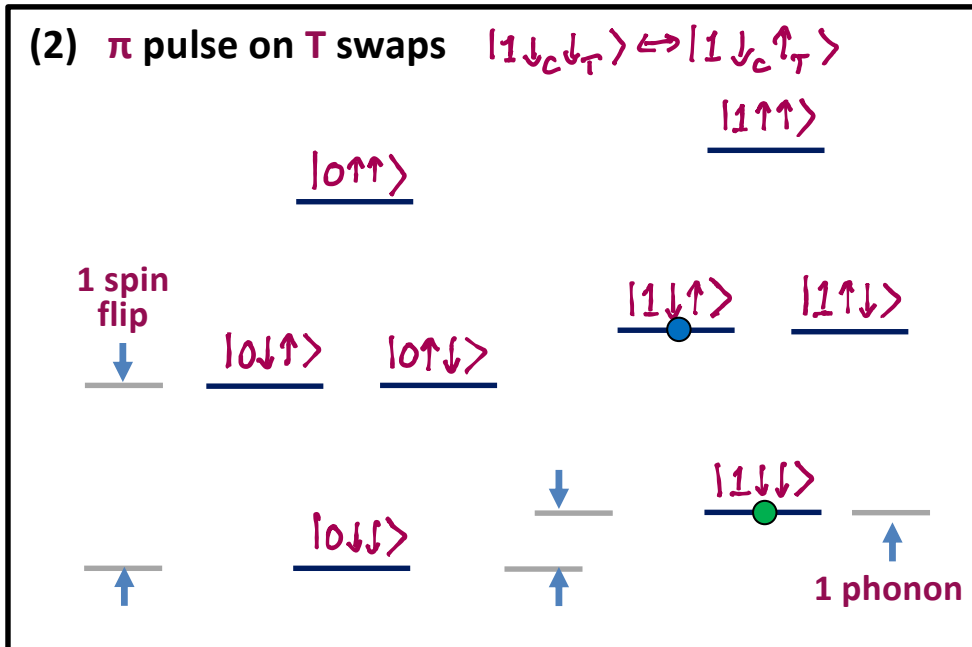
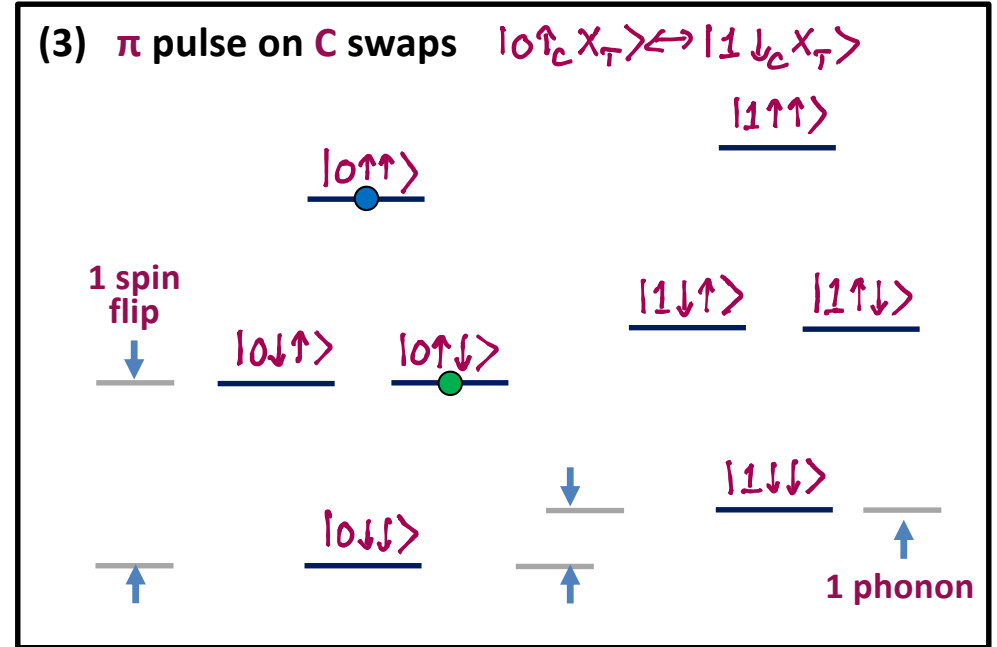
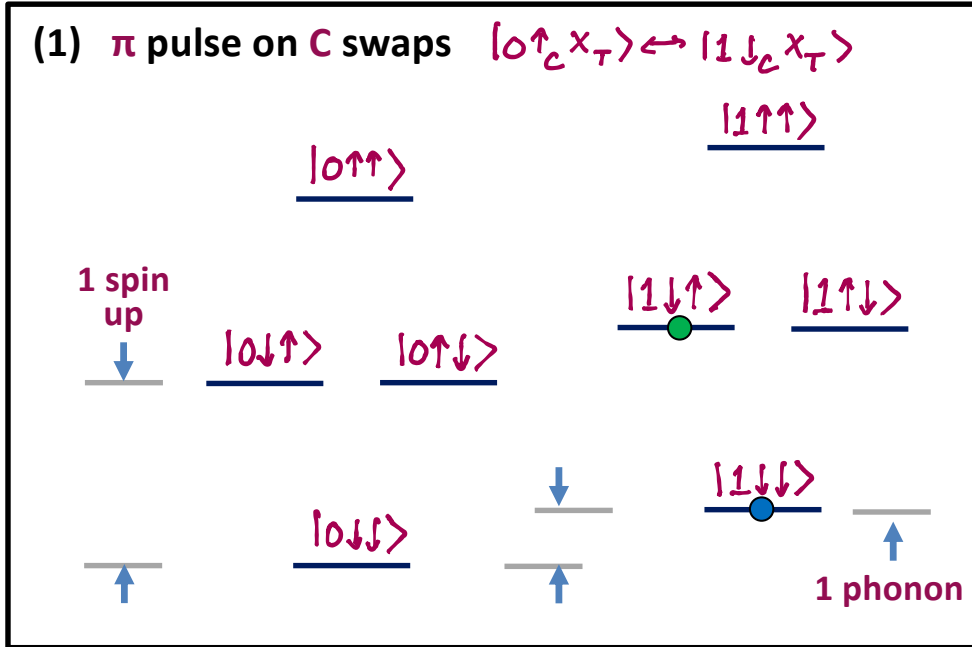


# Introduction and Overview (Preskills Notes)

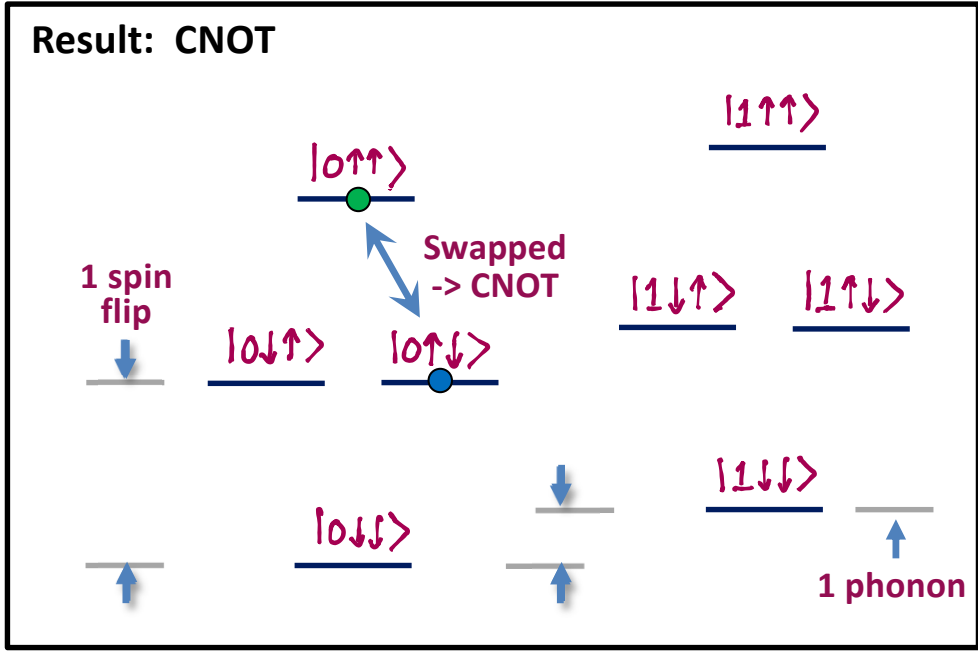


Result: CNOT

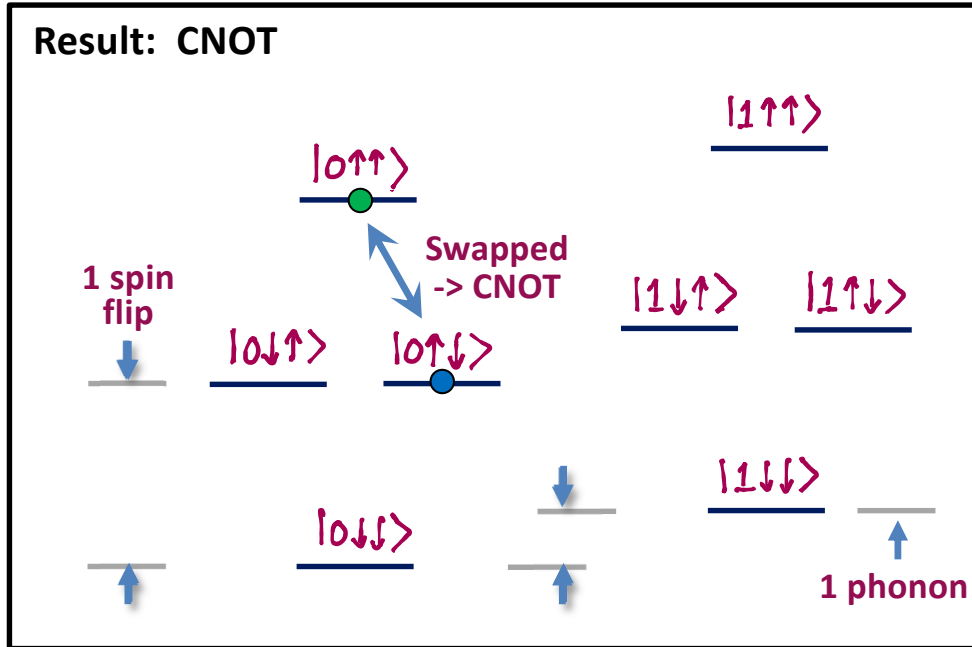
# Introduction and Overview (Preskills Notes)



# Introduction and Overview (Preskills Notes)



# Introduction and Overview (Preskills Notes)



**Note:** The sequence (1)  $\rightarrow$  (2)  $\rightarrow$  (3) leaves the spin and vibrational degrees of freedom unentangled after the CNOT

**Note:** Today's Ion Trap QC experiments rely on much more sophisticated, accurate and robust gate protocols



# Introduction and Overview (Preskills Notes)

**Status:** Many important milestones achieved

- \* Entanglement of  $\geq 20$  ions (2018)
- \* Highest gate & readout fidelities, longest coherence times
- \* Error Correction, Fault Tolerance proof of principle demonstrations
- \* Complex algorithms on few ions, quantum simulations with  $\geq 50$
- \* Research groups in academia, National Labs, Industry

## Some leading groups

NIST	Innsbruck	Quantinuum
Sandia NL	Duke U	IonQ
Many, many others		

## Some links to get started

**Amazon Braket** (IonQ, other Technologies)  
<https://aws.amazon.com/braket/>

**Quantinuum** (Ion Trap Quantum Computing)  
<https://www.quantinuum.com>

**IonQ** <https://ionq.com>

**NIST** <https://www.nist.gov/pml/time-and-frequency-division/ion-storage>

**Innsbrück**  
<https://www.uibk.ac.at/th-physik/qic-group/>