

# OPTI 646

## Introduction to Quantum Information and Computation

The course covers the foundations of quantum information and selected topics in quantum communication and quantum computation, including physical implementations.

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**Text:** “Quantum Information and Computation”, lecture notes by John Preskill, Caltech 1998. Can be downloaded at

<http://theory.caltech.edu/~preskill/ph219/index.html#lecture>

**Course Website:** <https://wp.optics.arizona.edu/opti646/>

**Lectures:** Meinel 432, Tuesdays and Thursdays 12noon-1:30pm.

**Zoom Link:** <https://arizona.zoom.us/j/89787418732> / PW QuISE646

**Office Hours:** Tuesdays and Thursdays 2-3:30pm.  
If you give me a heads-up beforehand, I can often find time for a chat outside regular office hours.

**NOTE:** OPTI 646 is taught in a live in-person format. I plan to zoom-record lectures and post video on the course website, but these recordings are not meant to substitute for in-person attendance.

**Grading:** Homework (30%), student presentation or paper (40%), and class participation (30%). Each student is required to give a lecture presentation or submit a paper on a topic related to Quantum Information Science

**Prerequisites:**

A solid knowledge and understanding of graduate level quantum mechanics is essential, as developed for example in OPTI/PHYS 570A “Quantum Mechanics” or equivalent.

# Topics

## **Introduction and overview**

Physics of information, Quantum computation  
Quantum parallelism, Deutsch's problem  
Quantum error correction  
Physical implementation: Ion trap, Cavity QED, NMR

## **Review of quantum mechanics I - basics**

State vectors, Linear operators, Observables  
Postulates of quantum mechanics

## **Review of quantum mechanics II – bipartite systems**

Tensor product of state spaces  
Measurements on one part of a system  
Density operator, Separate description of part of a system, Partial trace

## **Qubits, spin-1/2 & other 2-level systems**

Spin observables, Pauli matrices  
Pure states, density operator, Bloch picture  
Rotations, Schrödinger evolution, single-qubit gates.

## **Entanglement**

2-spin state space  
Alice & Bob joint experiments, Local measurements and correlations  
Sending non-orthogonal states, Significance of ensemble decomposition  
Local hidden variable theories, Bell inequalities

## **Quantum Communication**

Information in entangled pairs, Dense coding  
Quantum key distribution, Security against eavesdroppers, No cloning theorem  
Quantum teleportation

## **General Theory of Measurement**

Von Neumanns theory of orthogonal measurement, System-meter model  
Non-orthogonal measurements – POVM's  
Implementation as orthogonal measurement in extended state space

## **Superoperators and Decoherence**

Operator-sum representation, Kraus operators, Super-operators  
Decohering quantum channels – depolarizing, phase & amplitude damping

## **Quantum Information Theory**

Shannon entropy, classical data compression  
Shannons noiseless coding theorem, Noisy channel coding theorem  
Von Neumann entropy  
Quantum data compression, Schumacher compression,  
Schumachers noiseless coding theorem  
Mixed-state coding

## **Quantum Computation**

Classical circuits, universal gate sets  
Classical circuit complexity, complexity classes (P, NP, NPC, NPI)  
Quantum circuits, Quantum complexity (BQP)  
Universal quantum gates, Deutsch's gate, other universal sets  
Quantum database search, Grovers algorithm

## **Student Lecture Topics 2002 (7)**

EPR and GHZ, loopholes  
Quantum teleportation  
Quantum communication and quantum cryptography  
Neutral atom quantum computation – optical lattices  
Slow light and quantum data storage  
Quantum games  
Quantum measurement – QND and POVM

## **Student Lecture Topics 2005 (6)**

Quantum Computing with Ion Traps  
Quantum Data Storage in Ensembles  
Quantum Algorithms  
Quantum Key Distribution  
Solid State Implementations of Quantum Computation  
Classical Wave Simulations of QM

## **Student Lecture Topics 2008 (14)**

EPR experiments  
Quantum Non-Demolition Measurements  
Quantum State Reconstruction  
Public Key Cryptography and the RSA cryptosystem  
Slow light and quantum data storage  
Quantum teleportation  
Ion trap quantum computation  
Linear optics quantum computation  
Solid state implementations of quantum computation  
Robust quantum control of qubits  
Quantum simulation of model Hamiltonians  
Shors algorithm for factoring  
Topological quantum computing

**Student Lecture Topics 2010 (9)**

EPR experiments  
Quantum Non-Demolition measurements  
Quantum State Reconstruction  
Quantum Metrology  
Public Key Cryptography and the RSA cryptosystem  
Slow Light and Quantum Data Storage  
Ion Trap Quantum Computation  
Grover's Algorithm for Data Base Search  
Quantum Trajectories and Quantum Monte Carlo Simulation

**Student Lecture Topics 2012 (7)**

Quantum Non-Demolition measurements  
Spin Squeezing  
Weak Values in Quantum Measurement  
Quantum Cryptography  
Grover's Algorithm  
Adiabatic Quantum Computing  
Quantum Simulation in Chemistry

**Student Lecture Topics 2015 (4)**

Quantum non-demolition measurements  
Superoperators and decoherence  
Dynamical decoupling and composite pulses  
Measurement based one-way quantum computation

**Student Lecture Topics 2018 (5)**

Quantum Repeaters  
Surface Code Quantum Computing  
Grover's Algorithm  
Quantum Tomography  
Squeezed States

**Student Lecture Topics 2020 (13)**

Frequency Combs and Quantum Computation  
Overview of Quantum Gates for Ion Trap Quantum Computers  
Quantum Non-Demolition Measurements in Quantum Optomechanics  
GHZ States and Tests of LHV Theories  
Quantum Neural Networks  
Continuous Measurement and Quantum Control  
Analog vs Digital Simulation and the Effects of Trotterization  
Variational Quantum Eigensolver (VQE)  
Quantum Metrology: Quantum Fisher Information and Estimation Strategies  
Quantum Memory: A Review  
Shor's Algorithm  
A Review of Quantum Error Correction of a Qubit Encoded in Grid States  
Quantum Error Correction Codes