OPTI 646
Introduction to Quantum Information and Computation

The course covers the foundations of quantum information and selected topics in quantum communication and quantum computation, including physical implementations.

Professor: Poul Jessen, Meinel 604. Email: jessen@optics.arizona.edu

Text: "Quantum Information and Computation", lecture notes by John Preskill, Caltech 1998. Can be downloaded at

http://theory.caltech.edu/~preskill/ph219/index.html#lecture

Course Website: https://wp.optics.arizona.edu/opti646/

Grading: Homework (30%), student presentation (40%) and class participation (30%). Each student is required to give a lecture presentation on a topic related to Quantum Information Science

Prerequisites:
A solid knowledge and understanding of graduate level quantum mechanics is essential, as developed for example in OPTI/PHYS 570A "Quantum Mechanics" or equivalent.

Topics

Introduction and overview
Physics of information, Quantum computation
Quantum parallelism, Deutsch's problem
Quantum error correction
Physical implementation: Ion trap, Cavity QED, NMR

Review of quantum mechanics I - basics
State vectors, Linear operators, Observables
Postulates of quantum mechanics

Review of quantum mechanics II – bipartite systems
Tensor product of state spaces
Measurements on one part of a system
Density operator, Separate description of part of a system, Partial trace

Qubits, spin-1/2 & other 2-level systems
Spin observables, Pauli matrices
Pure states, density operator, Bloch picture
Rotations, Schrödinger evolution, single-qubit gates.

Entanglement
2-spin state space
Alice & Bob joint experiments, Local measurements and correlations
Sending non-orthogonal states, Significance of ensemble decomposition
Local hidden variable theories, Bell inequalities

Quantum Communication
Information in entangled pairs, Dense coding
Quantum key distribution, Security against eavesdroppers, No cloning theorem
Quantum teleportation

General Theory of Measurement
Von Neumanns theory of orthogonal measurement, System-meter model
Non-orthogonal measurements – POVM's
Implementation as orthogonal measurement in extended state space

Superoperators and Decoherence
Operator-sum representation, Kraus operators, Super-operators
Decohering quantum channels – depolarizing, phase & amplitude damping

Quantum Information Theory

Shannon entropy, classical data compression
Shannons noiseless coding theorem, Noisy channel coding theorem
Von Neumann entropy
Quantum data compression, Schumacher compression,
Schumachers noiseless coding theorem
Mixed-state coding

Quantum Computation

Classical circuits, universal gate sets
Classical circuit complexity, complexity classes (P, NP, NPC, NPI)
Quantum circuits, Quantum complexity (BQP)
Universal quantum gates, Deutsch’s gate, other universal sets
Quantum database search, Grovers algorithm

Student Lecture Topics 2002

EPR and GHZ, loopholes
Quantum teleportation
Quantum communication and quantum cryptography
Neutral atom quantum computation – optical lattices
Slow light and quantum data storage
Quantum games
Quantum measurement – QND and POVM

Student Lecture Topics 2005

Quantum Computing with Ion Traps
Quantum Data Storage in Ensembles
Quantum Algorithms
Quantum Key Distribution
Solid State Implementations of Quantum Computation
Classical Wave Simulations of QM

Student Lecture Topics 2008

EPR experiments
Quantum Non-Demolition Measurements
Quantum State Reconstruction
Public Key Cryptography and the RSA cryptosystem
Slow light and quantum data storage
Quantum teleportation
Ion trap quantum computation
Linear optics quantum computation
Solid state implementations of quantum computation
Robust quantum control of qubits
Quantum simulation of model Hamiltonians
Shors algorithm for factoring
Topological quantum computing
Quantum Information Theory - Holevo Information, Accessibe Information

Student Lecture Topics 2010

EPR experiments
Quantum Non-Demolition measurements
Quantum State Reconstruction
Quantum Metrology
Public Key Cryptography and the RSA cryptosystem
Slow Light and Quantum Data Storage
Ion Trap Quantum Computation
Grovers Agorithm for Data Base Search
Quantum Trajectories and Quantum Monte Carlo Simulation

Student Lecture Topics 2012

Quantum Non-Demolition measurements
Spin Squeezing
Weak Values in Quantum Measurement
Quantum Cryptography
Grovers Algorithm
Adiabatic Quantum Computing
Quantum Simulation in Chemistry

Student Lecture Topics 2015

Quantum non-demolition measurements
Superoperators and decoherence
Dynamical decoupling and composite pulses
Measurement based one-way quantum computation

Student Lecture Topics 2018

Quantum Repeaters
Surface Code Quantum Computing
Grovers Algorithm
Quantum Tomography
Squeezed States