Problem 1) The chain rule of differentiation is written as follows:

$$\frac{d}{dx}f[g(x)] = g'(x)f'[g(x)]. \tag{1}$$

Therefore, considering that $(e^x)' = e^x$, we will have

$$\frac{d}{dx}\left(e^{e^x}\right) = (e^x)\left(e^{e^x}\right).$$
(2)

$$\frac{d}{dx}\left(e^{e^{e^{x}}}\right) = (e^{x})\left(e^{e^{x}}\right)\left(e^{e^{e^{x}}}\right).$$
(3)