
Problem 12-2) Let $\mathbf{A} = |\mathbf{A}| \cos \theta_A \hat{\mathbf{x}} + |\mathbf{A}| \sin \theta_A \hat{\mathbf{y}}$ and $\mathbf{B} = |\mathbf{B}| \cos \theta_B \hat{\mathbf{x}} + |\mathbf{B}| \sin \theta_B \hat{\mathbf{y}}$. We will have

$$\begin{aligned} \mathbf{A} \times \mathbf{B} &= (A_x B_y - A_y B_x) \hat{\mathbf{z}} = |\mathbf{A}| |\mathbf{B}| (\cos \theta_A \sin \theta_B - \sin \theta_A \cos \theta_B) \hat{\mathbf{z}} \\ &= |\mathbf{A}| |\mathbf{B}| \sin(\theta_B - \theta_A) \hat{\mathbf{z}}. \end{aligned}$$

Note that $|\mathbf{A}| |\mathbf{B}| \sin(\theta_B - \theta_A)$ is the area of the parallelogram, and $\hat{\mathbf{z}}$ is perpendicular to the xy -plane, which is the plane defined by \mathbf{A} and \mathbf{B} .
