Problem 1) The chain rule of differentiation is written as follows:

$$\frac{d}{dx}f[g(x)] = g'(x)f'[g(x)]. \tag{1}$$

Therefore, considering that $(e^x)' = e^x$, we will have

$$\frac{d}{dx}(e^{e^x}) = (e^x)(e^{e^x}). \tag{2}$$

$$\frac{d}{dx}\left(e^{e^{e^x}}\right) = (e^x)\left(e^{e^x}\right)\left(e^{e^{e^x}}\right). \tag{3}$$