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**Problem 3)** Since  $AC'$  is one-half the length of  $AB$  and  $AB'$  is one-half the length of  $AC$ , the triangles  $ABC$  and  $AC'B'$ , which also share a common angle at  $A$ , are similar. This means that  $C'B'$  is parallel to  $BC$ , and also that the length of  $C'B'$  is one-half that of  $BC$ . The triangles  $QBC$  and  $QB'C'$  are thus similar (their angles are the same). Since  $BC$  is twice as long as  $B'C'$ , we conclude that  $QB$  is also twice the length of  $QB'$ , and, similarly,  $QC$  is twice as long as  $QC'$ .

The above argument can be applied to any pair of medians, say  $AA'$  and  $BB'$ . Since the crossing point must once again split  $BB'$  in a 2:1 ratio, it cannot be any point other than  $Q$ . The three medians, therefore, cross at a single point.

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