Opti 501 Prelim Questions, Fall 2008

1. A semi-infinite slab of transparent glass (refractive index = n) is coated with a *perfect* antireflection coating on its entrance facet. A monochromatic, linearly-polarized plane-wave arrives at the slab at normal incidence, as shown below. The incidence medium is free space, the vacuum wavelength of the light is λ_0 , and the incident *E*-field is along the *x*-axis.

- 2 pts a) What is the relation between the incident *E* and *H*-fields, *E*_i and *H*_i, in terms of the impedance of the free-space, $Z_0 = \sqrt{\mu_0/\varepsilon_0}$?
- 2 pts b) What is the relation between the fields E_t , H_t transmitted into the slab in terms of Z_0 and n?
- 3 pts c) Without making any assumptions about the structure of the anti-reflection coating, simply knowing that the optical energy of the beam passes entirely from the free space into the slab, determine the relation between the incident and transmitted *E*-fields E_i and E_t .



3 pts d) Assume now that, instead of a plane-wave, the incident beam is a pulse of light having the same central wavelength λ_0 as before. Moreover, the front-facet coating is effective as a perfect anti-reflection coating for the entire pulse, and the semi-infinite slab is free from dispersion, so that, inside the slab, the pulse propagates with velocity c/n, as shown below. What are the *E*- and *H*-field energies inside the slab? Is the total *E*-field energy of the pulse equal to its total *H*-field energy? Is the pulse energy conserved before and after incidence?



2. Shown below is a collimated, monochromatic beam with a large, uniform cross-sectional area (essentially a finite-diameter plane-wave), incident on a semi-infinite, transparent medium of refractive index *n*. The angle of incidence is θ , the medium of incidence is free space, the footprint of the beam along the *x*-axis is ζ , and the incident beam is p-polarized (with the *E*- and *H*-field amplitudes being E_0 and H_0 , respectively). Denote the *E*-field amplitude of the reflected beam by ρE_0 , that of the transmitted beam by τE_0 .

- 2 pts a) In terms of ρ , τ , n, E_0 , and the free-space impedance $Z_0 = \sqrt{\mu_0/\varepsilon_0}$, what are the *H*-field amplitudes of the reflected and transmitted beams?
- 3 pts b) Determine the rate of flow of optical energy (per unit area per unit time) for the incident, reflected, and transmitted beams?
- 3 pts c) Use conservation of energy to find a relationship between ρ and τ in terms of *n* and θ .
- 2 pts d) How is the relation between ρ and τ obtained in part (c) affected if the incident beam happens to be s-polarized?

