

Problem 48) a) $E_z(x, z=0^-, t) = E_z^{(\text{incident})} + E_z^{(\text{reflected})} \Rightarrow$

$$E_z(x, z=0^-, t) = (r_p - 1) E_p \sin \theta \exp \{ i k_0 (\Delta z \theta x - ct) \}; \quad k_0 = \omega/c \quad \checkmark$$

↑ reflected
↑ incident
↑ σ_x

b) $D_{\perp}(x, z=0, t) = \epsilon_0 E_z(x, z=0^-, t) = \epsilon_0 \epsilon(\omega) E_z(x, z=0^+, t) \Rightarrow$

$$E_z(x, z=0^+, t) = \frac{r_p - 1}{\epsilon(\omega)} E_p \sin \theta \exp \{ i k_0 (\Delta z \theta x - ct) \} \quad \checkmark$$

c) $\vec{\nabla} \cdot \vec{E} = \rho/\epsilon_0 \Rightarrow E_z(x, z=0^+, t) - E_z(x, z=0^-, t) = \frac{1}{\epsilon_0} \sigma_s(x, z=0, t) \Rightarrow$

$$\sigma_s(x, z=0, t) = \epsilon_0 \left[\frac{1}{\epsilon(\omega)} - 1 \right] (r_p - 1) E_p \sin \theta \exp \{ i k_0 (\Delta z \theta x - ct) \} \quad \checkmark$$