

Problem 25) We have seen that $\tan\theta_B = n_o$ and $\sin\theta_B = n_o \sin\theta'_B$ (Snell's law). Therefore,

$$\tan\theta_B = \sin\theta_B / \cos\theta_B = n_o \quad \rightarrow \quad \sin\theta_B = n_o \cos\theta_B.$$

$$n_o \sin\theta'_B = \sin\theta_B \quad \rightarrow \quad n_o \sin\theta'_B = n_o \cos\theta_B \quad \rightarrow \quad \sin\theta'_B = \cos\theta_B = \sin\left(\frac{\pi}{2} - \theta_B\right)$$

$$\rightarrow \quad \theta'_B = \frac{\pi}{2} - \theta_B \quad \rightarrow \quad \theta_B + \theta'_B = \frac{\pi}{2}.$$

$$\text{b) } \theta'_B = \frac{\pi}{2} - \theta_B \rightarrow \begin{cases} \sin\theta'_B = \cos\theta_B \\ \cos\theta'_B = \sin\theta_B \end{cases} \rightarrow \tan\theta'_B = 1/\tan\theta_B = 1/n_o.$$

We conclude that θ'_B is the Brewster angle of incidence on the second facet of the plate.
