

**Problem 3)** Consider two uniformly-charged slabs having charge-densities  $+\rho_0$  and  $-\rho_0$ , as shown. Let these slabs be superposed, with the center of one slab shifted by  $d$  relative to the center of the other. The direction of shift makes an angle  $\theta$  with the surface-normal. The individual charges are  $q$ , the individual dipoles are  $p = qd$ , and, when multiplied by the number of charges  $N$  per unit volume, the polarization density is  $P = Np = Nqd = \rho_0 d$ . The direction of  $\mathbf{P}$  coincides with the direction of displacement  $\mathbf{d}$ . Now, the surface charge-density (i.e., charge per unit area) is given by the volume charge-density  $\pm\rho_0$  times the thickness of the surface layer  $d \cos \theta$ . Therefore,  $\sigma_s = \rho_0 d \cos \theta = P \cos \theta$ .

