

**Problem 2-23)** The magnetic field  $\mathbf{B}$  produced by the current  $I_1$  at the location of the second wire is  $\mathbf{B}_{12} = \mu_0 I_1 \hat{\boldsymbol{\phi}} / (2\pi d)$ . Here  $\hat{\boldsymbol{\phi}}$  is the azimuthal unit-vector of the cylindrical coordinates.

Next, assume that the density (per unit length) of the mobile charges in the second wire is  $Q$ . If these charges move along the length of the wire with velocity  $\mathbf{V}$ , the amount of charge crossing any cross-section per unit time will be  $QV$ ; therefore,  $I_2 = QV$ . The force per unit length is thus given by the Lorentz force law as follows:

$$\mathbf{F}_{12} = Q\mathbf{V} \times \mathbf{B} = - \left( \frac{\mu_0 I_1 I_2}{2\pi d} \right) \hat{\boldsymbol{\rho}}.$$

Here  $\hat{\boldsymbol{\rho}}$  is the radial unit-vector of the cylindrical coordinates. From symmetry we find that

$$\mathbf{F}_{21} = + \left( \frac{\mu_0 I_1 I_2}{2\pi d} \right) \hat{\boldsymbol{\rho}}.$$

The wires thus attract each other when  $I_1$  and  $I_2$  are in the same direction; they repel each other when  $I_1$  and  $I_2$  are in opposite directions.

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