Problem 1-38) From Problem 34, part (b), we have $\nabla \cdot (A \times B) = B \cdot (\nabla \times A) - A \cdot (\nabla \times B)$. Replacing B, which, in general, is a function of position r, with the constant vector C, makes the second curl on the right-hand side of the above identity to vanish. We will then have $\nabla \cdot (A \times C) = C \cdot (\nabla \times A)$. Applying Gauss's theorem to the left-hand-side of this equation, we find

$$\int_{\text{volume}} \nabla \cdot (\mathbf{A} \times \mathbf{C}) \, dv = \oint_{\text{surface}} [\mathbf{A}(\mathbf{r}) \times \mathbf{C}] \cdot ds = -\oint_{\text{surface}} [\mathbf{A}(\mathbf{r}) \times ds] \cdot \mathbf{C} = -\mathbf{C} \cdot \oint_{\text{surface}} \mathbf{A}(\mathbf{r}) \times ds. \quad (1)$$

On the right-hand-side, the volume integral may be somewhat simplified, as follows:

$$\int_{\text{volume}} C \cdot (\nabla \times A) d\nu = C \cdot \int_{\text{volume}} \nabla \times A(r) d\nu.$$
 (2)

The above expressions are valid for *any* (arbitrary) constant vector C and, moreover, they are equal to each other. We conclude that the coefficients of C on the right-hand-sides of Eqs.(1) and (2) must be the same, that is, $\int_{\text{volume}} \nabla \times A(r) \, dv = -\oint_{\text{surface}} A(r) \times ds$.