Problem 1-37) From Problem 34, part (a), we have $\nabla \cdot (\psi A) = (\nabla \psi) \cdot A + \psi \nabla \cdot A$. Replacing A, which, in general, is a function of position r, with the constant vector C, makes the divergence term on the right-hand side of the above identity to vanish. We will then have $\nabla \cdot (\psi C) = (\nabla \psi) \cdot C$. Applying Gauss's theorem to the left-hand-side of the above equation, we find

$$\int_{\text{volume}} \nabla \cdot (\psi C) dv = \oint_{\text{surface}} \psi(r) C \cdot ds = C \cdot \oint_{\text{surface}} \psi(r) ds.$$
 (1)

On the right-hand-side, the volume integral may be somewhat simplified, as follows:

$$\int_{\text{volume}} (\nabla \psi) \cdot C \, dv = C \cdot \int_{\text{volume}} \nabla \psi(r) \, dv.$$
 (2)

The above expressions are valid for *any* (arbitrary) constant vector C and, moreover, they are equal to each other. We conclude that the coefficients of C on the right-hand-sides of Eqs.(1) and (2) must be the same, that is, $\int_{\text{volume}} \nabla \psi(r) \, dv = \oint_{\text{surface}} \psi(r) \, ds$.