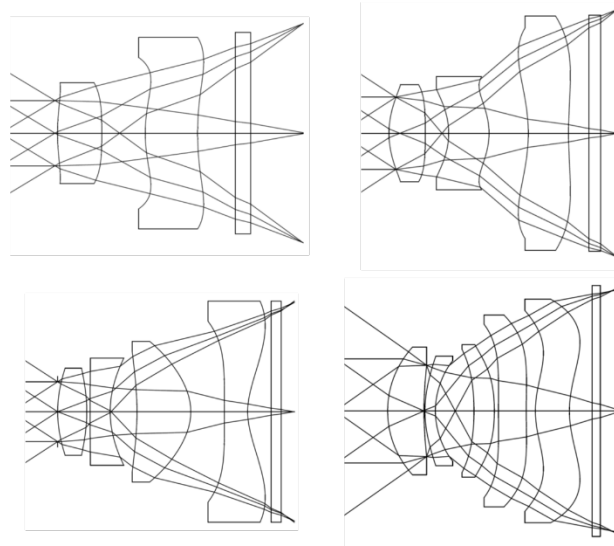


# Mobile phone lenses

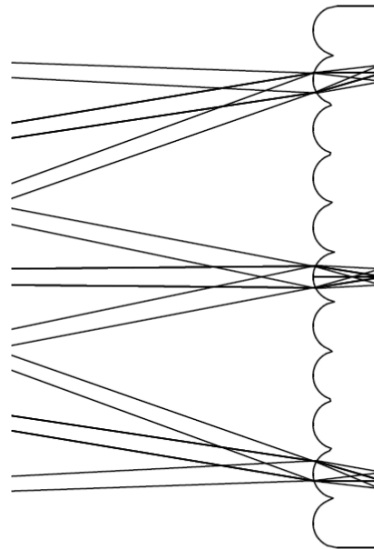


## Lens Design OPTI 696A

# Specifications

Typical mobile phone lens specifications			
Year	2006	2012	2018
Focal length	3 mm - 6 mm	3 mm -5 mm	3 mm -5 mm
FOV	66°	72°	78°
F/#	2.8	2.2-2.4	2.0-1.4
TTL	<5.0 mm	<5.0 mm	<6.0 mm
Distortion	<1%-2%	<1%-2%	<1%-2%
CRA	<24°	<30°	<33°
RI	>50%	>50%	>32%
# lens elements	3-5	4-6	5-8

# Chief ray angle



# Image quality

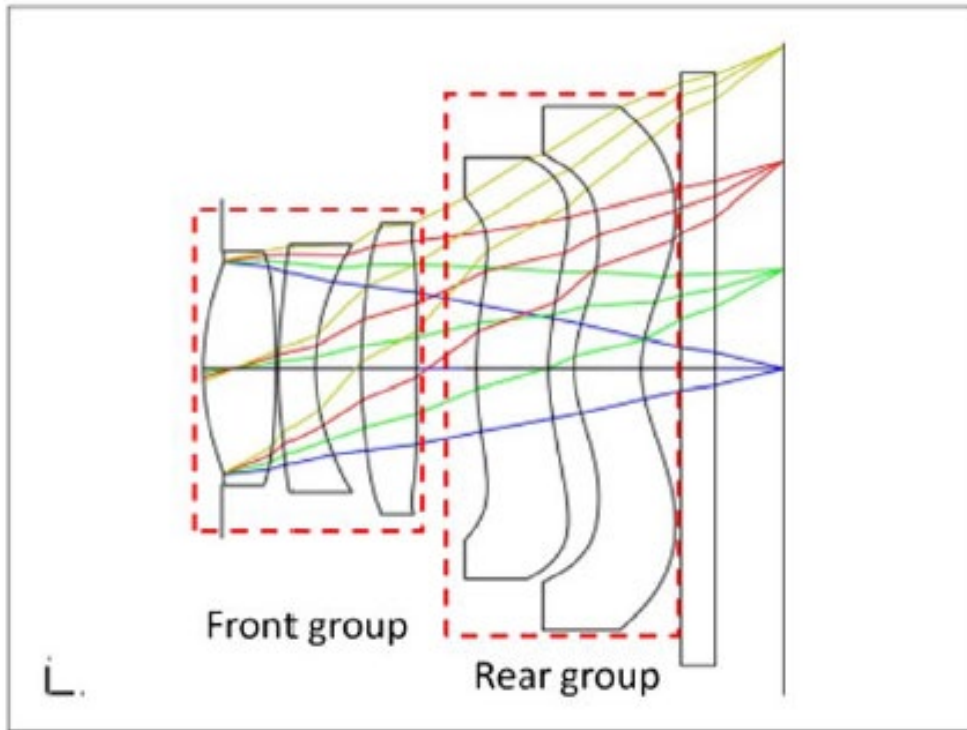
**Example of MTF specifications in fractions of the Nyquist frequency and in cycles/mm for an object at infinity**

	$N_Q$	$N_Q / 2$	$N_Q / 4$
<b>MTF On-axis</b>	>40%	>60%	>80%
<b>MTF Off-axis</b> <b>@ 0.7 field</b>	S>30% T>20%	S>50% T>40%	S>70% T>60%
<b>MTF Off-axis</b> <b>@ 1.0 field</b>	S>20% T>10%	S>30% T>20%	S>40% T>30%

$$N_q = 1/2 \times \text{pixelsize}$$

$$F_c = 1/\lambda f\#$$

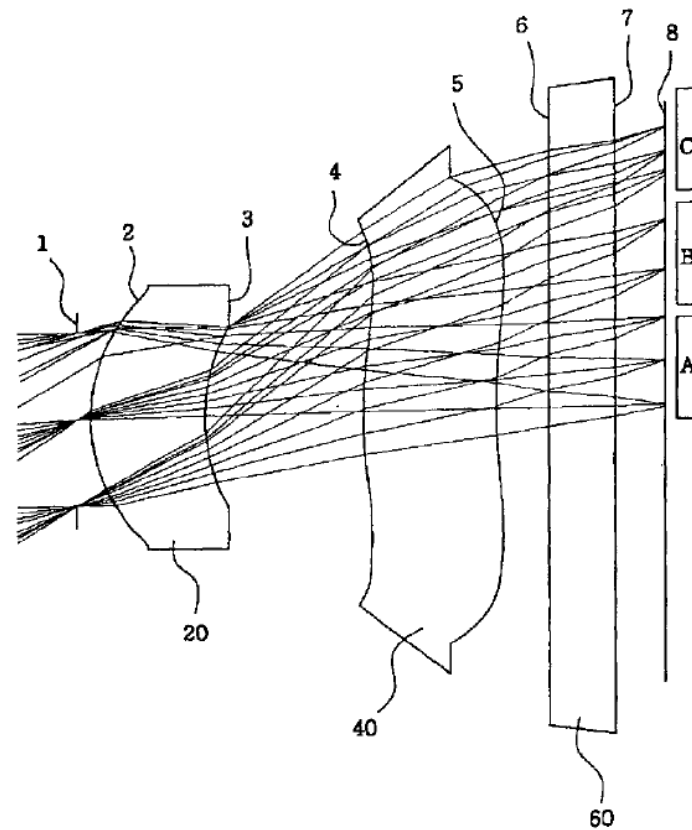
# Aberration correction



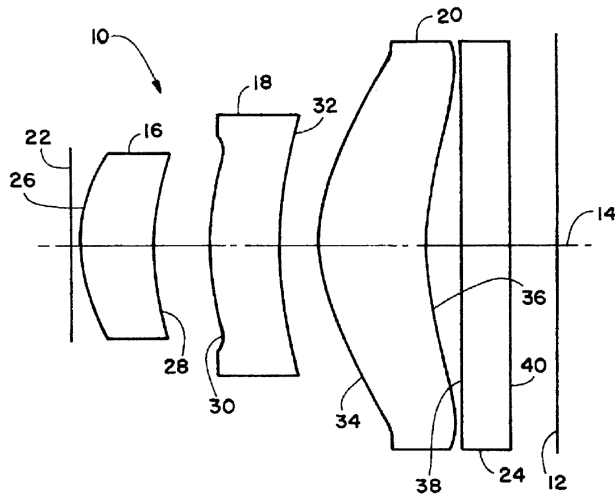
# Jo

**Patent No.:** US 6,853,504 B2

**Date of Patent:** Feb. 8, 2005



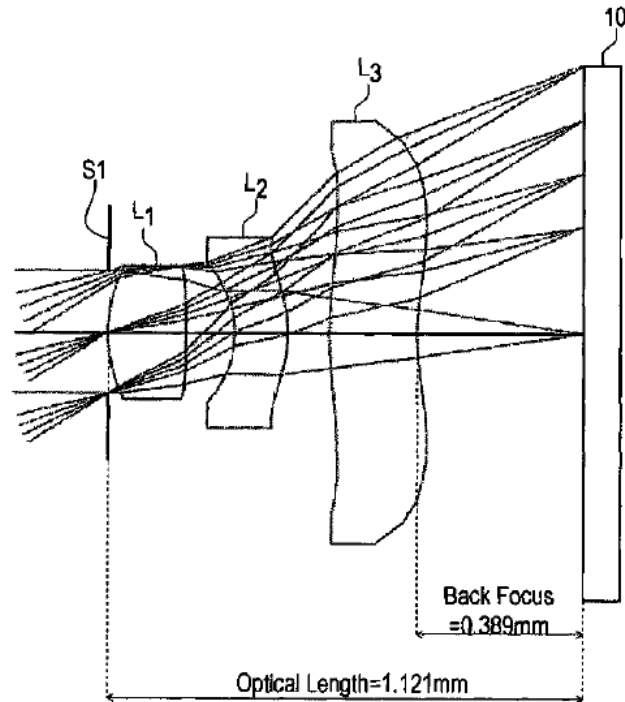
# Ning



**US 6,441,971 B2**  
**Aug. 27, 2002**

# Do

**Patent No.:** US 7,675,692 B2  
**Date of Patent:** Mar. 9, 2010

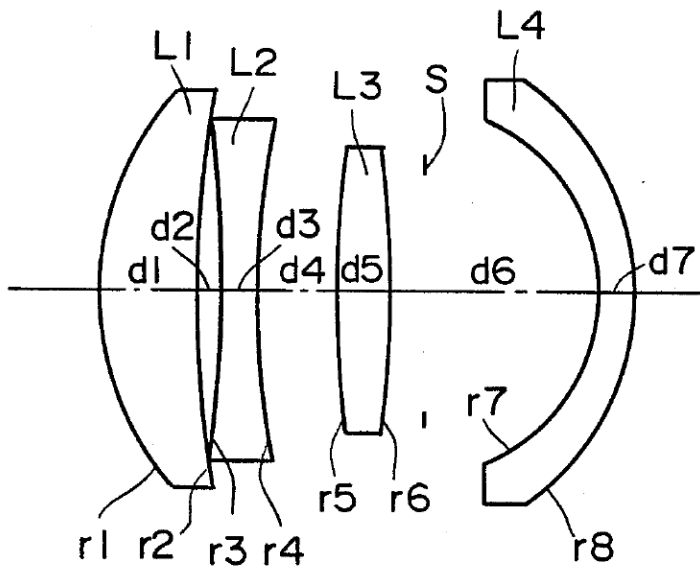




# Kudo

Patent Number: 4,792,216

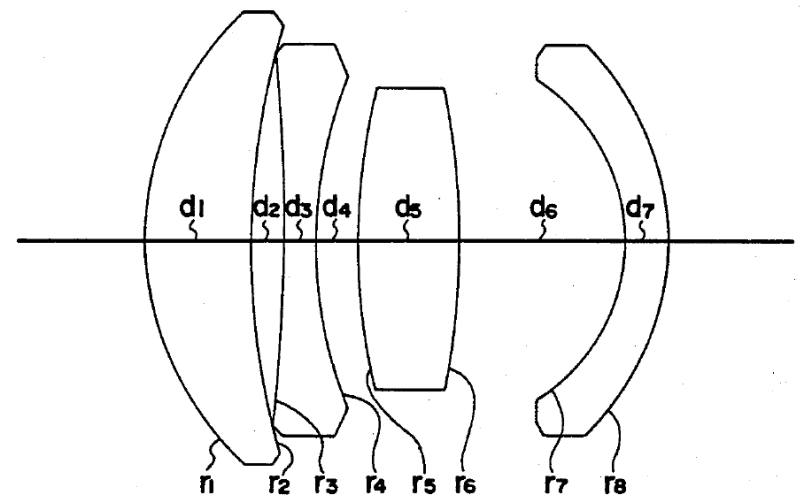
Date of Patent: Dec. 20, 1988



# Mihara

Patent Number: 4,659,190

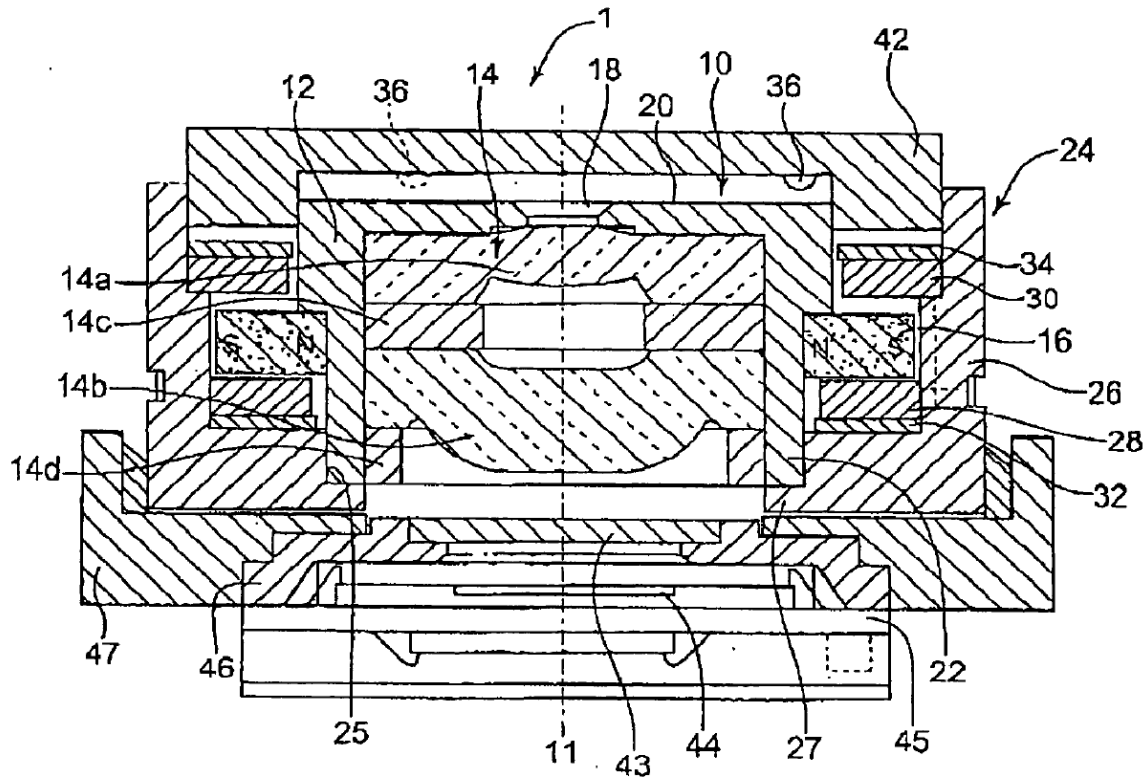
Date of Patent: Apr. 21, 1987



# Tsuruta

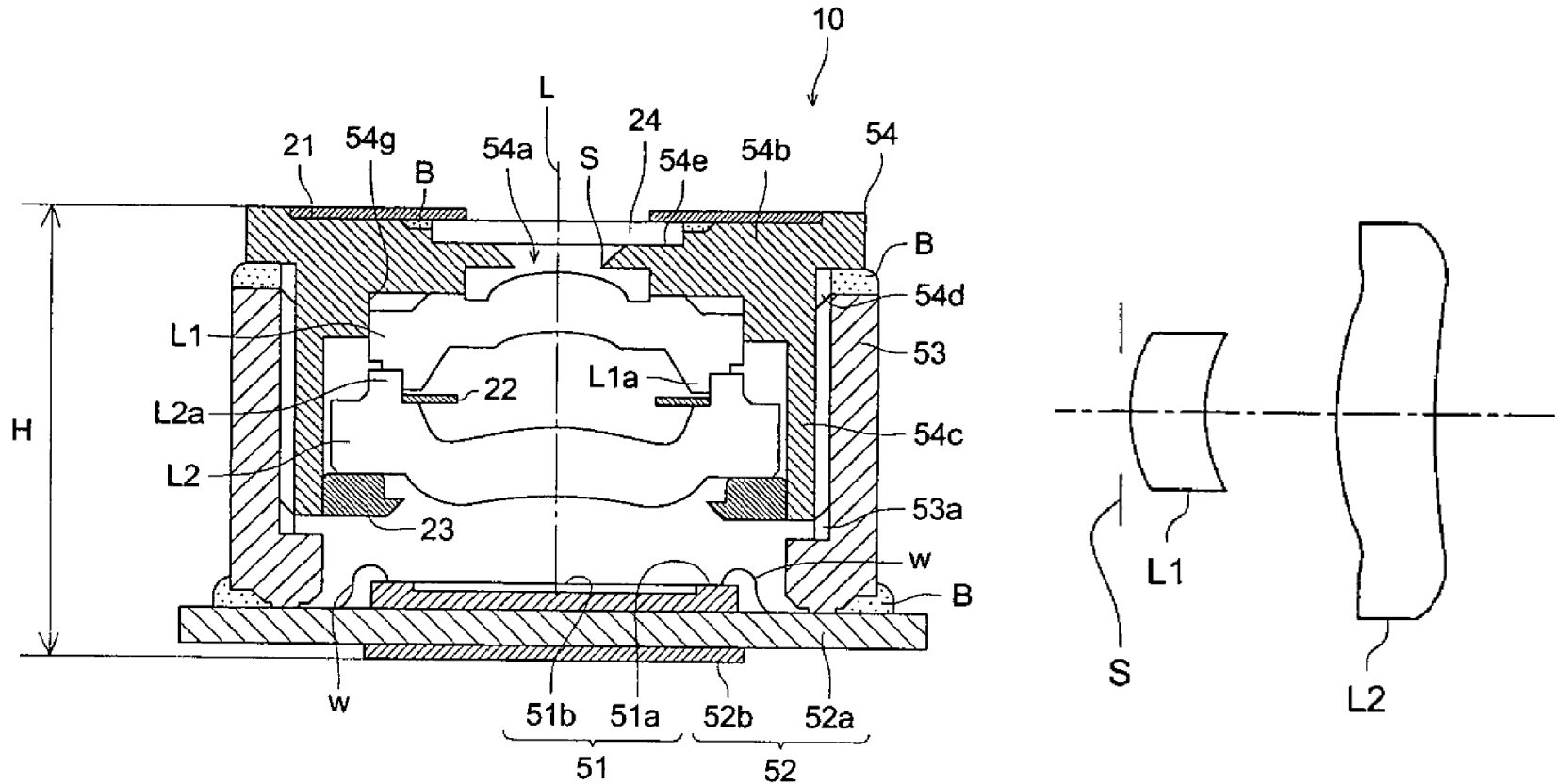
Pub. No.: US 2004/0207745 A1

Pub. Date: Oct. 21, 2004



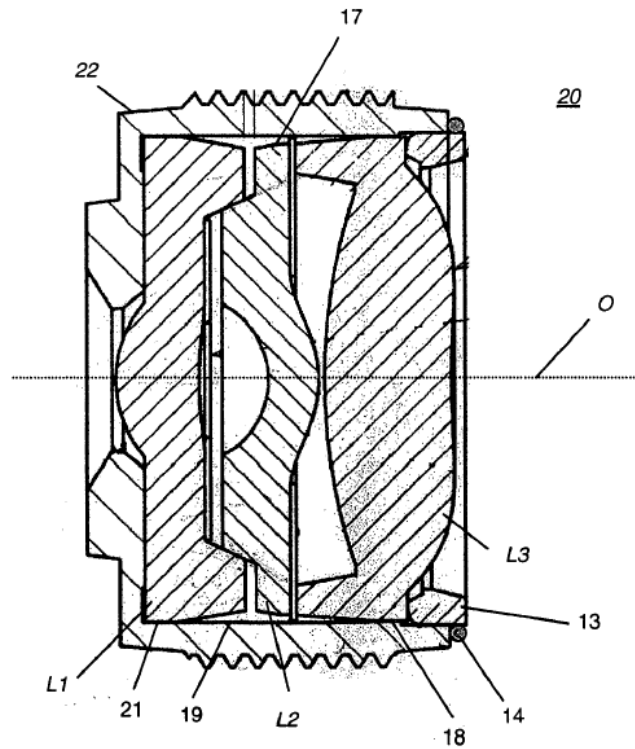
# Yamaguchi

US 2004/0105173



# Recco

Pub. No.: US 2006/0171046 A1  
Pub. Date: Aug. 3, 2006

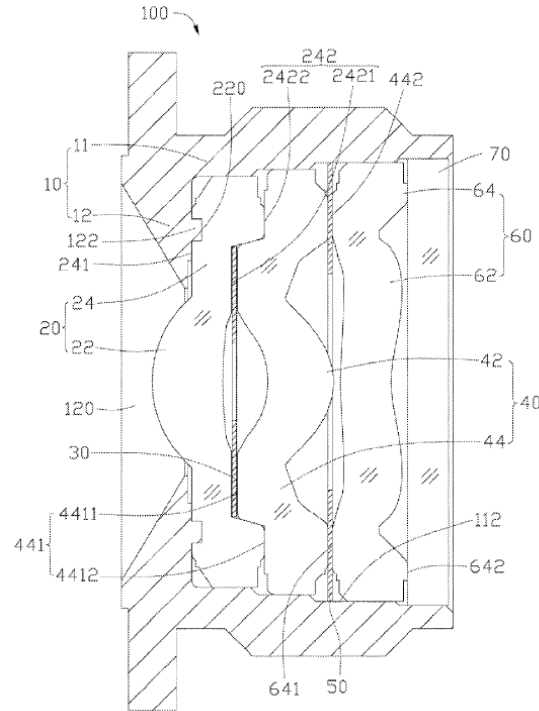


**FIG. 2**

# Lin

**Pub. No.: US 2013/0050850 A1**

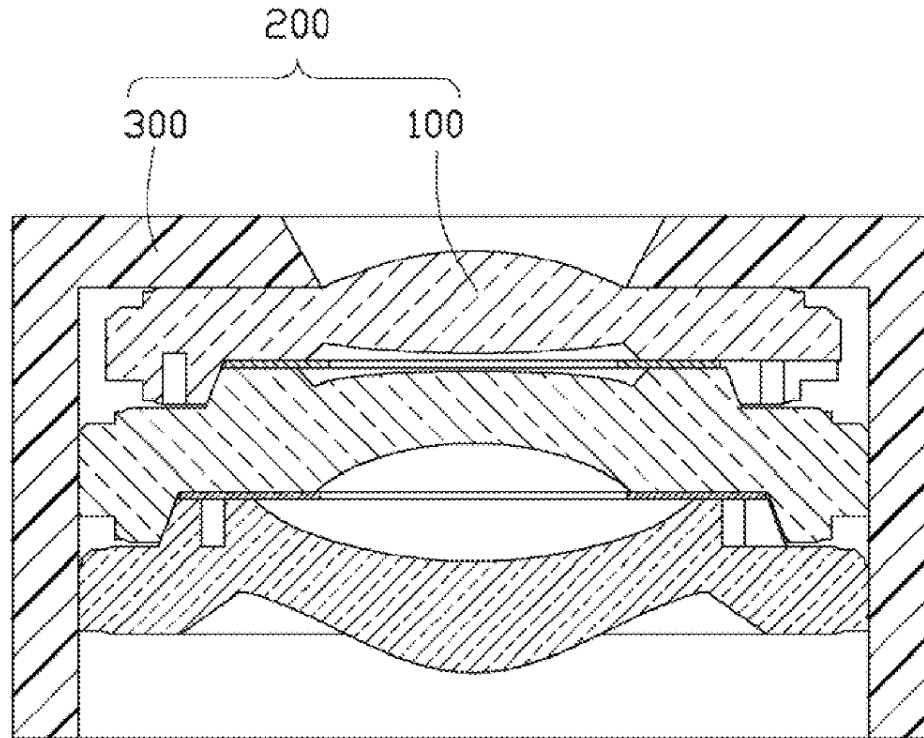
**Pub. Date: Feb. 28, 2013**



# Chou

**Pub. No.: US 2011/0090582 A1**

**Pub. Date: Apr. 21, 2011**



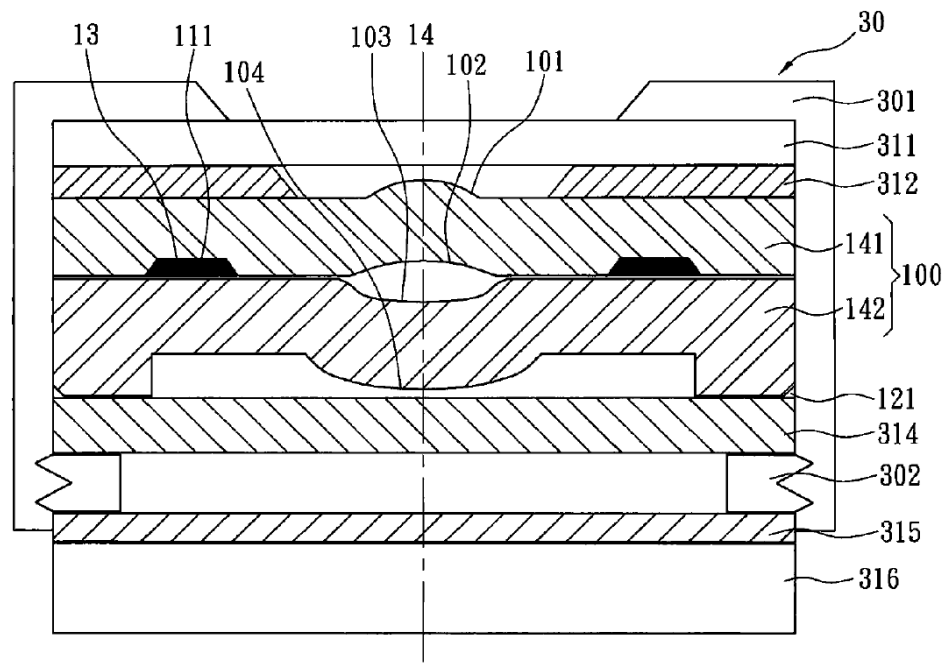
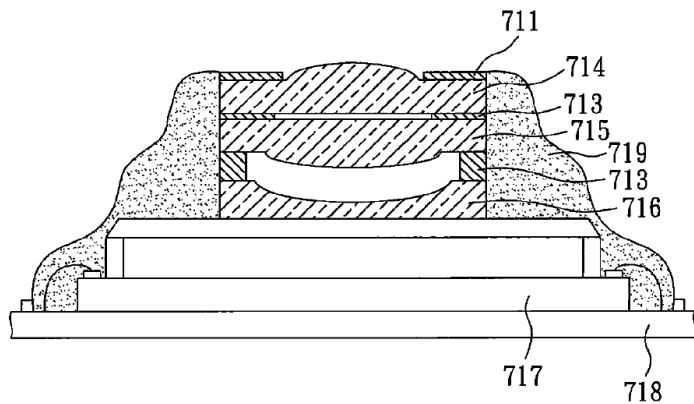
# Shyu

**Patent No.:**

**US 8,023,208 B2**

**Date of Patent:**

**Sep. 20, 2011**



**FIG. 3**

# Lyu

Pub. No.: US 2014/0254034 A1  
Pub. Date: Sep. 11, 2014

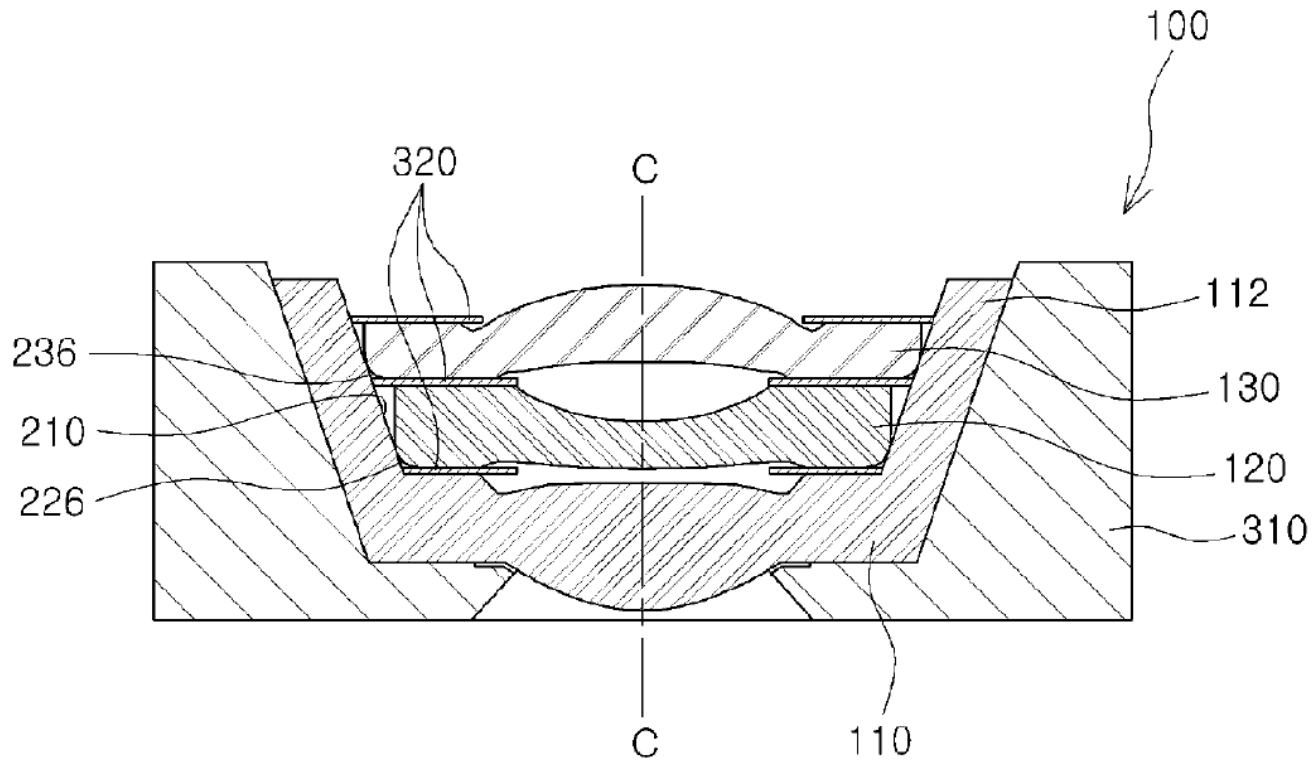


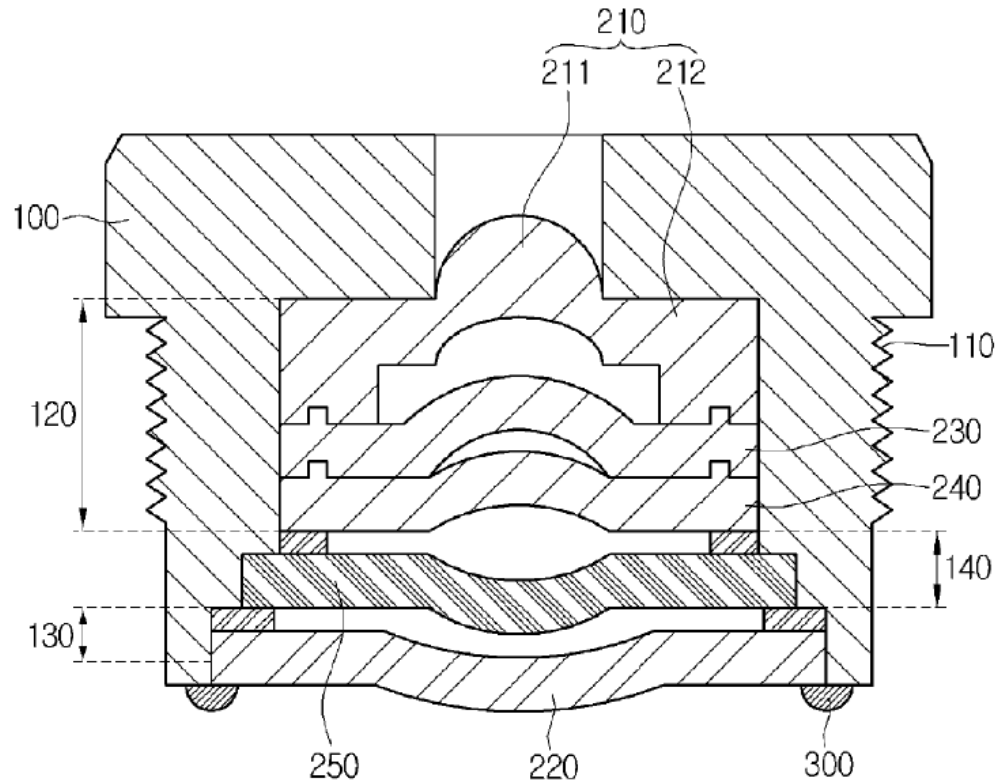
FIG. 3



# Seung

Pub. No.: US 2013/0077183 A1

Pub. Date: Mar. 28, 2013



# Kang

Pub. No.: US 2015/0062727 A1  
Pub. Date: Mar. 5, 2015

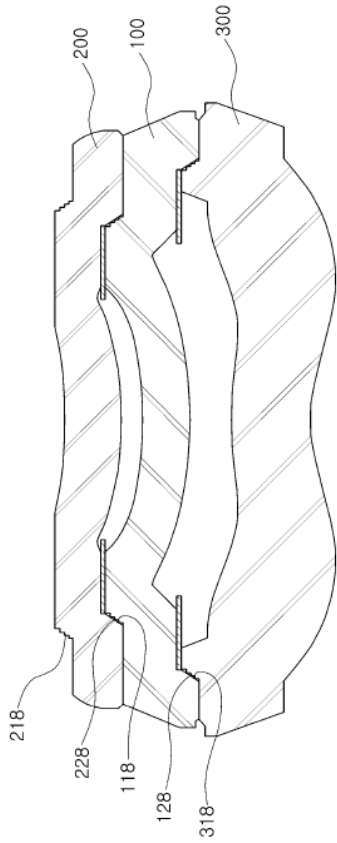


FIG. 7

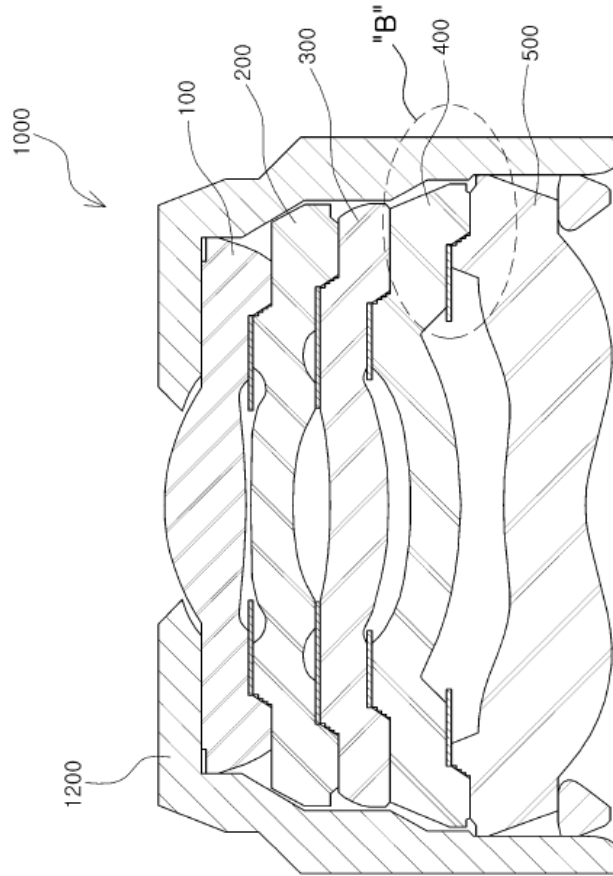


FIG. 10

# Lin

Pub. No.: US 2016/0231526 A1  
Pub. Date: Aug. 11, 2016

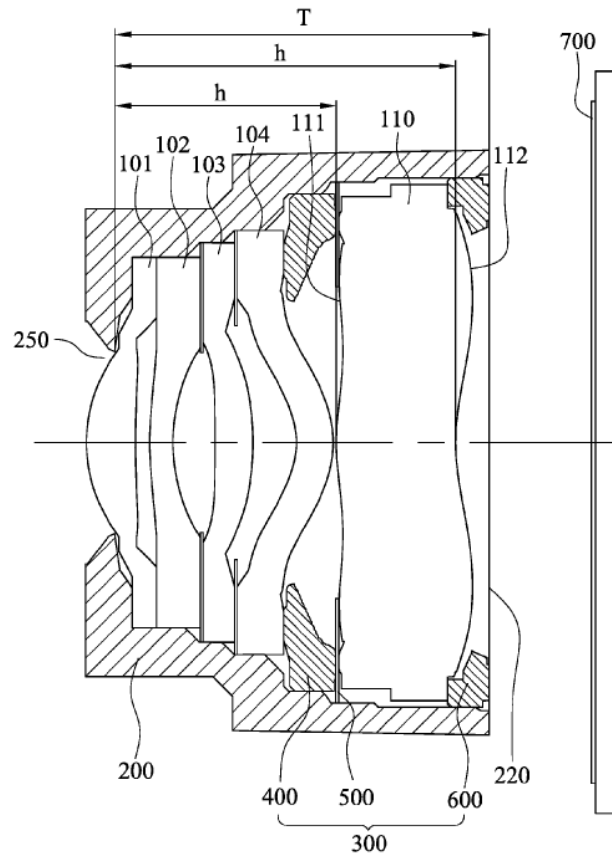
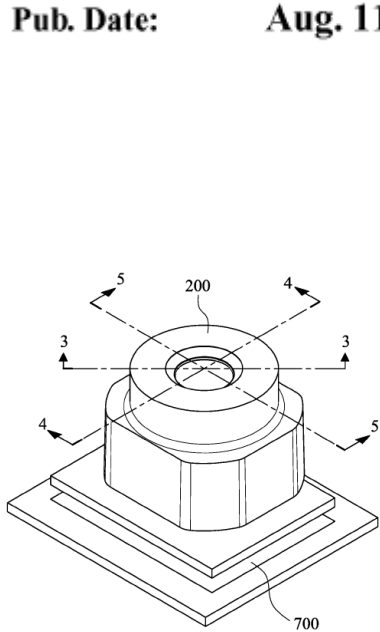


Fig. 5

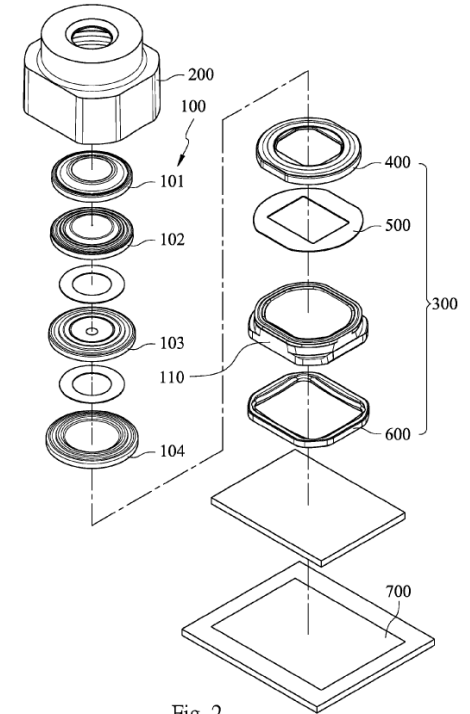


Fig. 2

# Tsai

Pub. No.: US 2018/0129011 A1  
Pub. Date: May 10, 2018

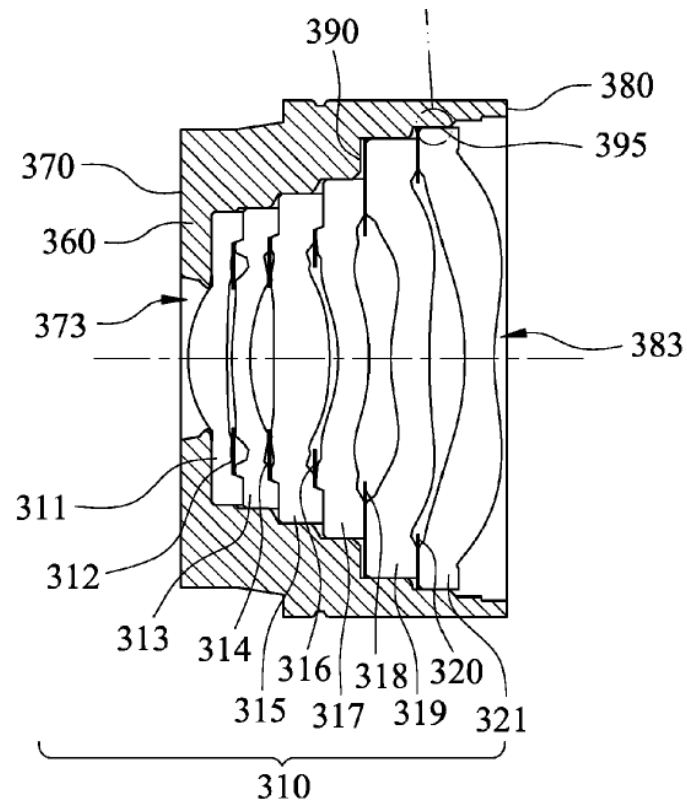


Fig. 3A

# Suwon-Si

Pub. No.: US 2015/0241656 A1

Pub. Date: Aug. 27, 2015

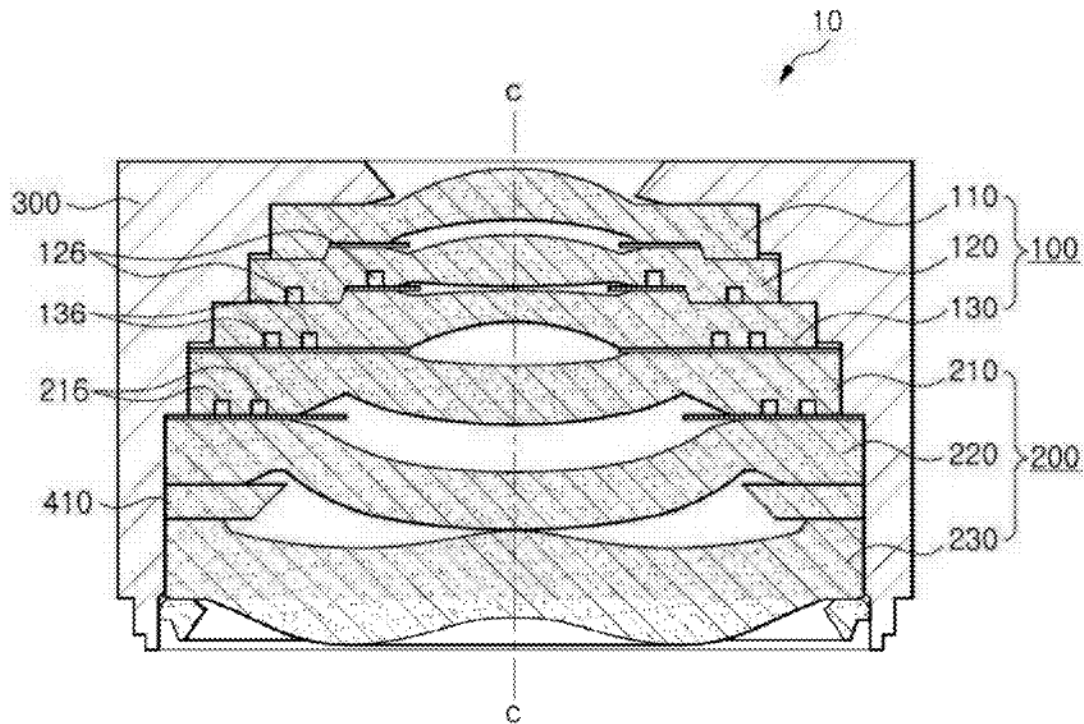
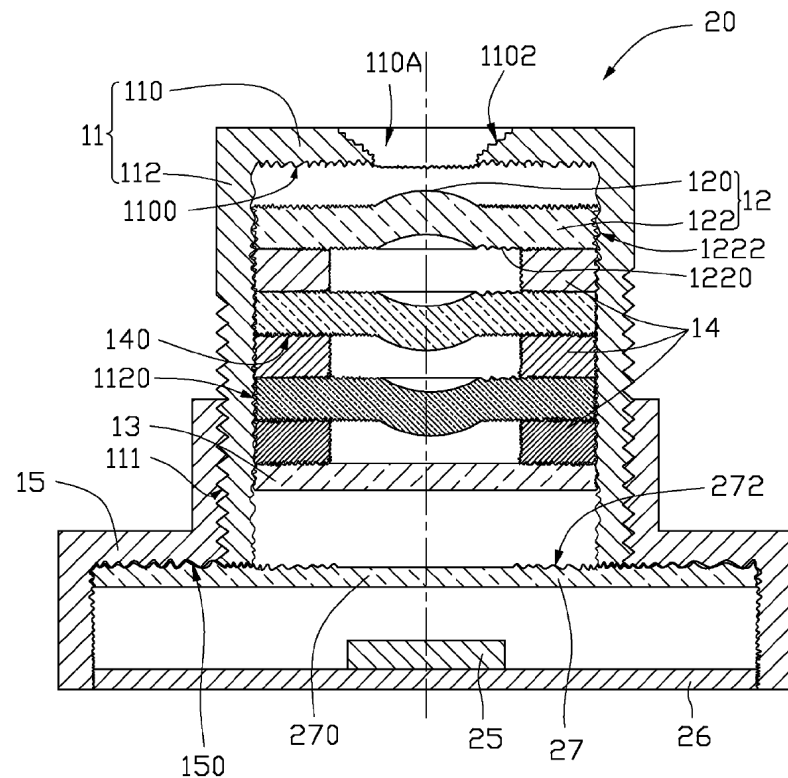


FIG. 12

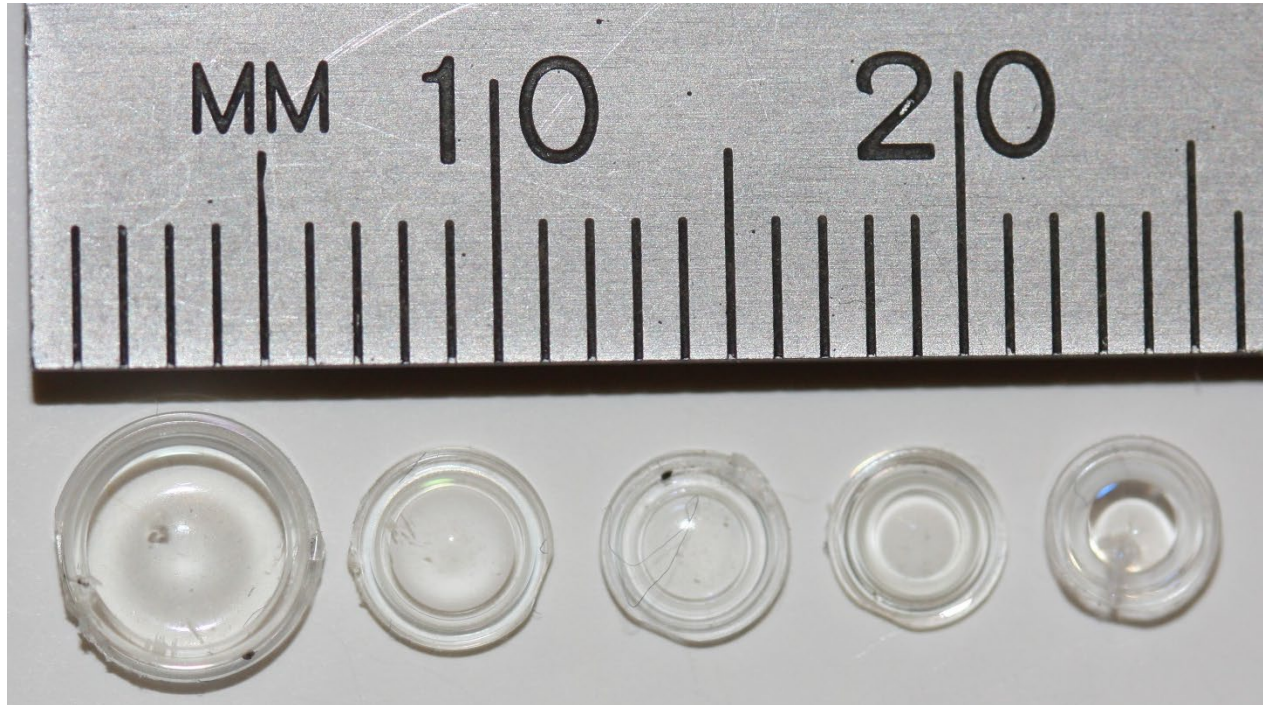
# Chen

Pub. No.: US 2009/0147381 A1

Pub. Date: Jun. 11, 2009



# Rear camera I-phone 6





# Manufacturing

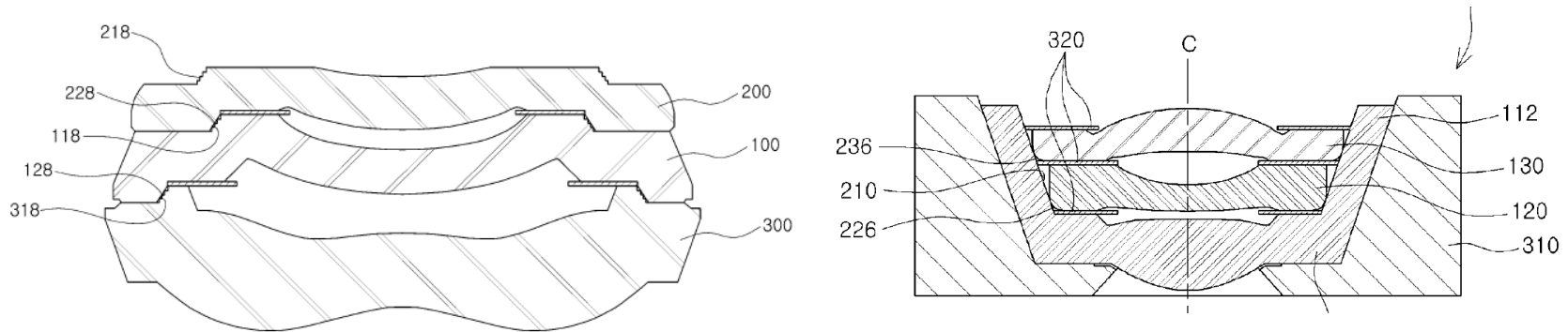


FIG. 7

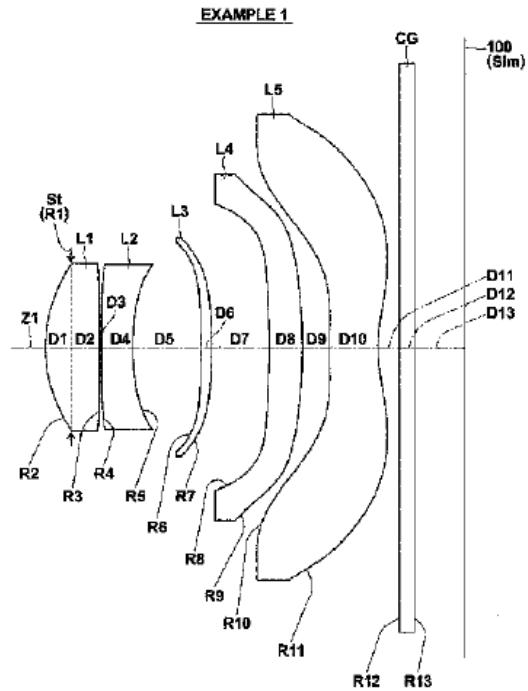
For proper plastic flow and cooling, plastic lens manufacturers have some requirements for the aspect ratio of positive and negative lenses. Some guidelines are as follows: for positive lenses the ratio of lens central thickness to edge thickness should not be no more than 3.2, and the edge thickness should not be less than 0.32 mm; for negative lenses the ratio of the maximum thickness to the central thickness should not be larger than 2.7 and the central thickness should not be less than 0.27 mm.

The ideal lens for injection molding approaches a lens with parallel surfaces so that plastic flow, cooling, and shrinkage are uniform. For miniature lenses tolerances of 10  $\mu\text{m}$  for thickness, decenter, total indicator runoff and lens tilt, are low; tolerances between 2  $\mu\text{m}$  and 5  $\mu\text{m}$  are medium and feasible to achieve in manufacturing, and tolerances between 0.5  $\mu\text{m}$  and 2  $\mu\text{m}$  are challenging to achieve and are met for some miniature optics.

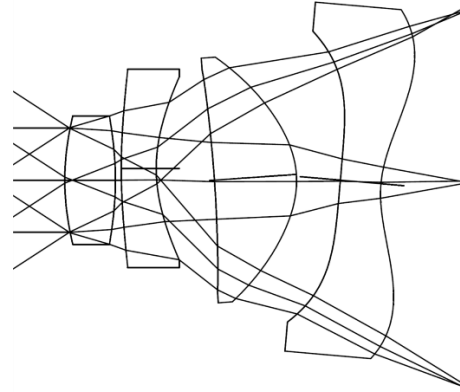


# Iwasaki

Patent No.: US 9,678,310 B2  
Date of Patent: Jun. 13, 2017



# Desensitizing

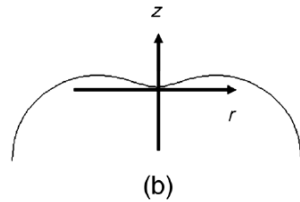
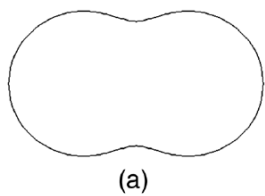


**Lens configuration setting for desensitizing a Cooke triplet lens for lens wedge.**

**Units are in mm and degrees.**

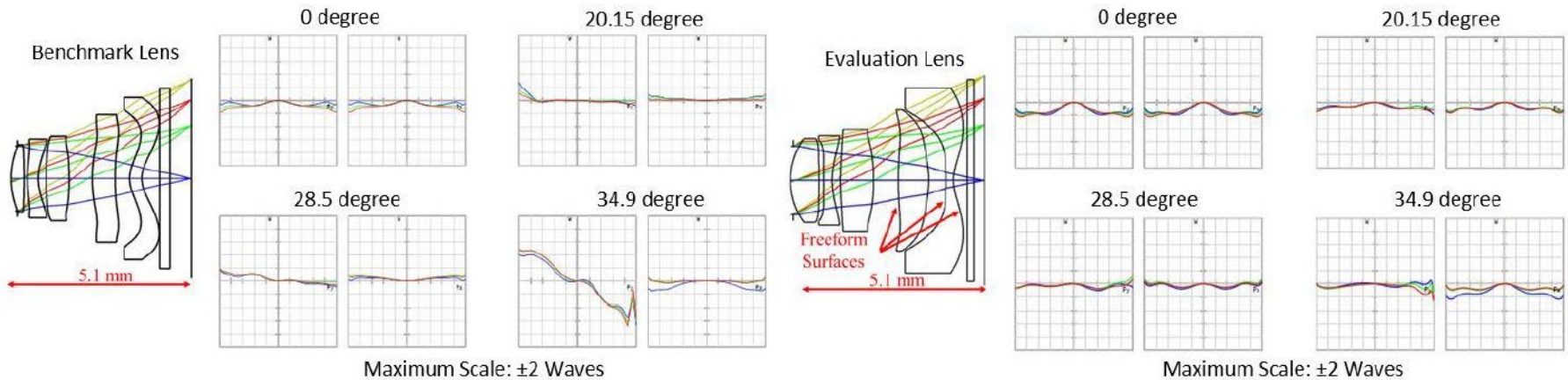
Configuration	1	2	3	4	5	6	7
Focal length	100						
Surface #1 tilt		0.1°					
Surface #2 tilt			0.1°				
Surface #3 tilt				0.1°			
Surface #4 tilt					0.1°		
Surface #5 tilt						0.1°	
Surface #6 tilt							0.1°

# Choice of surface



$$S(r) = b - \sqrt{\frac{b^2 - 2r^2 + \sqrt{b^4 + 4(a^2 - b^2)r^2}}{2}}$$

$$z_p(r) = A_1 S_1(r) + A_2 S_1^2(r) + A_3 S_1^3(r) + B_1 S_1(r) + B_2 S_1^2(r) + B_3 S_1^3(r),$$



## Miniature Camera Lens Design with a Freeform Surface

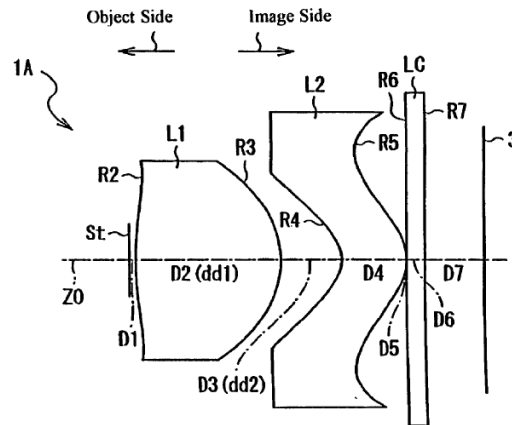
Yufeng Yan and Jose Sasian

Prof. Jose Sasian

# Aspheric coefficients

Shinohara

Even and odd  
Aspheric surfaces



Pub. No.: US 2003/0117723 A1

Pub. Date: Jun. 26, 2003

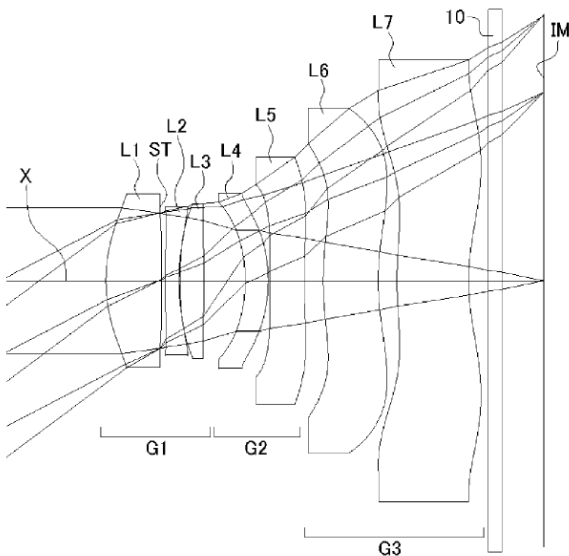
TABLE 6

#	C	K	$A_4$	$A_6$	$A_8$	$A_{10}$
2	0.2416	-16.7875	6.3491E-03	-5.5390E-03	3.1005E-06	5.7561E-07
3	-0.8046	-0.9488	-3.4059E-02	-1.6547E-04	-5.2245E-07	-1.3727E-09
4	-2.0019	-0.4916	1.5323E-02	7.4362E-05	2.4722E-07	6.9822E-10
5	-1.6571	-0.7550	3.1674E-02	4.9464E-04	2.5648E-05	3.1273E-07

# Aspheric coefficients

Kubota

Patent No.: US 9,146,380 B2  
Date of Patent: Sep. 29, 2015



## Aspheric Surface Data

### First Surface

$k = 0.000, A_4 = -2.995E-03, A_6 = -1.855E-04, A_8 = -2.472E-04,$   
 $A_{10} = -3.907E-06, A_{12} = -5.270E-07, A_{14} = 2.761E-07,$   
 $A_{16} = -1.217E-09$

### Second Surface

$k = 0.000, A_4 = 1.174E-02, A_6 = -1.391E-02, A_8 = 5.212E-03, A_{10} =$   
 $-9.563E-04, A_{12} = 7.839E-05, A_{14} = -2.213E-06, A_{16} = 5.641E-08$

$f = 9.57 \text{ mm}, Fno = 2.4, \omega = 32.1^\circ$   
Unit: mm

### Fourth Surface

$k = 0.000, A_4 = 1.333E-02, A_6 = -2.008E-02, A_8 = 7.838E-03, A_{10} =$   
 $-1.302E-03, A_{12} = 7.691E-05, A_{14} = 5.904E-07, A_{16} = -5.005E-07$

### Fifth Surface

$k = 0.000, A_4 = 6.851E-03, A_6 = -1.313E-02, A_8 = 3.616E-03, A_{10} =$   
 $-2.531E-04, A_{12} = -2.370E-05, A_{14} = -1.000E-05, A_{16} = 1.564E-06$

### Sixth Surface

$k = 0.000, A_4 = 1.103E-02, A_6 = -2.591E-03, A_8 = 1.170E-03, A_{10} =$   
 $-4.329E-05, A_{12} = -5.911E-06, A_{14} = 2.463E-06, A_{16} = -1.368E-06$

### Seventh Surface

$k = 0.000, A_4 = -1.065E-03, A_6 = 2.211E-03, A_8 = 8.593E-04, A_{10} =$   
 $-4.613E-04, A_{12} = 7.895E-05, A_{14} = 7.220E-06, A_{16} = -5.043E-06$

### Eighth Surface

$k = 0.000, A_4 = -1.547E-02, A_6 = 2.513E-03, A_8 = -2.149E-05, A_{10} =$   
 $-2.485E-04, A_{12} = -1.856E-05, A_{14} = 1.073E-07, A_{16} = 1.527E-06$

### Ninth Surface

$k = 0.000, A_4 = -6.920E-03, A_6 = 1.871E-03, A_8 = 8.894E-05, A_{10} =$   
 $1.388E-06, A_{12} = -2.970E-05, A_{14} = -1.020E-06, A_{16} = 2.369E-06$

### Tenth Surface

$k = 0.000, A_4 = -8.230E-03, A_6 = -9.253E-04, A_8 = -7.779E-05,$   
 $A_{10} = 6.194E-06, A_{12} = -1.505E-06, A_{14} = 5.207E-07,$   
 $A_{16} = -3.481E-08$

### Eleventh Surface

$k = 0.000, A_4 = -1.020E-02, A_6 = -6.061E-04, A_8 = 1.202E-04, A_{10} =$   
 $1.683E-06, A_{12} = 1.154E-07, A_{14} = -4.525E-08, A_{16} = 7.640E-11$

### Twelfth Surface

$k = 0.000, A_4 = -1.374E-02, A_6 = -3.962E-04, A_8 = -3.784E-05,$   
 $A_{10} = -2.372E-06, A_{12} = 1.515E-07, A_{14} = 2.223E-08,$   
 $A_{16} = -2.404E-09$

### Thirteenth Surface

$k = 0.000, A_4 = -1.172E-02, A_6 = 2.665E-05, A_8 = 2.272E-05, A_{10} =$   
 $-1.026E-06, A_{12} = -5.260E-09, A_{14} = 1.463E-09, A_{16} = -2.885E-11$

### Fourteenth Surface

$k = 0.000, A_4 = -2.216E-02, A_6 = 1.317E-03, A_8 = -2.194E-05, A_{10} =$   
 $-2.470E-07, A_{12} = 6.753E-10, A_{14} = 1.105E-10, A_{16} = 1.524E-11$

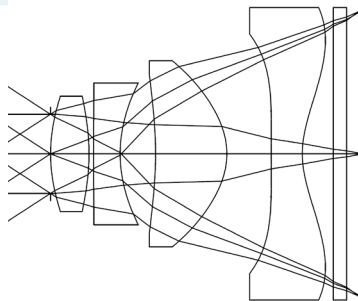
### Fifteenth Surface

$k = -1.551E+01, A_4 = -9.918E-03, A_6 = 3.875E-04, A_8 = -1.268E-05,$   
 $A_{10} = 1.234E+07, A_{12} = 9.762E-09, A_{14} = -5.202E-10, A_{16} =$   
 $6.871E-12$

# Prescription table

Example of a four lens element design for a mobile phone lens.  
 $F=5.0$  mm,  $FOV=+/-32^\circ$ ,  $TTL/f=1.4$ ,  $F/2.8$ .  $CRA=30.6^\circ$ .

Surface	Radius	Thickness	Plastic	K	$A_4$
<b>STOP</b>					
<b>2</b>	3.5432.72	0.87	E48R	-3.2457	
<b>3</b>	-4.57977	0.1		-11.7213	
<b>4</b>	126.2449	0.6	OKP4	0.0	
<b>5</b>	3.013807	0.8		-0.9977	-2.533E-3
<b>6</b>	-8.81693	1.61	E48R	0.0	4.161E-3
<b>7</b>	-1.61409	1.0		-2.2699	-0.0126713
<b>8</b>	72.73421	0.7	OKP4	0.0	-0.0100888
<b>9</b>	2.101288	0.7		-6.3020	-6.073E-3
<b>10</b>	Plano	0.3	BK7		
<b>11</b>	Plano	0.4			
<b>Image</b>					



# Materials

Properties of some plastics used  
in mobile phone lenses

Code	$n_d$	$v$	$\gamma$	$\rho$
480R	1.525	55.95	$+1.44 \times 10^{-4}$	1.01
E48R	1.531	56.04	$-2.62 \times 10^{-4}$	1.02
F52R	1.534	57.09	$-2.21 \times 10^{-4}$	1.01
OKP4	1.607	26.90	$-3.44 \times 10^{-4}$	1.20
OKP4HT	1.632	23.33	$-2.72 \times 10^{-4}$	1.24

- Water absorption
- Light scattering and haze
- Transmission
- CTE
- $Dn/dt$
- Opto-thermal coefficients
- Durability
- Birefringence

Links to optical plastics vendors:

<http://www.ogc.co.jp/e/products/fluorene/okp.html>

<https://www.zeonex.com/Optics.aspx.html#glass-like>

# Zooms/folded

Pub. No.: US 2007/0258711 A1  
 Pub. Date: Nov. 8, 2007

Pub. No.: US 2016/0231540 A1  
 Pub. Date: Aug. 11, 2016

Patent No.: US 7,626,767 B2  
 Date of Patent: Dec. 1, 2009

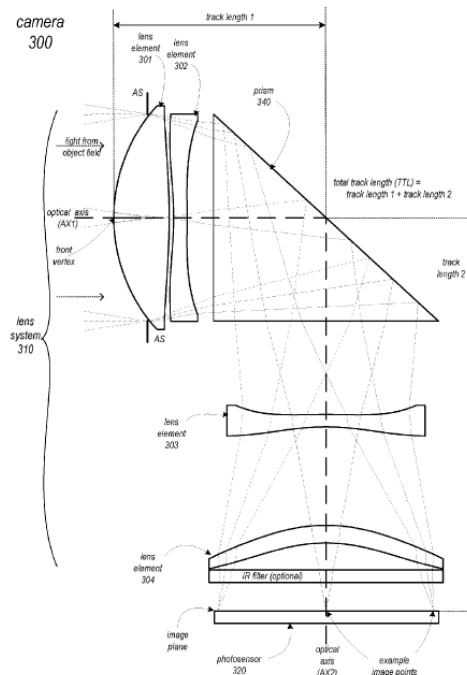
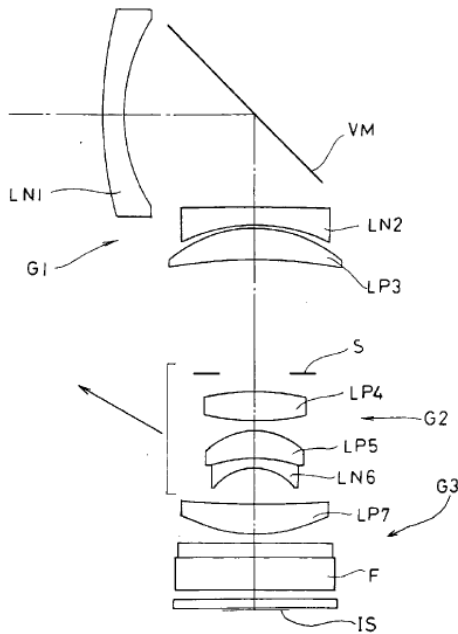
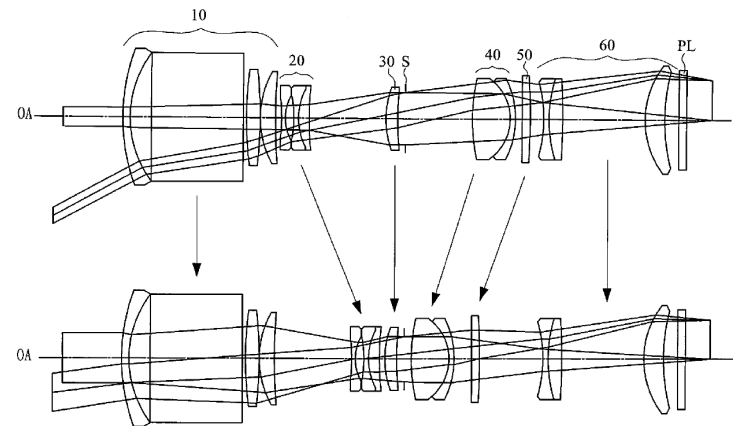


FIG. 5A





# Papers

1. P. Clark, “Lens design and advanced function for mobile cameras,” Chapter 1, in *Smart Mini-Cameras*, Galstian, T. V. Editor, CRC Press, Boca Raton, FL, (2014).
2. Jane Bateau, Peter P. Clark, "The optics of miniature digital camera modules", Proc. SPIE 6342, International Optical Design Conference 2006, 63421F (25 July 2006); doi: 10.1117/12.692291; <https://doi.org/10.1117/12.692291>
3. Peter P. Clark, "Mobile platform optical design", Proc. SPIE 9293, International Optical Design Conference 2014, 92931M (17 December 2014); doi: 10.1117/12.2076395; <https://doi.org/10.1117/12.2076395>
4. M. Schaub, “The design of plastic optical systems,” SPIE Press, Vol. TT80, 2009.
5. Reshidko, D., & Sasian, J. (2015). Optical analysis of miniature lenses with curved imaging surfaces. *Applied Optics*, 54(28), E216-E223. DOI: 10.1364/AO.54.00E216
6. Yufeng Yan, Jose Sasian, "Miniature camera lens design with a freeform surface", Proc. SPIE 10590, International Optical Design Conference 2017, 1059012 (27 November 2017); doi: 10.1117/12.2292653; <https://doi.org/10.1117/12.2292653>