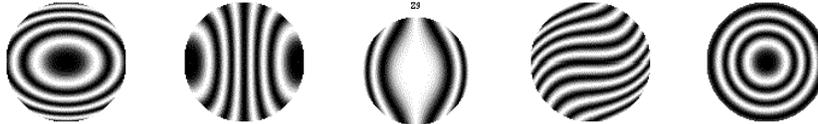




Introduction to Interferometric Optical Testing



James C. Wyant
College of Optical Sciences
University of Arizona
jcwyant@optics.arizona.edu
www.optics.arizona.edu
www.optics.arizona.edu/jcwyant

Outline



- 1. Basic Interferometers for Optical Testing
- 2. Phase-Shifting Interferometry
- 3. Specialized Optical Tests
- 4. Long Wavelength Interferometry
- 5. Testing of Aspheric Surfaces
- 6. Measurement of Surface Microstructure
- 7. Absolute Measurements
- 8. Concluding Remarks

Part 1 - Basic Interferometers for Optical Testing



- Two Beam Interference
- Fizeau and Twyman-Green interferometers
- Basic techniques for testing flat and spherical surfaces
- Scatterplate and Smartt Interferometers
- Lateral Shearing Interferometers
- Typical Interferograms

Two-Beam Interference Fringes



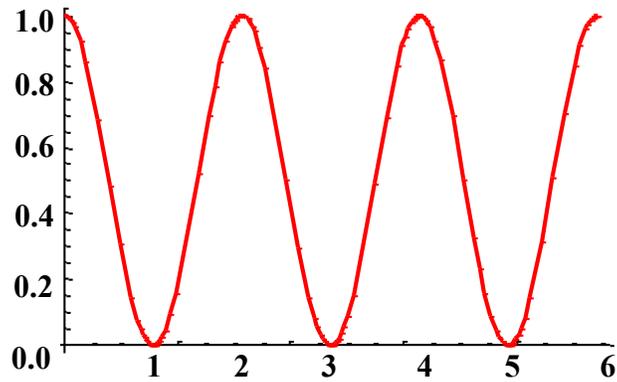
$$I = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos(\alpha_1 - \alpha_2)$$

$\alpha_1 - \alpha_2$ is the phase difference between the two interfering beams

$$\alpha_1 - \alpha_2 = \left(\frac{2\pi}{\lambda} \right) (\text{optical path difference})$$



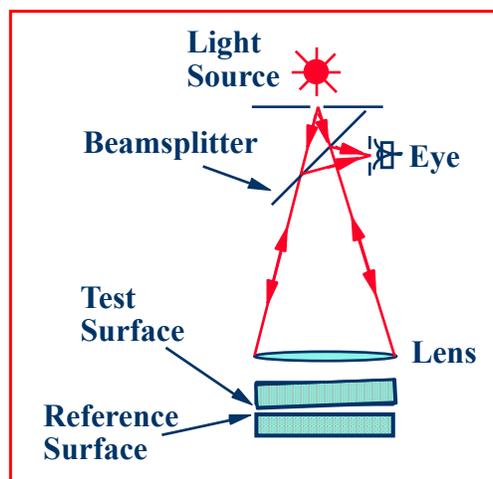
Sinusoidal Interference Fringes



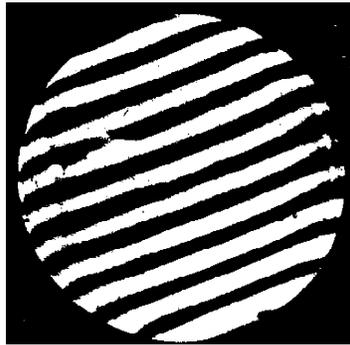
$$I = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos(\alpha_1 - \alpha_2)$$



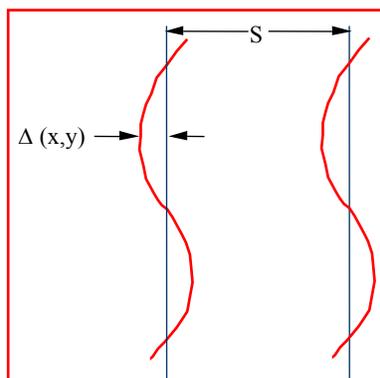
Pioneer Fizeau Interferometer - 1862



Typical Interferogram Obtained using Fizeau Interferometer



Relationship between Surface Height Error and Fringe Deviation



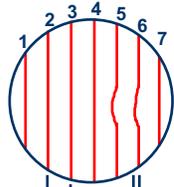
$$\text{Surface height error} = \left(\frac{\lambda}{2}\right)\left(\frac{\Delta}{S}\right)$$



Fizeau Fringes

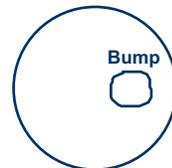


Top View

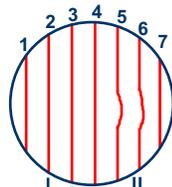


Interferogram

For a given fringe the separation between the two surfaces is a constant.



Top View

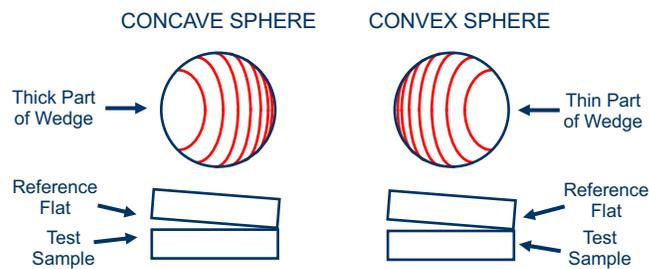


Interferogram

$$\text{Height error} = (\lambda/2)(\Delta/S)$$



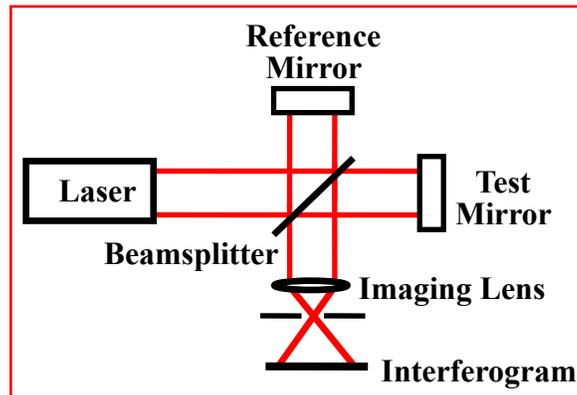
Fizeau Fringes for Concave and Convex Surfaces



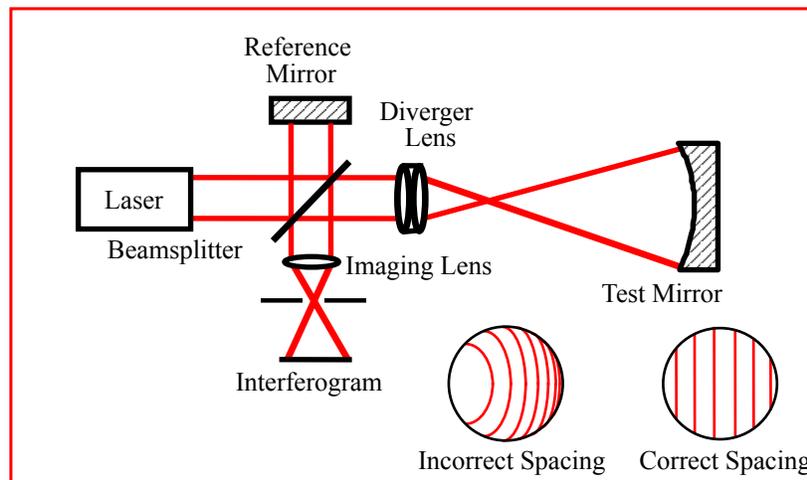


Twyman-Green Interferometer (Flat Surfaces)

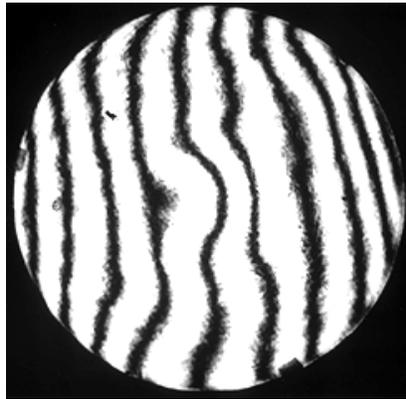
1918



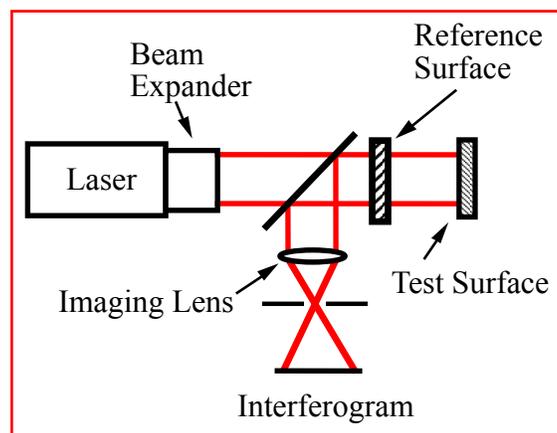
Twyman-Green Interferometer (Spherical Surfaces)



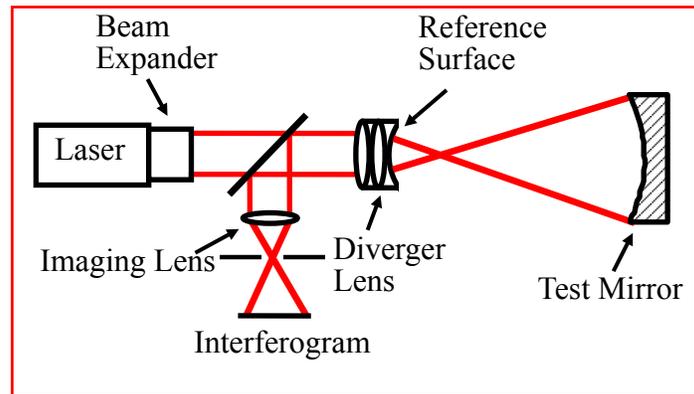
Typical Interferogram



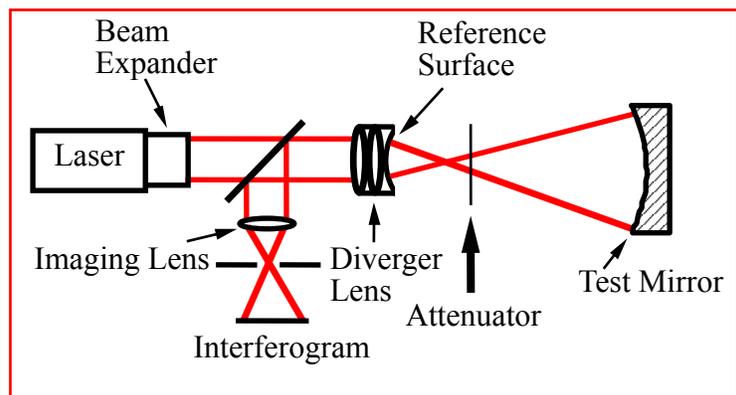
Fizeau Interferometer-Laser Source (Flat Surfaces)



Fizeau Interferometer-Laser Source (Spherical Surfaces)

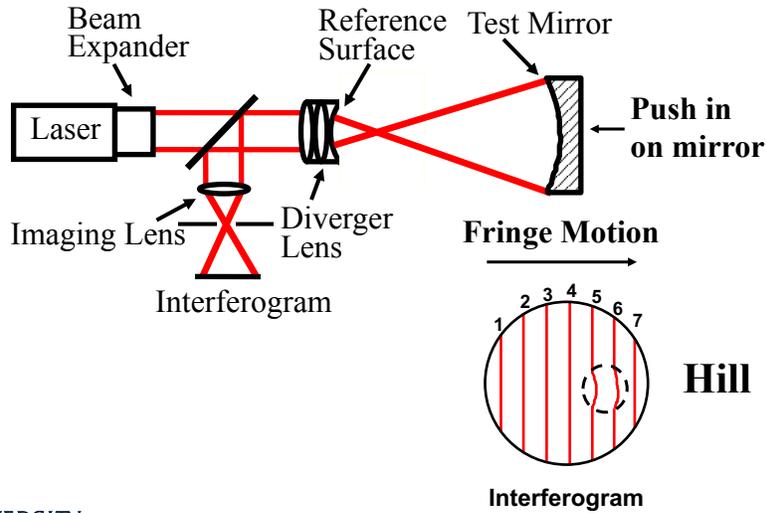


Testing High Reflectivity Surfaces

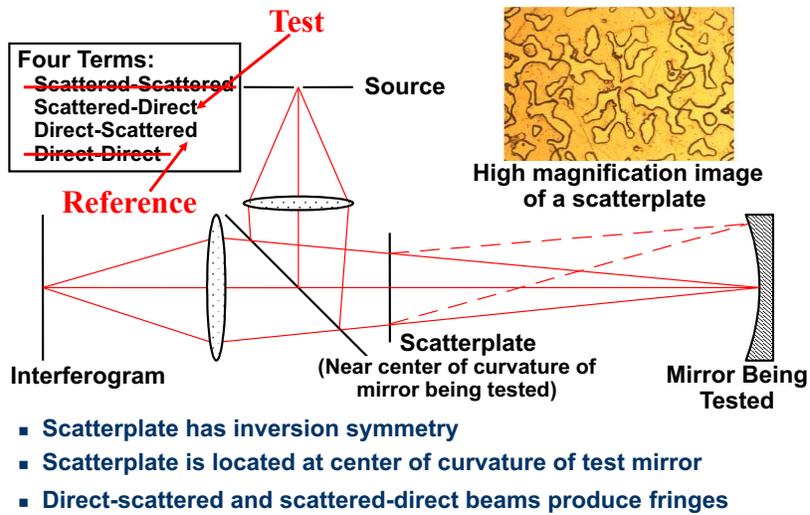




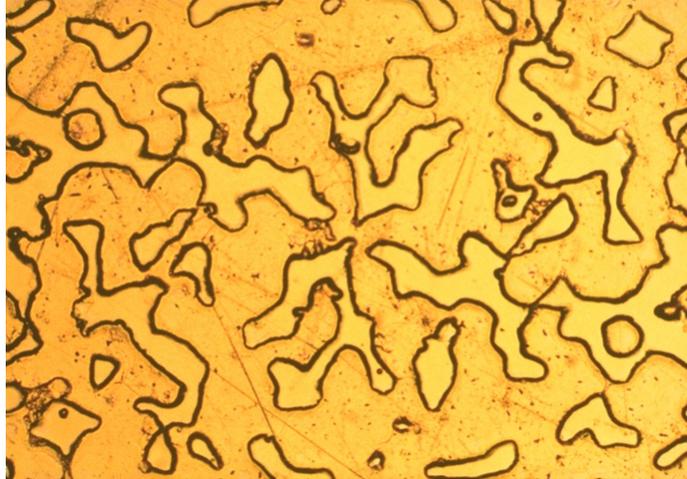
Hill or Valley?



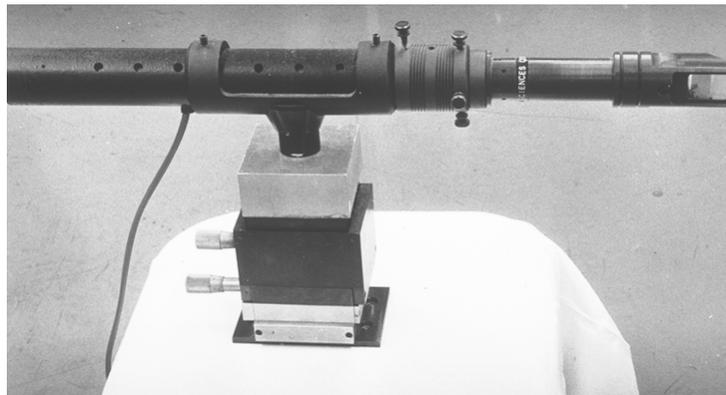
Scatterplate Interferometer



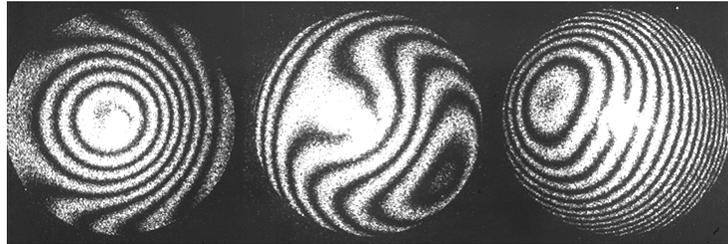
Microscopic Image of Scatterplate



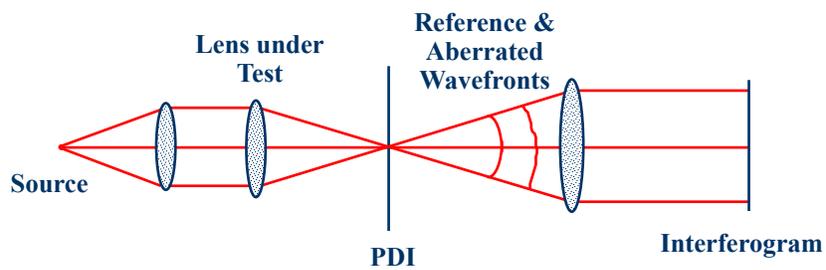
Scatterplate Interferometer



Scatterplate Interferograms



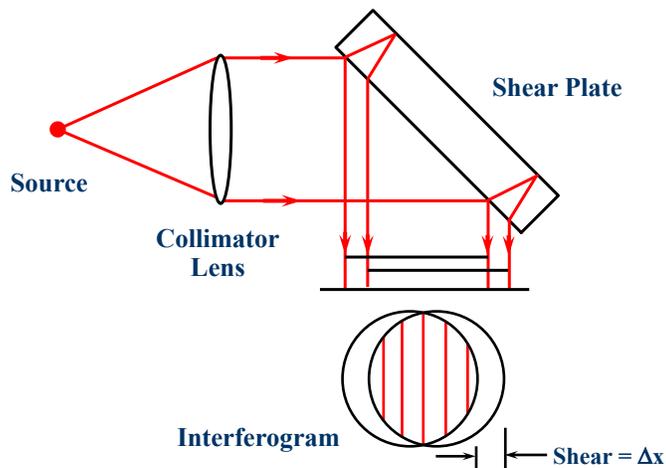
Smartt Point Diffraction Interferometer





Lateral Shear Interferometry

Measures wavefront slope



Lateral Shear Fringes

$\Delta W(x, y)$ is wavefront being measured

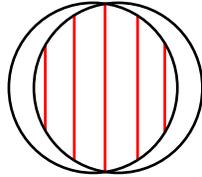
Bright fringe obtained when

$$\Delta W(x + \Delta x, y) - \Delta W(x, y) = m\lambda$$

$$\left(\frac{\partial \Delta W(x, y)}{\partial x} \text{ Average over shear distance} \right) (\Delta x) = m\lambda$$

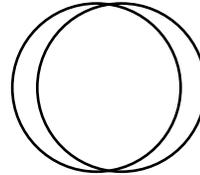
Measures average value of slope over shear distance

Collimation Measurement

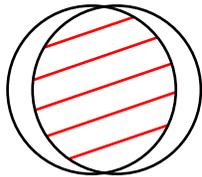


Not collimated

No wedge in shear plate

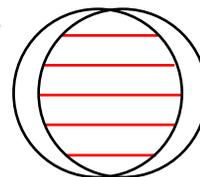


Collimated (one fringe)



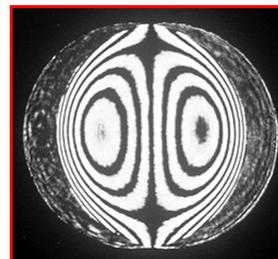
Not collimated

Vertical wedge in shear plate



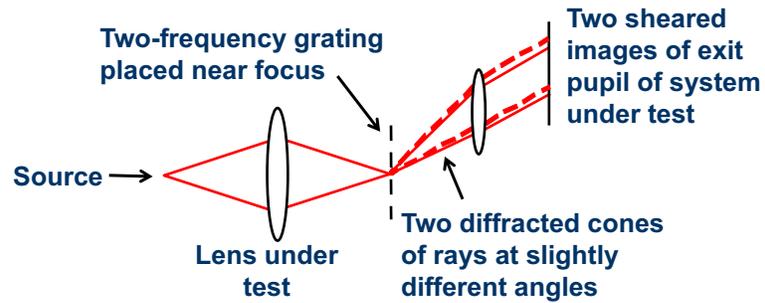
Collimated

Typical Lateral Shear Interferograms





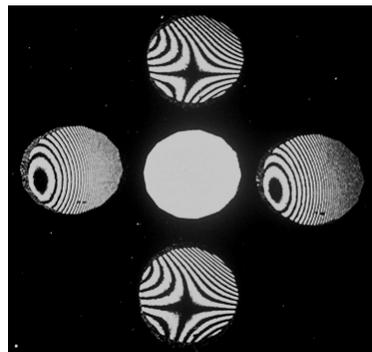
Lateral Shear Interferometer



Measures slope of wavefront, not wavefront shape.

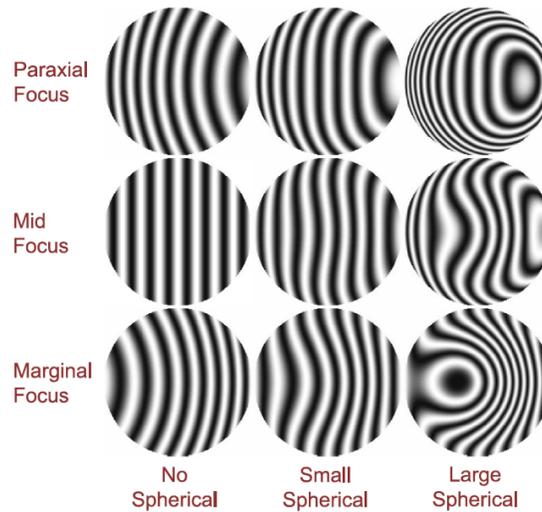


Interferogram Obtained using Grating Lateral Shear Interferometer

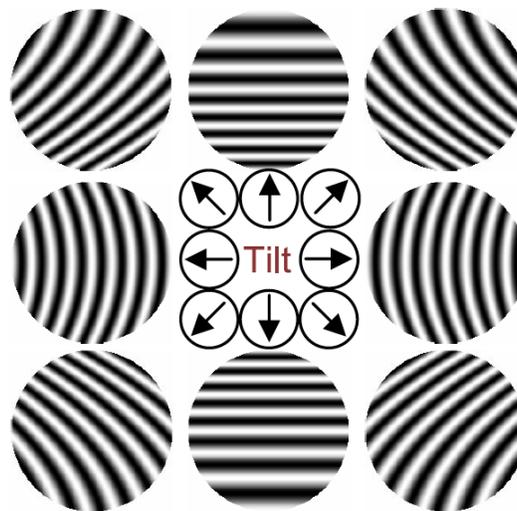




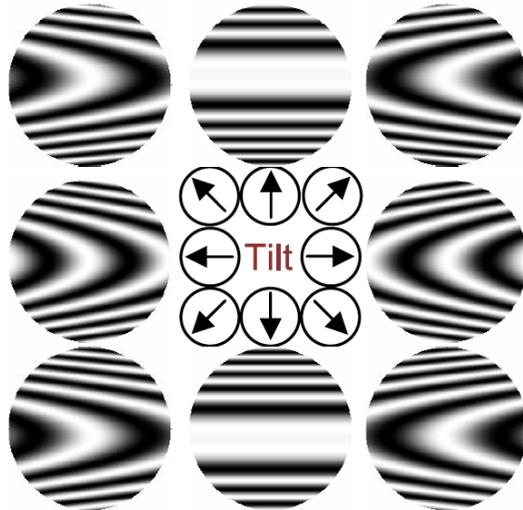
Interferograms - Spherical Aberration



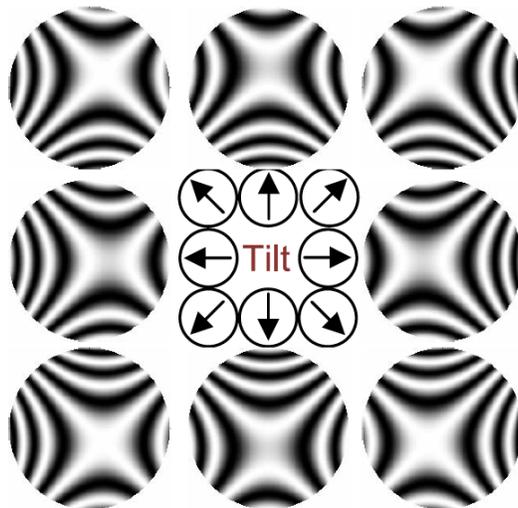
Interferograms - Small Astigmatism, Sagittal Focus



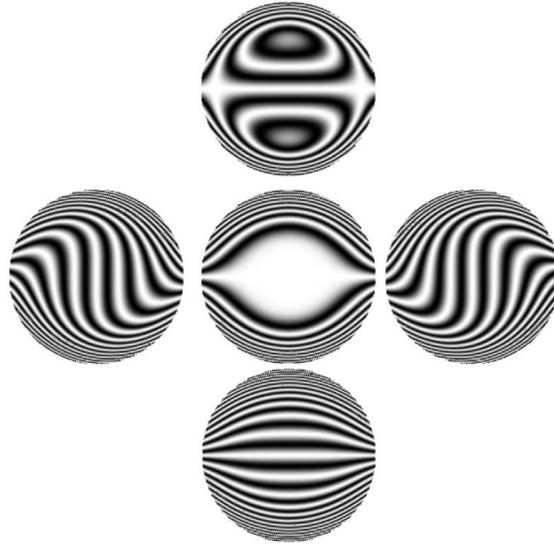
Interferograms - Large Astigmatism, Sagittal Focus



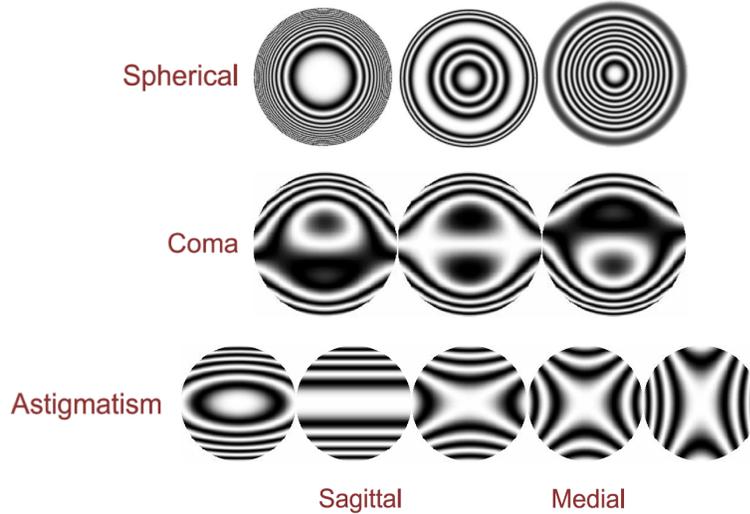
Interferograms - Large Astigmatism, Medial Focus



Interferograms - Large Coma, Varying Tilt

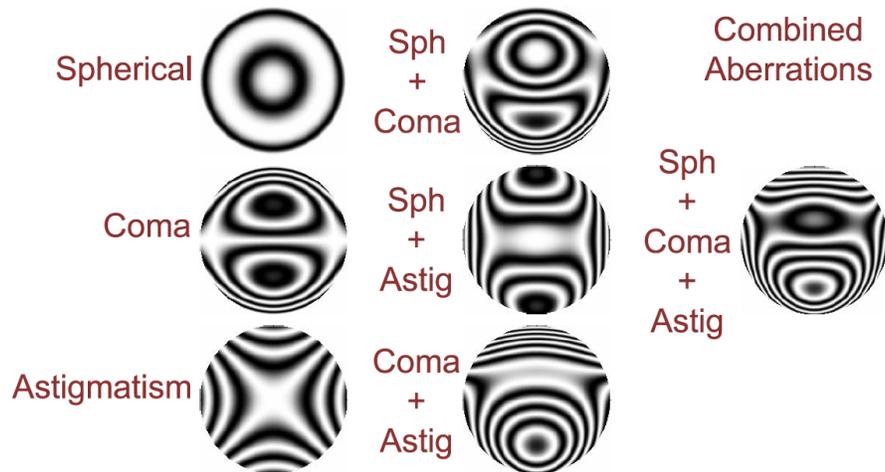


Interferograms - Changing Focus





Interferograms - Combined Aberrations



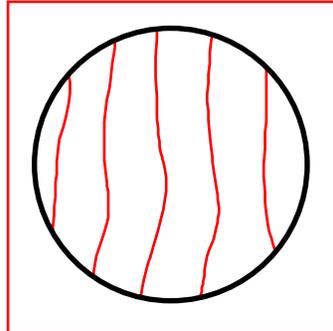
Part 2 - Phase-Shifting Interferometry

- Classical analysis of interferograms
- Basic algorithms
- Removing phase ambiguities
- Single-shot phase-measurement interferometers

Typical Interferogram



$$\text{Surface Error} = (\lambda/2) (\Delta/S)$$

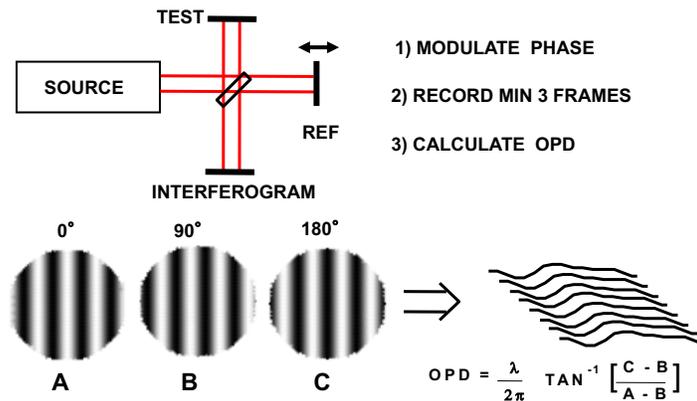


Classical Analysis

Measure positions of fringe centers.

Deviations from straightness and equal spacing gives aberration.

Phase-Shifting Interferometry

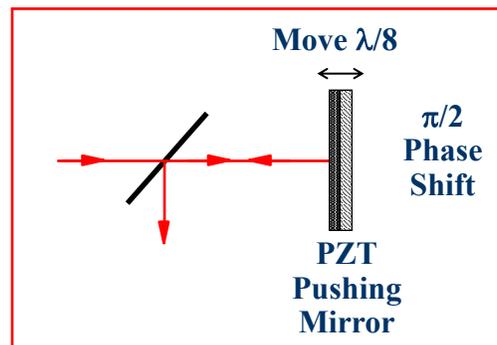


Advantages of Phase-Shifting Interferometry



- High measurement accuracy ($>1/1000$ fringe, fringe following only $1/10$ fringe)
- Rapid measurement
- Good results with low contrast fringes
- Results independent of intensity variations across pupil
- Phase obtained at fixed grid of points
- Easy to use with large solid-state detector arrays

Phase-Shifting - Moving Mirror



Phase Stepping (Shifting) Interferometry - Four-Step Method



$$I(x,y) = I_{dc} + I_{ac} \cos[\underbrace{\phi(x,y)}_{\text{measured object phase}} + \underbrace{\phi(t)}_{\text{phase shift}}]$$

$I_1(x,y) = I_{dc} + I_{ac} \cos [\phi(x,y)]$	$\phi(t) = 0 \quad (0^\circ)$
$I_2(x,y) = I_{dc} - I_{ac} \sin [\phi(x,y)]$	$= \pi/2 \quad (90^\circ)$
$I_3(x,y) = I_{dc} - I_{ac} \cos [\phi(x,y)]$	$= \pi \quad (180^\circ)$
$I_4(x,y) = I_{dc} + I_{ac} \sin [\phi(x,y)]$	$= 3\pi/2 \quad (270^\circ)$

$$\text{Tan}[\varphi(x,y)] = \frac{I_4(x,y) - I_2(x,y)}{I_1(x,y) - I_3(x,y)}$$

Relationship between Phase and Height



$$\phi(x,y) = \text{Tan}^{-1} \left[\frac{I_4(x,y) - I_2(x,y)}{I_1(x,y) - I_3(x,y)} \right]$$

$$\text{Height Error}(x,y) = \frac{\lambda}{4\pi} \phi(x,y)$$



Phase-Measurement Algorithms

Three Measurements $\phi = \text{ArcTan} \left[\frac{I_3 - I_2}{I_1 - I_2} \right]$

Four Measurements $\phi = \text{ArcTan} \left[\frac{I_4 - I_2}{I_1 - I_3} \right]$

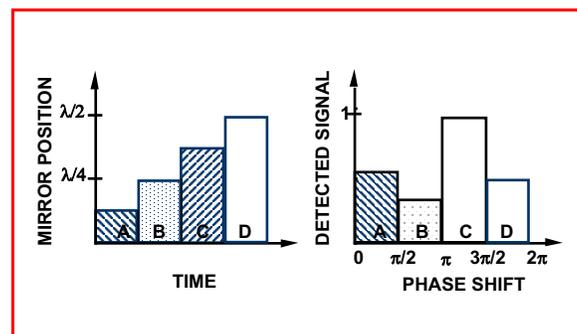
Schwider-Hariharan Five Measurements $\phi = \text{ArcTan} \left[\frac{2(I_4 - I_2)}{I_1 - 2I_3 + I_5} \right]$

Carré Equation

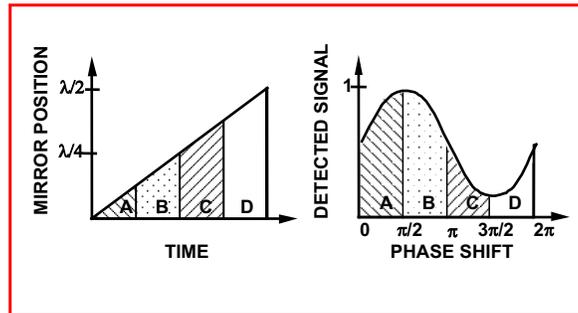
$$\phi = \text{ArcTan} \left[\frac{\sqrt{[3(I_2 - I_3) - (I_1 - I_4)][(I_2 - I_3) - (I_1 - I_4)]}}{(I_2 + I_3) - (I_1 + I_4)} \right]$$



Phase-Stepping Phase Measurement



Integrated-Bucket Phase Measurement



Integrating-Bucket and Phase-Stepping Interferometry



Measured irradiance given by

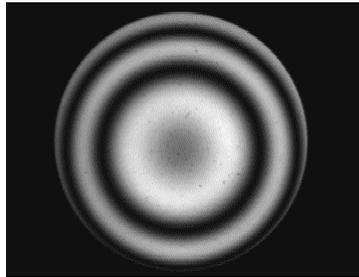
$$I_i = \frac{1}{\Delta} \int_{\alpha_i - \Delta/2}^{\alpha_i + \Delta/2} I_o \{1 + \gamma_o \text{Cos}[\phi + \alpha_i(t)]\} d\alpha(t)$$

$$= \left\{ 1 + \gamma_o \text{Sinc} \left[\frac{\Delta}{2} \right] \text{Cos}[\phi + \alpha_i] \right\}$$

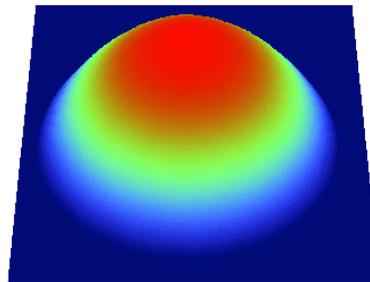
Integrating-Bucket $\Delta = \alpha$

Phase-Stepping $\Delta = 0$

Typical Fringes For Spherical Surfaces



Fringes

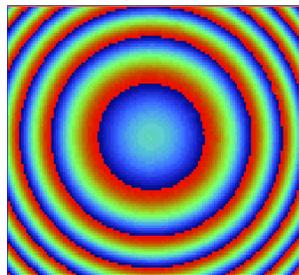


Phase map

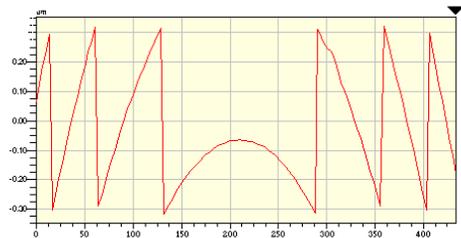
Phase Ambiguities - Before Unwrapping



2π Phase Steps



X Profile





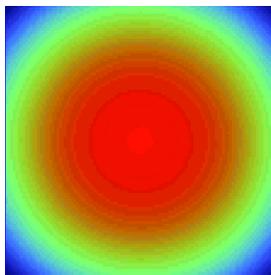
Removing Phase Ambiguities

- Arctan Mod 2π (Mod 1 wave)
- Require adjacent pixels less than π difference (1/2 wave OPD)
- Trace path
- When phase jumps by $> \pi$
Add or subtract $N2\pi$
Adjust so $< \pi$

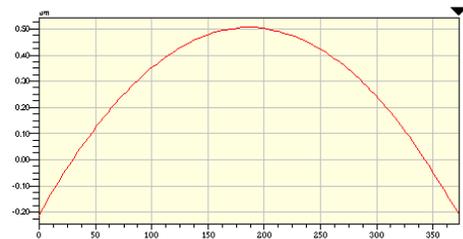


Phase Ambiguities - After Unwrapping

Phase Steps Removed



X Profile





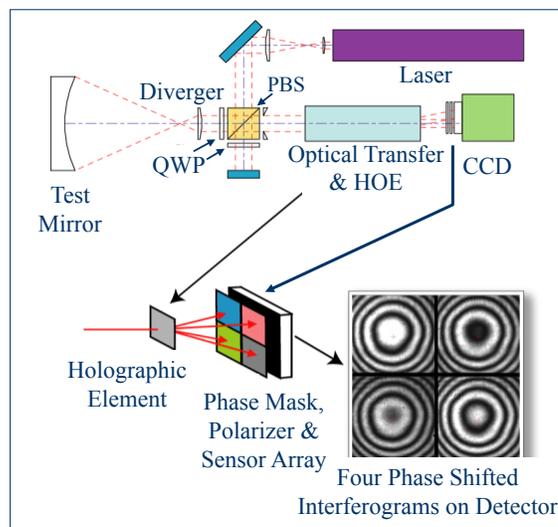
Error Due to Vibration

- Probably the most serious impediment to wider use of PSI is its sensitivity to external vibrations.
- Vibrations cause incorrect phase shifts between data frames.
- Error depends upon frequency of vibration present as well as phase of vibration relative to the phase shifting.



Single-Shot Phase-Measurement Interferometer

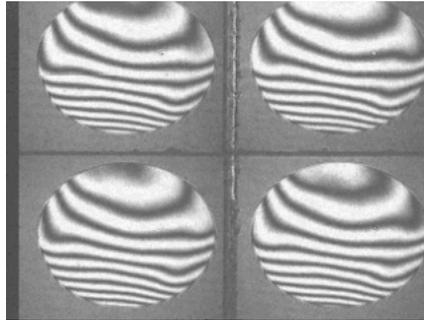
- Twyman-Green
 - Two beams have orthogonal polarization
- 4 Images formed
 - Holographic element
- Single Camera
 - 1024 x 1024
 - 2048 x 2048
- Polarization used to produce 90-deg phase shifts



Dynamic Interferometry

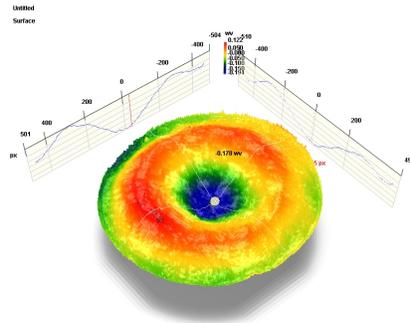
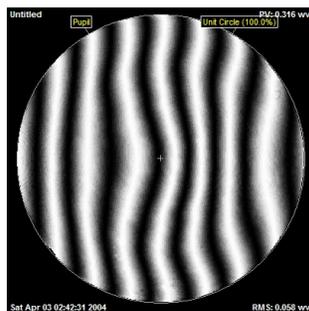


Fringes Vibrating



Phase relationship is fixed

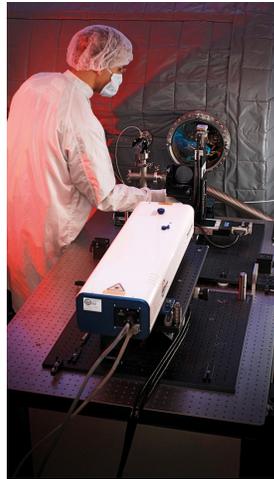
Measurement of 300 mm diameter, 2 meter ROC mirror



Mirror and interferometer on separate tables!



Testing of Large Optics



Testing in Environmental Chamber
(Courtesy Ball Aerospace)



Testing on Polishing Machine
(Courtesy OpTIC Technium)

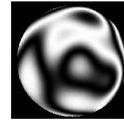
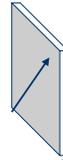
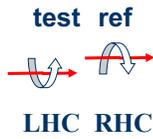


Pixelated Phase Sensor

- **Compacted pixelated array placed in front of detector**
- **Single frame acquisition**
 - High speed and high throughput
- **Achromatic**
 - Works from blue to NIR
- **True Common Path**
 - Can be used with white light



Use polarizer as phase shifter



Circ. Pol. Beams ($\Delta\phi$) + linear polarizer $\rightarrow \cos(\Delta\phi + 2\alpha)$

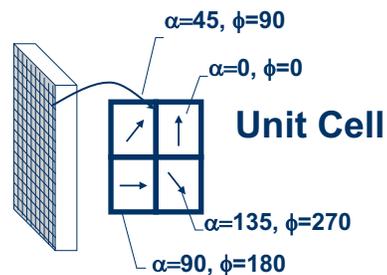
Phase-shift depends on polarizer angle

Reference: S. Suja Helen, M.P. Kothiyal, and R.S. Sirohi,
"Achromatic phase-shifting by a rotating polarizer", Opt.
Comm. 154, 249 (1998).



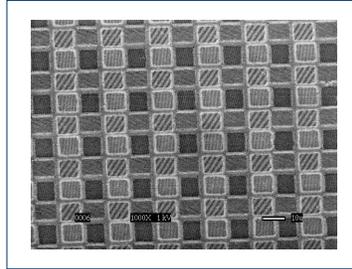
Array of Oriented Micropolarizers

Polarizer array
Matched to detector
array pixels





SEM of Patterned Polarizers



10 micron elements

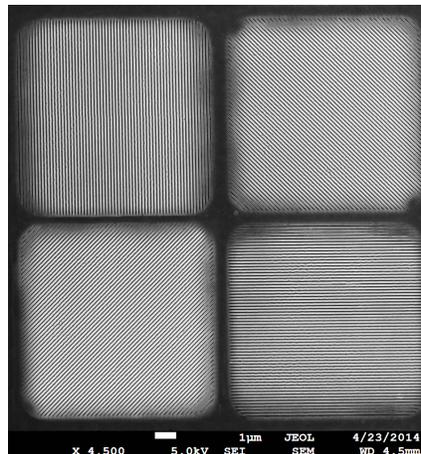
Photolithography used to pattern polarizers

- Ultra-thin (0.1 - 0.2 microns)
- Wide acceptance angle (0 to 50 degrees)
- Wide chromatic range (UV to IR)

Array bonded directly to CCD



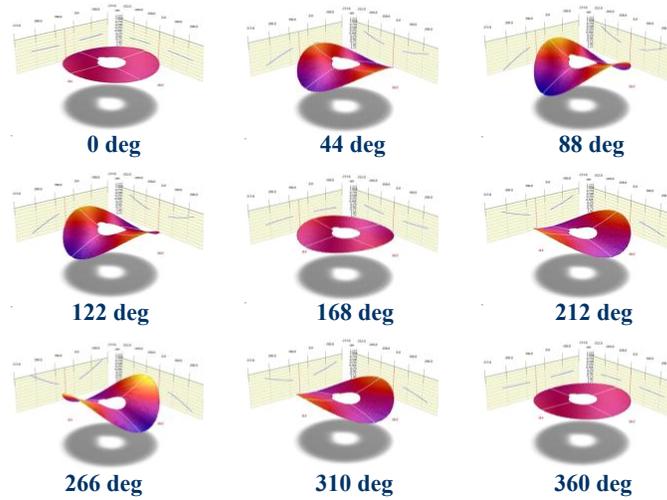
Electron micrograph of wire grid polarizers



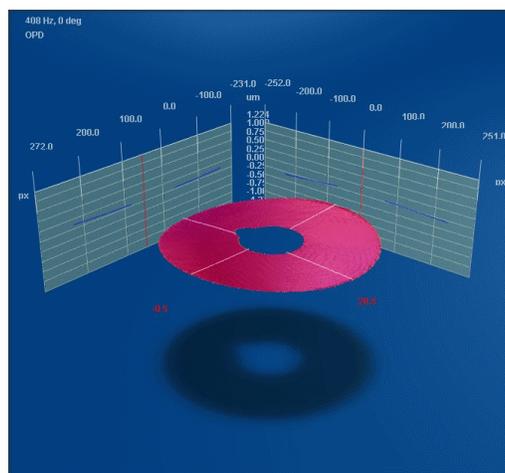
← 20 μm →



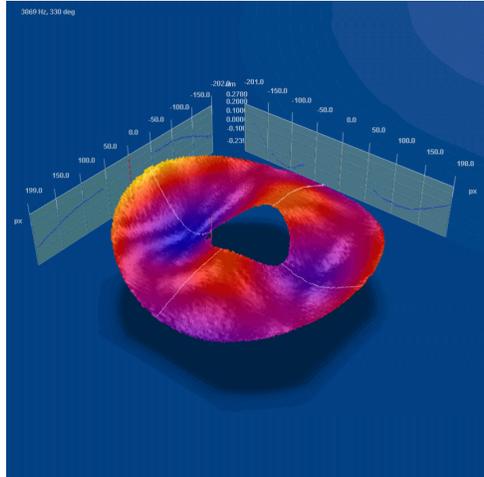
Phase Sweep at 408 Hz



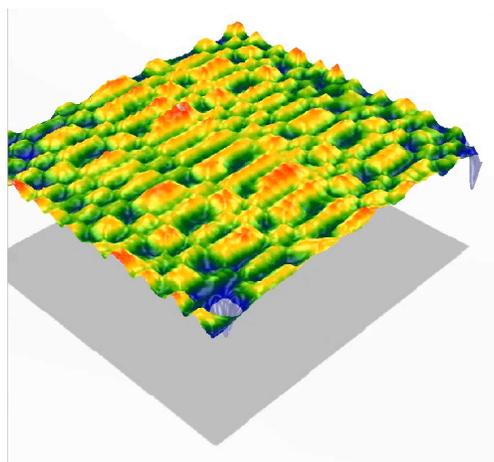
AI Mirror, 408 Hz



AI Mirror, 3069 Hz, Higher Order Mode



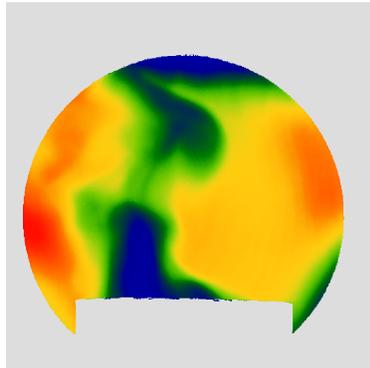
32 x 32 Element Deformable Mirror



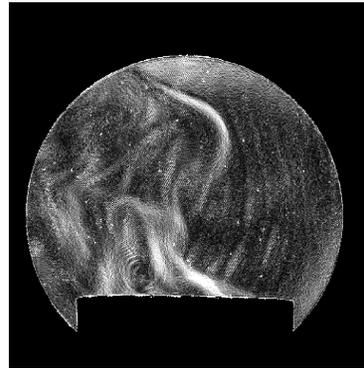
Heat Waves from Hot Coffee



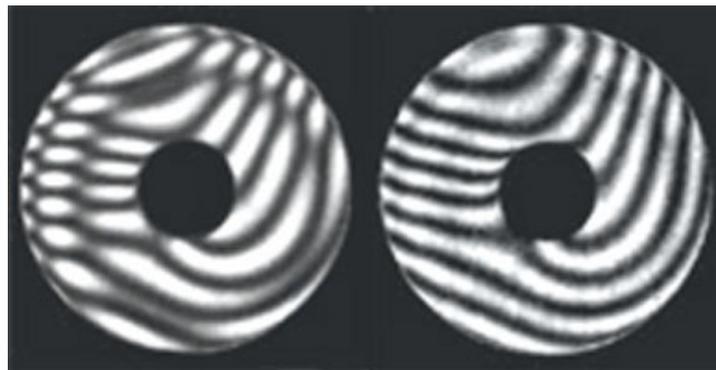
OPD



Slope



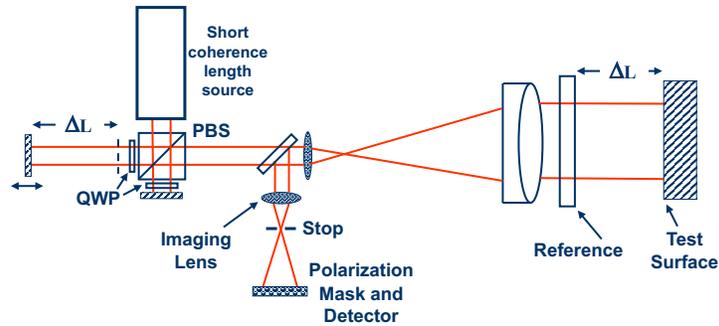
Interference Fringes Obtain Testing a Thin Glass Plate



a) Long coherence
length source

b) Short coherence
length source

Simultaneous Phase-Shifting Fizeau – Short Coherence Length Source

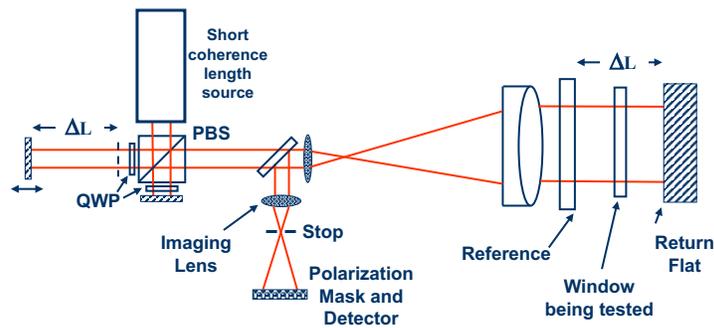


Interference pattern resulting from long path length source beam reflected off reference and short path length source beam reflected off test surface.

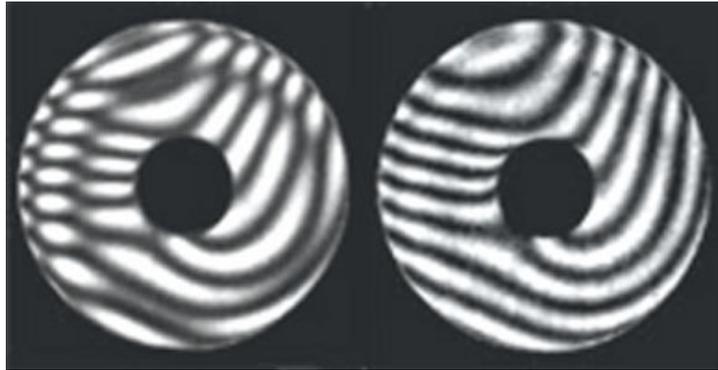
Test and reference beams have orthogonal polarization.

Fewer spurious fringes.

Testing Glass Sample - Short Coherence Length Source



Interference Fringes Obtain Testing a Thin Glass Plate



Long coherence length source Short coherence length source

Conclusions – Single Shot Interferometer



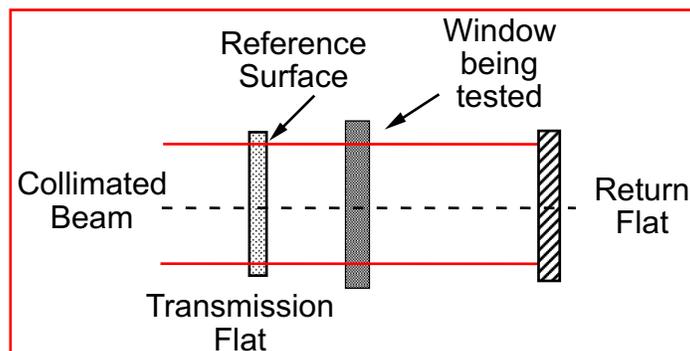
- **Vibration insensitive, quantitative interferometer**
- **Surface figure measurement (nm resolution)**
- **Snap shot of surface height**
- **Acquisition of “phase movies”**

Part 3 - Specialized Optical Tests



- Testing windows, prisms, and corner cubes
- Measuring radius of curvature
- Measuring index inhomogeneity
- Testing cylindrical surfaces

Testing Windows in Transmission

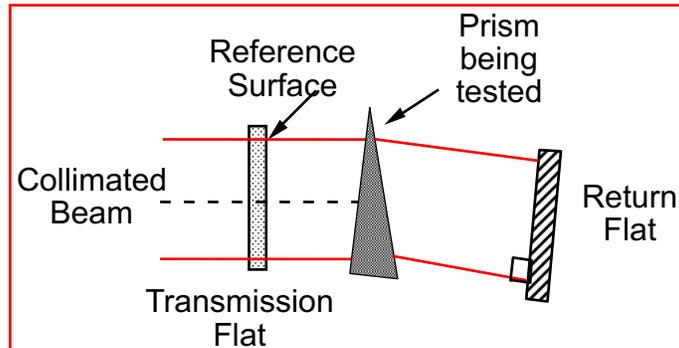


δt = window thickness variations

OPD measured = $2(n-1)\delta t$



Testing Prisms in Transmission

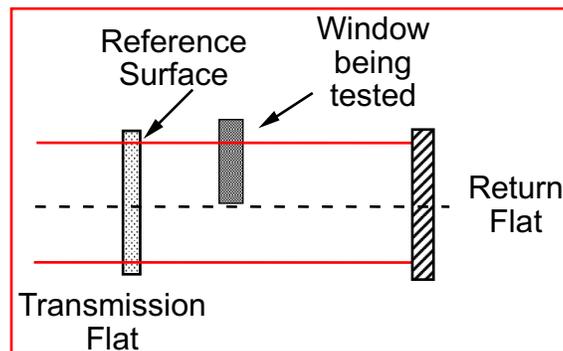


δt = error in prism thickness

$$\text{OPD measured} = 2(n-1)\delta t$$



Measuring Window Wedge

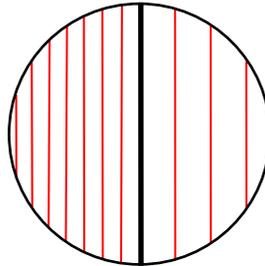


Tilt difference between two interferograms gives window wedge.

Calculating Window Wedge



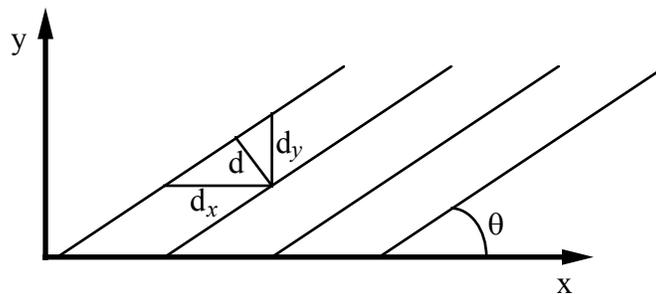
Tilt difference between two interferograms gives window wedge.



$\alpha = \text{window wedge}$

$$\alpha = \frac{\text{tilt difference}}{2(n-1)}$$

Calculation of Tilt

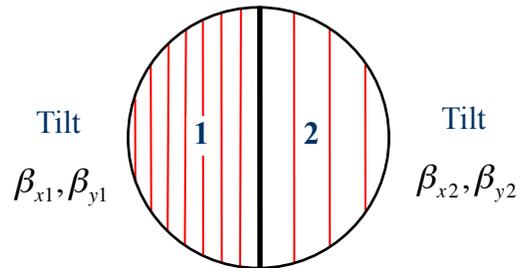


$$d = \text{fringe spacing} \quad d_x = d / \sin(\theta) \quad d_y = d / \cos(\theta)$$

$$\beta = \text{Tilt} = \frac{\lambda}{d} \quad \beta_x = \frac{\lambda}{d_x} \quad \beta_y = \frac{\lambda}{d_y}$$



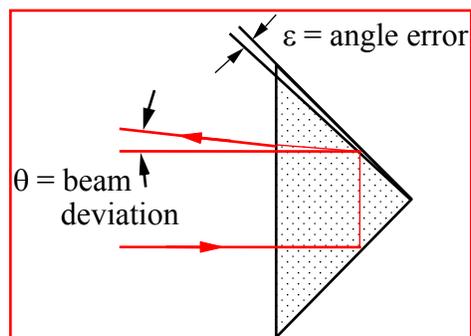
Calculation of Tilt Difference



$$\text{Tilt Difference} = \sqrt{(\beta_{x1} - \beta_{x2})^2 + (\beta_{y1} - \beta_{y2})^2}$$



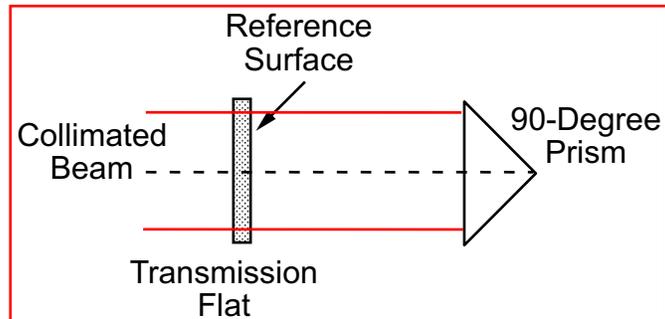
Angle Accuracy of 90-Degree Prisms



$$\epsilon = \frac{\theta}{2n}$$



Testing 90-Degree Prisms (Single Pass)



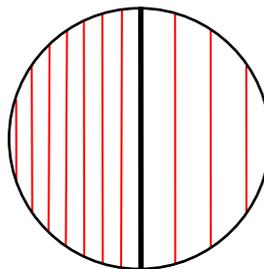
Tilt difference between two interferograms gives error in 90-degree angle.

Errors in collimated beam do not cancel.



Calculating Error in 90-Degree Prism (Single Pass)

Tilt difference between two interferograms gives prism angle error.

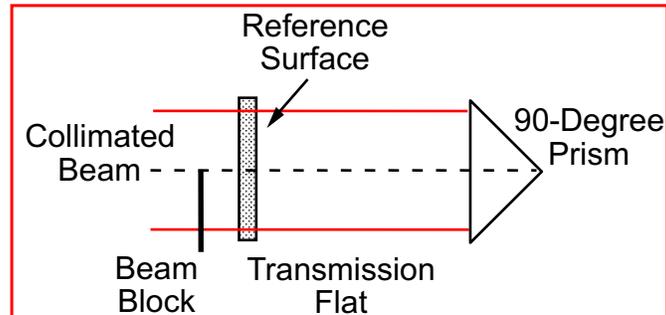


$\epsilon =$ prism angle error

$$\epsilon = \frac{\text{tilt difference}}{4n}$$



Testing 90-Degree Prisms (Double Pass)

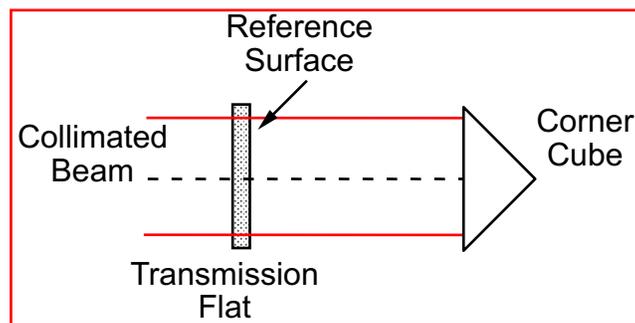


$$\varepsilon = \frac{x \text{ tilt in interferogram}}{4n} \quad \varepsilon = \text{prism angle error}$$

Errors in collimated beam cancel.



Testing Corner Cubes (Single Pass)



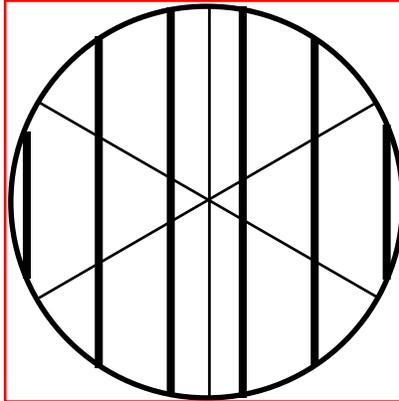
Errors in collimated beam do not cancel.

Interferogram for Perfect - Corner Cube (Single Pass)



6 interferograms obtained.

Straight fringes obtained for perfect corner cube.



Analyzing Corner Cube Interferograms (Single Pass)

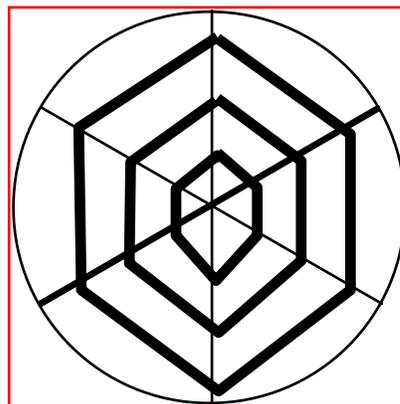


6 interferograms obtained.

Tilt difference between any 2 interferograms gives one angle error in corner cube.

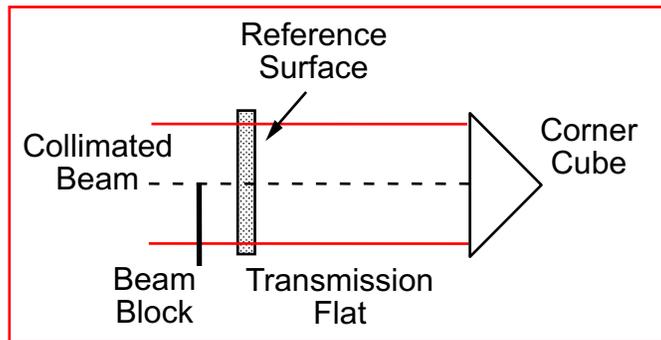
n is refractive index of corner cube.

$$\text{Error} = \text{Tilt difference} / (3.266 n)$$





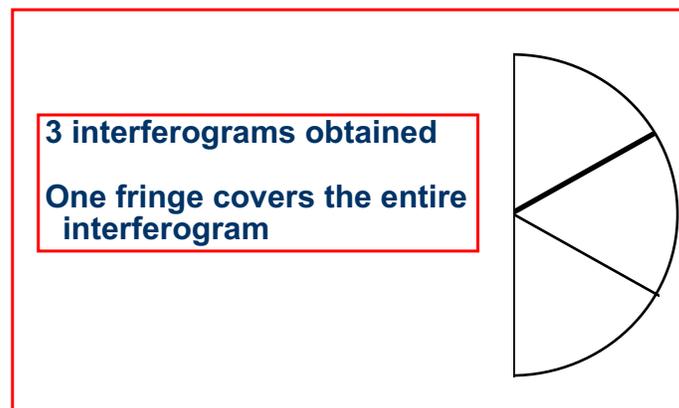
Testing Corner Cubes (Double Pass)



Errors in collimated beam cancel.



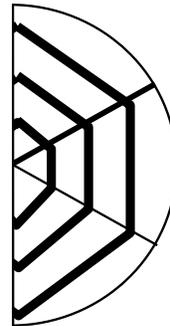
Interferogram for Perfect Corner Cube (Double Pass)



Analyzing Corner Cube Interferograms (Double Pass)

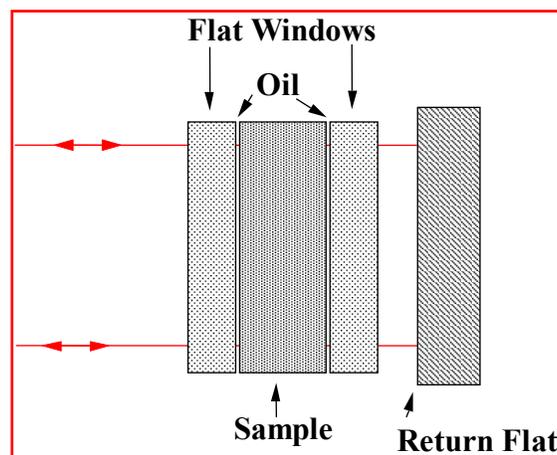


3 interferograms obtained.
Tilt of each interferogram gives one angle error in corner cube.
 n is refractive index of corner cube.

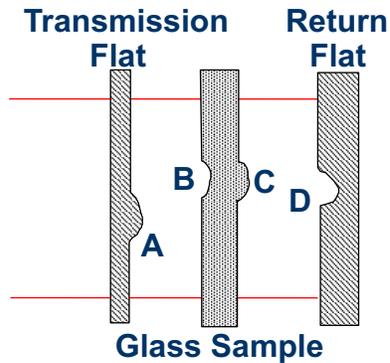


$$\text{Error} = \text{Tilt}/(3.266 n)$$

Measuring Index Inhomogeneity (Classical Technique)



Measuring Index Inhomogeneity Without Oil-On Plates



4 Measurements Required

Surface Errors in Test Optics and Glass Sample Cancel.

Measuring Index Inhomogeneity



1. Measure light reflected from front surface of sample.

$$OPD_1 = 2(B-A)$$

2. Measure light through sample and reflected off second surface.

$$OPD_2 = 2(B-A) + 2n_o(C-B) + 2\delta$$

3. Measure through sample and reflected off return mirror.

$$OPD_3 = 2(B-A) + 2n_o(C-B) + 2(D-C) + 2\delta$$

4. Remove sample and measure cavity.

$$OPD_4 = 2(D-A)$$

$$\begin{aligned}\delta &= [n_o(OPD_3 - OPD_4) - (n_o - 1)(OPD_2 - OPD_1)] / 2 \\ &= (n - n_o)T\end{aligned}$$

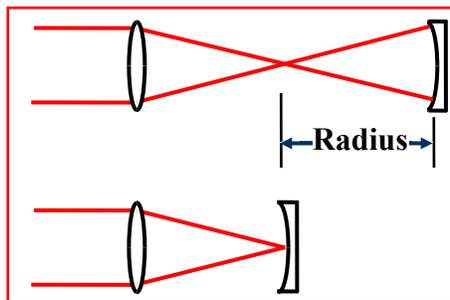
Index Inhomogeneity Test Results



RMS: 0.168 wv P-V: 0.711 wv wv: 632.8nm



Measuring Radius of Curvature



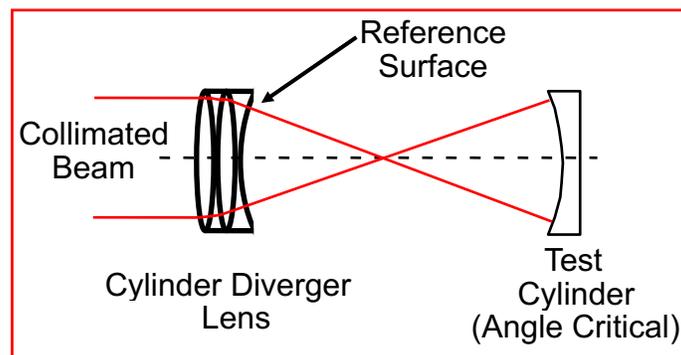
Two positions which give null fringe for spherical mirror.

Cylindrical Surface Test



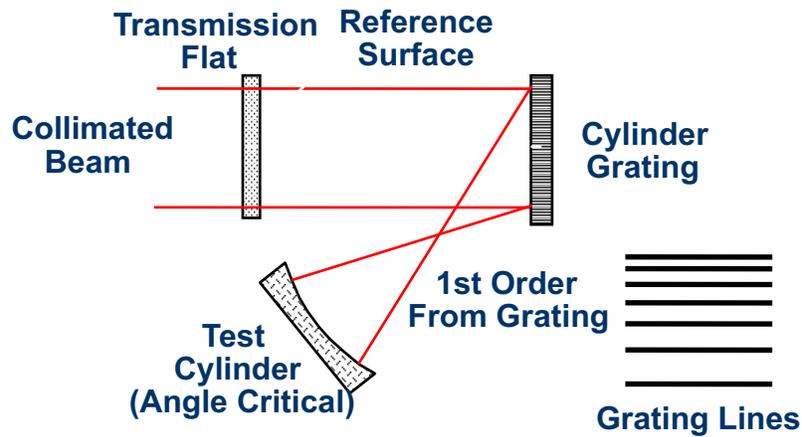
- Need cylindrical wavefront
 - Reference grating: Off-axis cylinder
 - Cylinder null lens: Hard to make
- Direct measurement - No modifications to interferometer
- Concave and convex surfaces
- Quantitative - phase measurement

Cylinder Null Lens Test Setup





Cylinder Grating Test Setup



Part 4 - Long Wavelength Interferometry

- Wavelengths of primary interest
- Test infrared transmitting optics
- Test optically rough surfaces

Wavelengths of Primary Interest



- **1.06 microns**
Reduced sensitivity
- **10.6 microns**
Reduced sensitivity
Test infrared transmitting optics
Testing optically rough surfaces

1.06 Micron Source Interferometer



- **Diode Pumped Yag Laser**
Excellent coherence properties
- **Normal Optics**
- **Normal CCD Camera**

Conventional interferometry techniques work well.

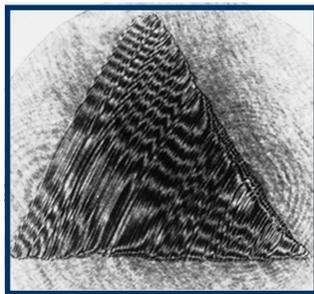
10.6 Micron Source Interferometer



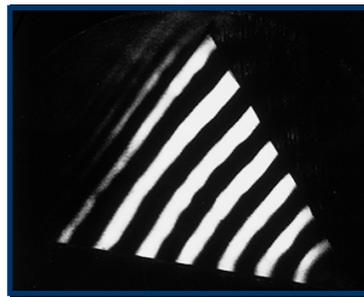
- Carbon Dioxide Laser
Excellent coherence properties
- Zinc Selenide or Germanium Optics
- Bolometer

Conventional interferometry techniques work well.

Reduced Sensitivity Testing



0.633 microns wavelength



10.6 microns wavelength

Testing Rough Surfaces



Assume surface height distribution is Gaussian with standard deviation σ .

The normal probability distribution for the height, h , is

$$p(h) = \frac{1}{(2\pi)^{1/2} \sigma} \exp\left(-\frac{h^2}{2\sigma^2}\right)$$

Fringe Contrast Reduction due to Surface Roughness

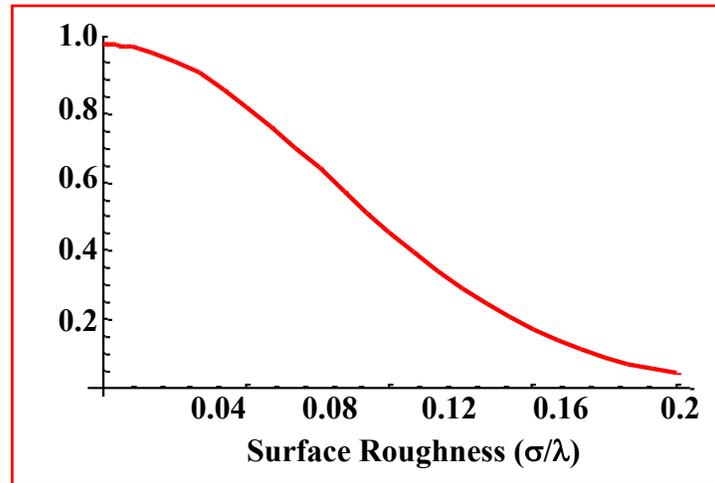


The fringe contrast reduction due to surface roughness is

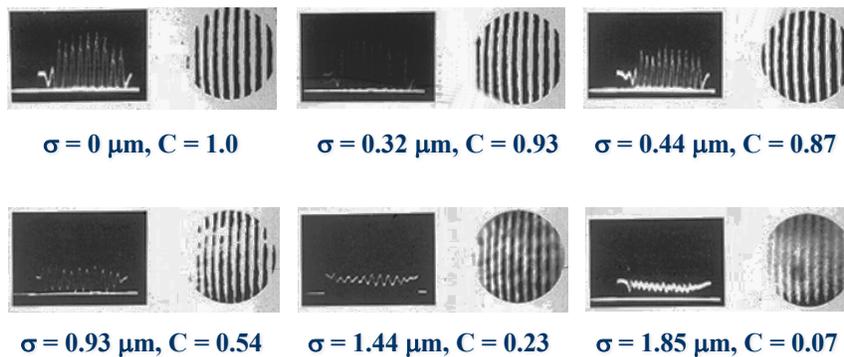
$$C = \exp\left(-8\pi^2 \frac{\sigma^2}{\lambda^2}\right)$$

Reference: Appl. Opt. 11, 1862 (1980).

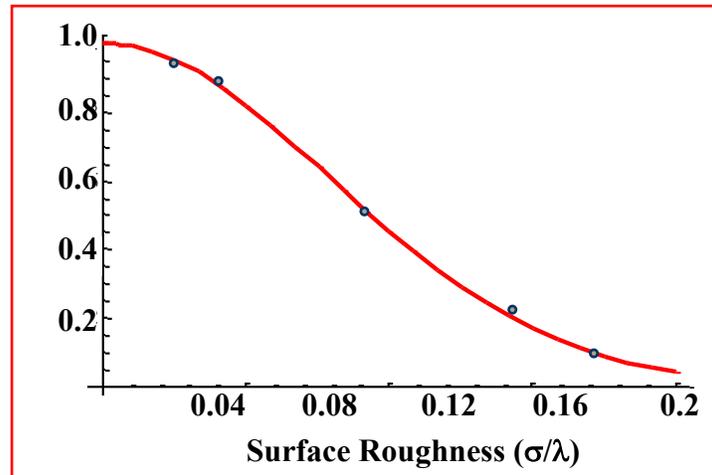
Fringe Contrast versus Surface Roughness - Theory



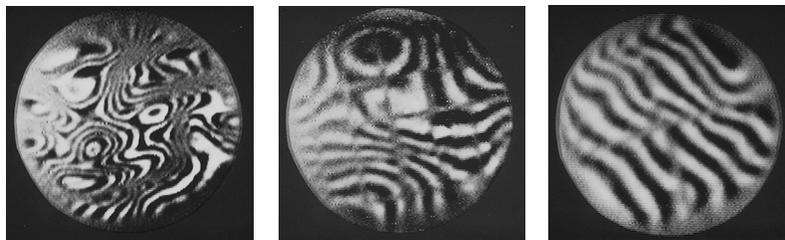
Interferograms Obtained for Different Roughness Surfaces



Fringe Contrast versus Surface Roughness - Theory and Experiment



Infrared Interferograms of Off-Axis Parabolic Mirror in Chronological Order



10.6 Micron Wavelength Interferometer



Part 5 - Testing of Aspheric Surfaces



- Description of aspheric surfaces
- Techniques for testing aspheric surfaces
- Requirements for use of optical analysis software in optical testing
- Limitations of current aspheric testing techniques

Aspheric Surfaces



Aspheric surfaces are of much interest because they can provide

- **Improved performance**
- **Reduced number of optical components**
- **Reduced weight**
- **Lower cost**

Conics



A conic is a surface of revolution defined by means of the equation

$$s^2 - 2rz + (k + 1)z^2 = 0$$

Z axis is the axis of revolution. k is called conic constant. r is the vertex curvature.

$$s^2 = x^2 + y^2$$

Sag for Conic



$$z = \frac{s^2 / r}{1 + [1 - (k + 1)(s / r)^2]^{1/2}}$$

$$s^2 = x^2 + y^2$$

Sag for Asphere



$$z = \frac{s^2 / r}{1 + [1 - (k + 1)(s / r)^2]^{1/2}} + A_4 s^4 + A_6 s^6 + \dots$$

$$s^2 = x^2 + y^2$$

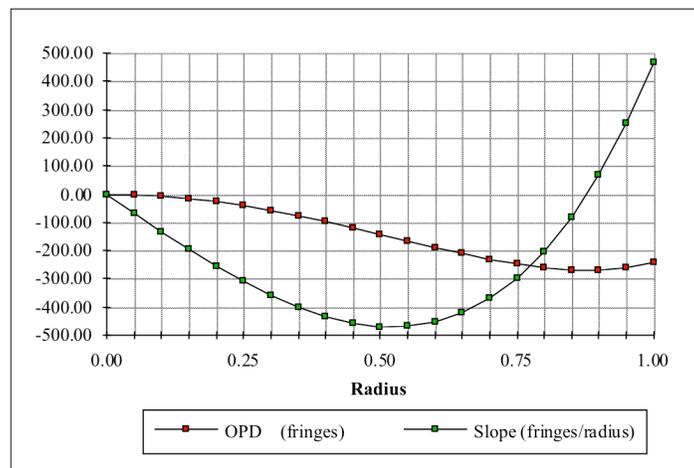
k is the conic constant
r is the vertex radius of curvature
A's are aspheric coefficients

Difficulty of Aspheric Test



Slope of aspheric departure determines difficulty of test

Wavefront Departure and Slope versus Radius



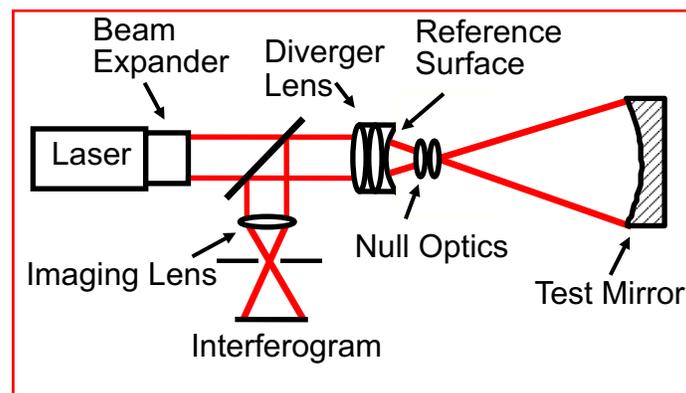


Aspheric Testing Techniques

- **Null Tests - Perfect optics give straight equally spaced fringes**
 - Conventional null optics
 - Computer generated holograms
- **Non-null Tests - Even perfect optics do not give straight equally spaced fringes**
 - Deflectometry (SCOTS)
 - Shack-Hartmann
 - Lateral shear interferometry
 - Radial shear interferometry
 - High-density detector arrays
 - Sub-Nyquist interferometry
 - Long-wavelength interferometry
 - Two-wavelength holography
 - Two-wavelength interferometry
 - Tilted wave interferometry
 - Stitching interferograms
 - Scanning interferometry



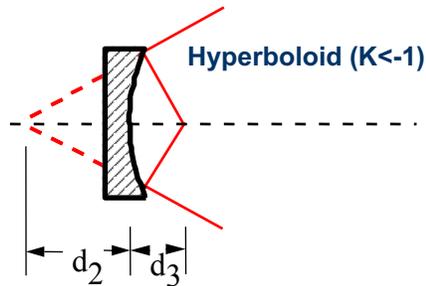
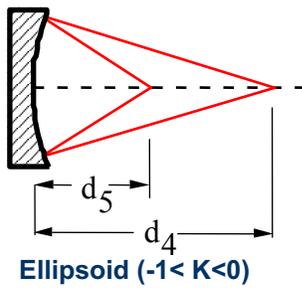
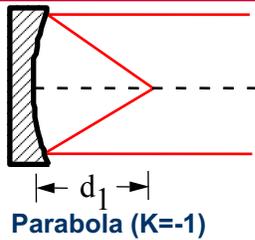
Conventional Null Optics



Hubble Pictures (Before and After the Fix)



Null Tests for Conics



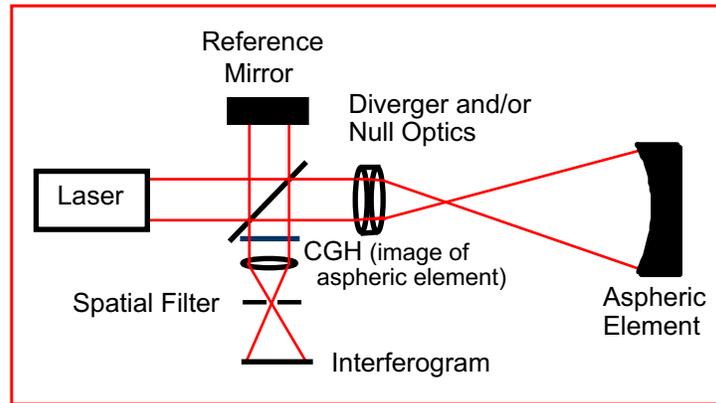
$$d_1 = r/2$$

$$d_2, d_3 = \frac{r}{K+1} (\sqrt{-K} \pm 1)$$

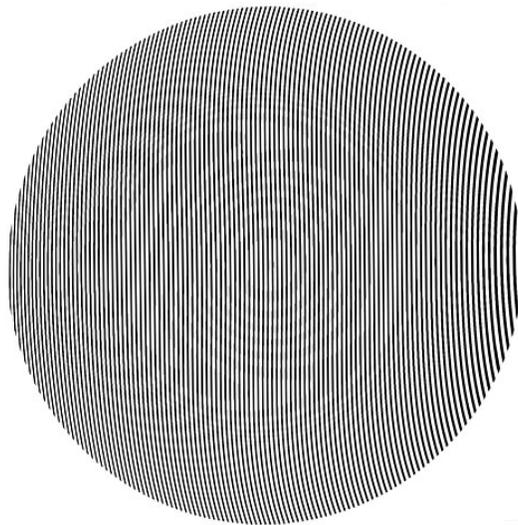
$$d_4, d_5 = \frac{r}{K+1} (1 \pm \sqrt{-K})$$



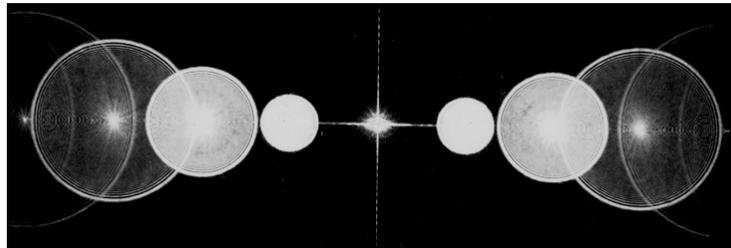
CGH Interferometer



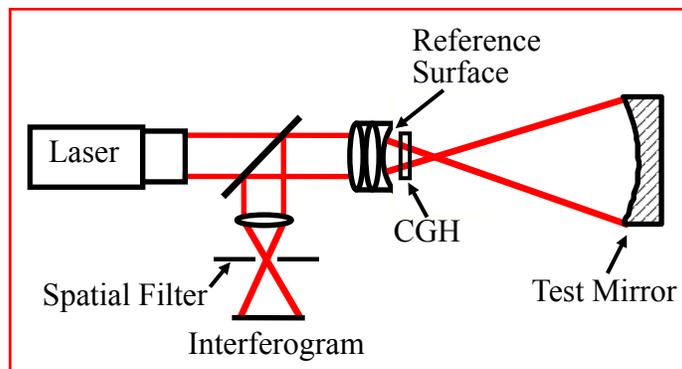
Computer Generated Hologram



Light in Spatial Filter Plane



CGH Used as Null Lens



- Can use existing commercial interferometer
- Double pass through CGH, must be phase etched for testing bare glass optics
- Requires highly accurate substrate

Error Source



- Pattern distortion (Plotter errors)
- Substrate surface figure
- Alignment Errors

Pattern Distortion



- The hologram used at m^{th} order adds m waves per line;
- CGH pattern distortions produce wavefront phase error:

$$\Delta W(x, y) = -m\lambda \frac{\varepsilon(x, y)}{S(x, y)}$$

$\varepsilon(x, y)$ = grating position error in direction perpendicular to the fringes;

$S(x, y)$ = localized fringe spacing;

For $m = 1$, phase error in waves = distortion/spacing

0.1 μm distortion / 20 μm spacing $\rightarrow \lambda/200$ wavefront

Plotters



- **E-beam**
 - Critical dimension – 1 micron
 - Position accuracy – 50 nm
 - Max dimensions – 150 mm
- **Laser scanner**
 - Similar specs for circular holograms

Solving Substrate Distortion Problems



- **Use direct laser writing onto custom substrates**
- **Use amplitude holograms, measure and back out substrate**
- **Use an optical test setup where reference and test beams go through substrate**

Alignment Errors

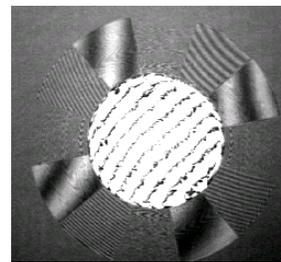
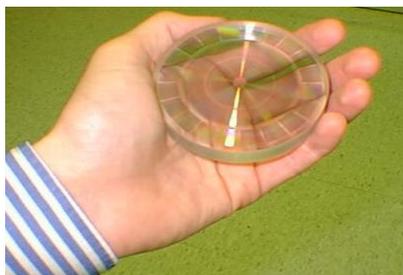


- Lateral misalignment gives errors proportional to slope of wavefront
- Errors due to longitudinal misalignment less sensitive if hologram placed in collimated light
- Alignment marks (crosshairs) often placed on CGH to aid in alignment
- Additional holographic structures can be placed on CGH to aid in alignment of CGH and optical system under test

Use of CGH for Alignment



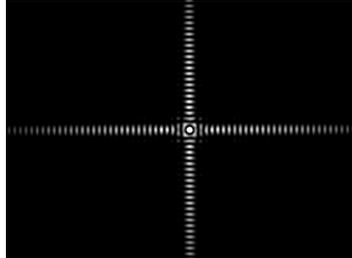
Commonly CGH's have patterns that are used for aligning the CGH to the incident wavefront.



Using multiple patterns outside the clear aperture, many degrees of freedom can be constrained using the CGH reference.



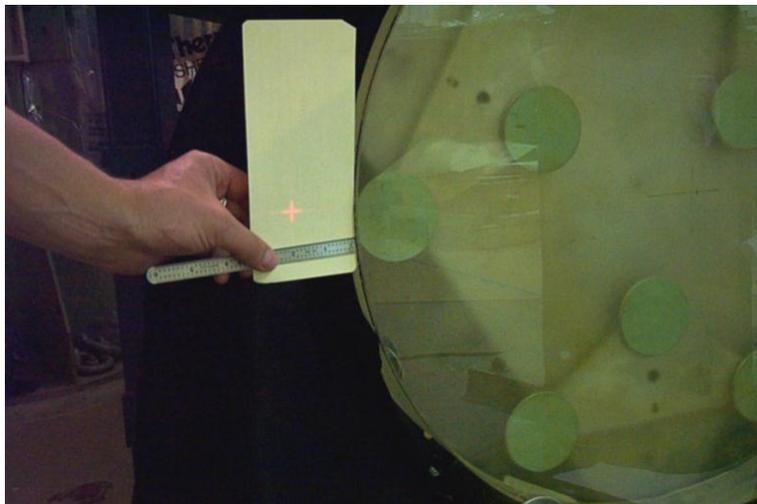
Projection of Fiducial Marks



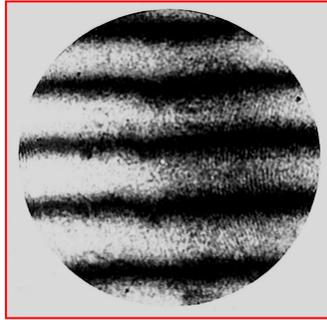
- The positions of the crosshairs can be controlled to micron accuracy
- The patterns are well defined and can be found using a CCD
- Measured pattern at 15 meters from CGH. Central lobe is only 100 μm FWHM



CGH Alignment for Testing Off-Axis Parabola



Holographic test of refractive element having 50 waves of third and fifth order spherical aberration



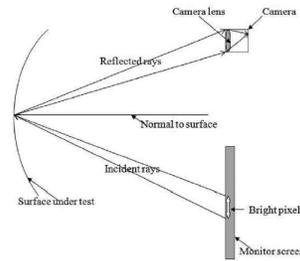
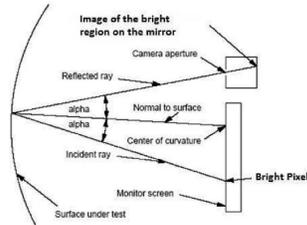
Deflectometry (SCOTS Test)



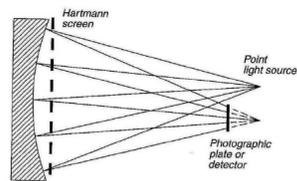
- Hartmann test in reverse
 - Measures slope
 - Accuracies in the range of 100 – 200 nrad (rms) have been achieved
- Ref: Su, Parks, Wang, Angel, and Burge, “Software configurable optical test system: a computerized reverse Hartmann test”, *Appl. Opt.*, 49(23), 4404-4412, (2010).
 - Ref: Su, Wang, Burge, Kaznatcheev, and Idir, “Non-null full field X-ray mirror metrology using SCOTS: a reflection deflectometry approach”, *Opt. Express* 20(11), 12393-12406 (2012).
 - Ref: Häusler, Faber, Olesch, and Ettl, “Deflectometry vs. Interferometry”, *Proc. SPIE. 8788, Optical Measurement Systems for Industrial Inspection VIII 87881C* (May 13, 2013) doi: 10.1117/12.2020578.



Deflectometry and Hartmann Test



Geometry of Deflectometry

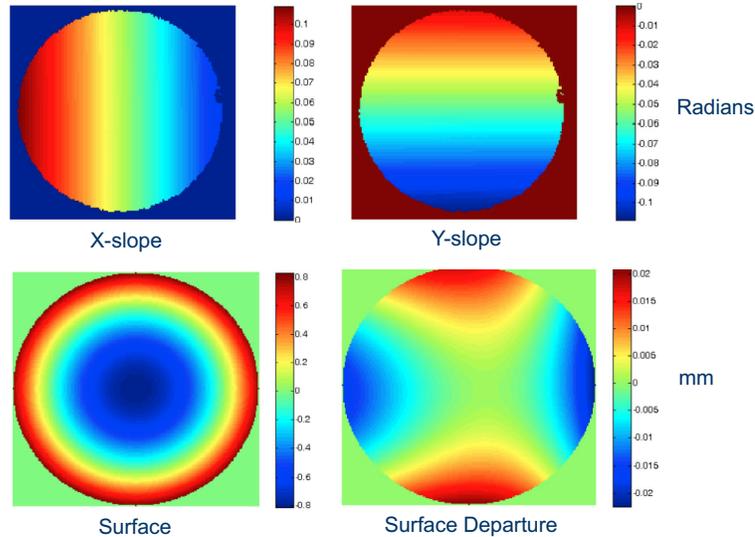


Hartmann Test

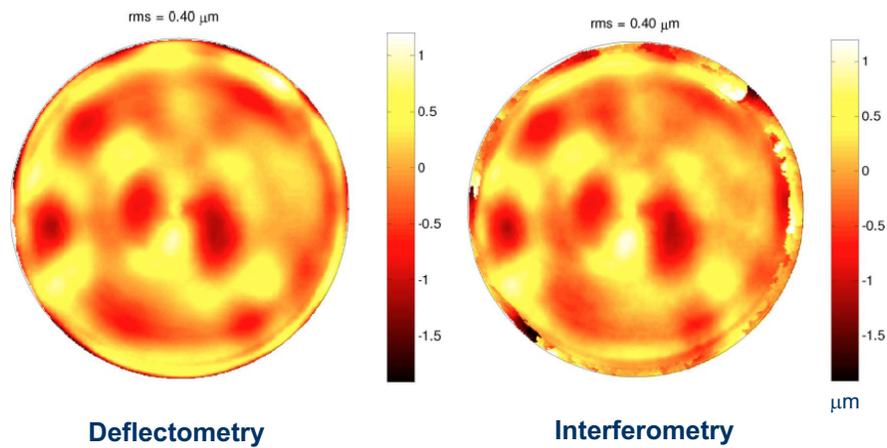
Use line source to measure either x-slope or y-slope. Sinusoidal fringes can be used instead of line and phase-shifting techniques can be used.



Measurement of Off-Axis Parabola



8.4 m Giant Magellan Telescope



Stitching Interferograms

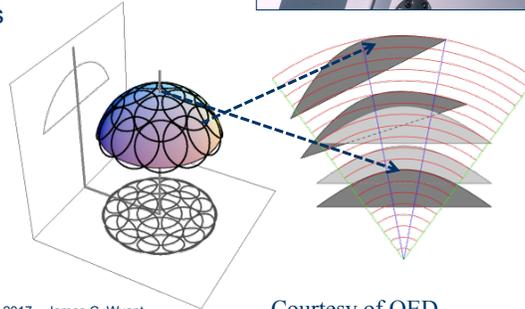
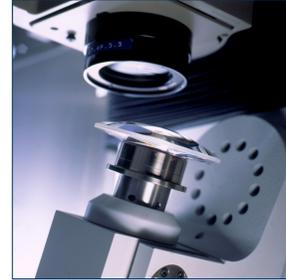


- Perform sub-aperture test of aspheric and stitch together interferograms.
- Trade-off between overlap between interferograms and number of interferograms required.
- Much easier to describe than to obtain accurate results.

Subaperture Stitching Interferometry (SSI®)



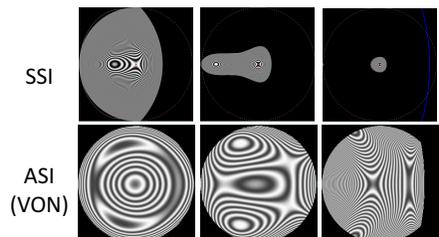
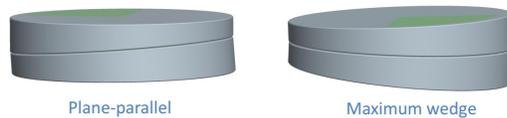
- What is it?
 - 6-axis motion system
 - “Standard” interferometer
 - Automatic collection of multiple subaperture measurements
 - **Magnified, locally nulled** sub-apertures **reduce “aspheric” fringe density**
 - Compensation of systematic errors
- SSI extends standard interferometry
 - **Fast & Large** parts
 - Aspheres (up to $\sim 200 \lambda$)
- And also can *improve*:
 - **Accuracy & Resolution**



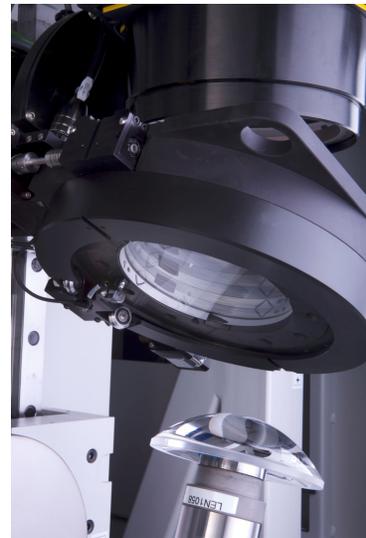
Extending the SSI to ASI®



- Variable Optical Null (VON) extends aspheric departure capture range
- Counter-rotating optical wedges
 - Varying the wedge angle and tilt produces astigmatism & coma



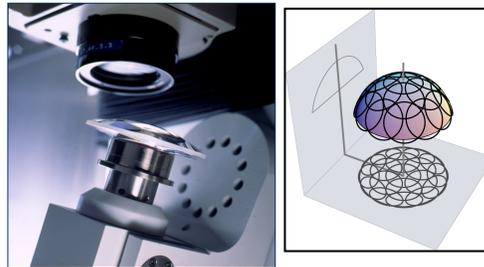
650 μm
departure
asphere



SSI/ASI: Summary

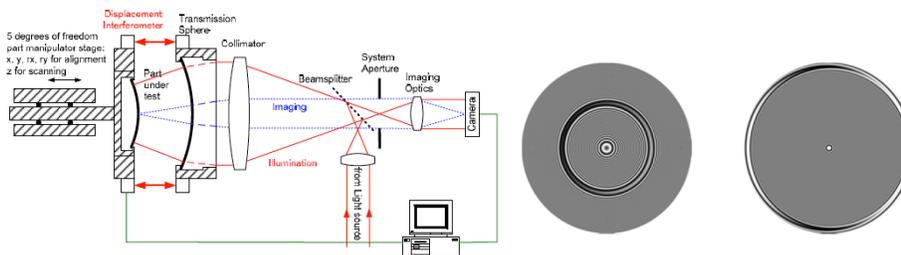


- What is it good for?
 - Flexible – no dedicated nulls
 - High departure
 - Large NA or CA
 - High vertical resolution
 - High lateral resolution
 - Compensation of systematic errors
- What are its key limitations?
 - Inflection points
 - High slope deviations
 - 3rd order spherical uncertainty



Capability Summary	
Size	👍
Shape	👎 👍
Lat Res	👍 👍
Vert Res	👍 👍

Zygo Verifire Multi-Zone Aspheric Tester



- Measure 6 to 200 sub-measurements of concentric zones.
- Measure distance of every zone from from center point of spherical reference surface.
- Measure distance to apex of part.
- Stitching of overlapping apertures not required.
- The results represents surface-deviation in normal direction.

Reference: M. F. Kuechel, "Interferometric measurement of rotationally symmetric aspheric surfaces," in "Proc. SPIE 7389, Optical Measurement Systems for Industrial Inspection VI, 738916," (2009).

Verifire Asphere Spec (from Zygo brochure)



Aspheric Shape ⁽⁷⁾	Axially symmetric concave or convex shape with specular surface and a measurable apex
Departure from asphere design	Up to 10 μm
Departure from vertex sphere R0	Approximately 800 μm
Part Diameter ⁽⁸⁾	1 mm to 130 mm
Simple Repeatability ^(2,3)	$\leq 1 \text{ nm } (\lambda/600) \text{ RMS}$
Surface Measurement Repeatability ^(2,4)	$\leq 5 \text{ nm } (\lambda/125) \text{ RMS}$
Height Resolution	0.08 nm
Cycle Time ⁽⁵⁾	2 - 8 minutes (typical)

Lens Analysis Software



- **Must know precisely how optics in test setup change aspheric wavefront.**
- **Must know effects of misalignments, so errors due to misalignments can be removed.**

Basic Limitations of Aspheric Testing



- **Must get light back into the interferometer**
- **Must be able to resolve the fringes**
- **Must know precisely the optical test setup**

This is the most serious problem

Part 6 - Measurement of Surface Microstructure



- **Non-Contact Optical Profilers**
- **White Light Interferometry**
- **Vertical Scanning Optical Profilers**

Non-Contact Optical Profilers for Measurement of Surface Microstructure



- Non-contact measurement
- 2D or 3D surface topography
- Visual qualitative surface inspection
- Vertical resolution suitable for super-polished optics
- Fast measurement and analysis

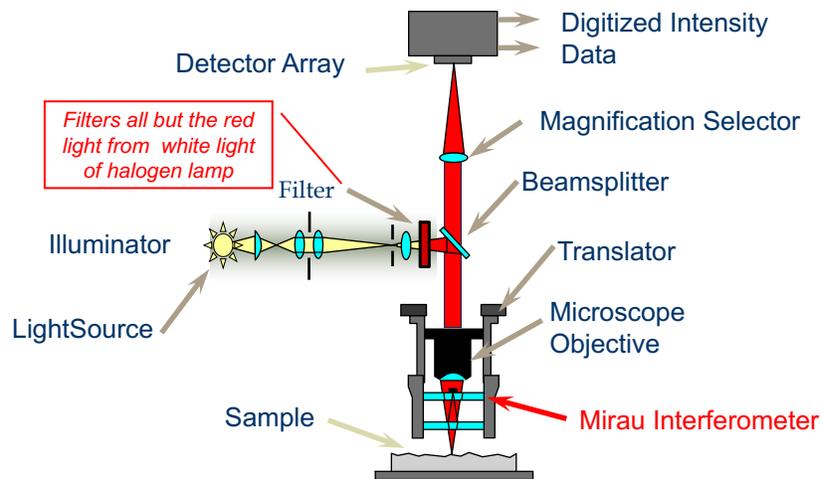
Advantages of White Light over Laser Light



- Lower noise
 - No spurious fringes
- Multiple wavelength operation
 - Measure large steps
- Focus easy to determine

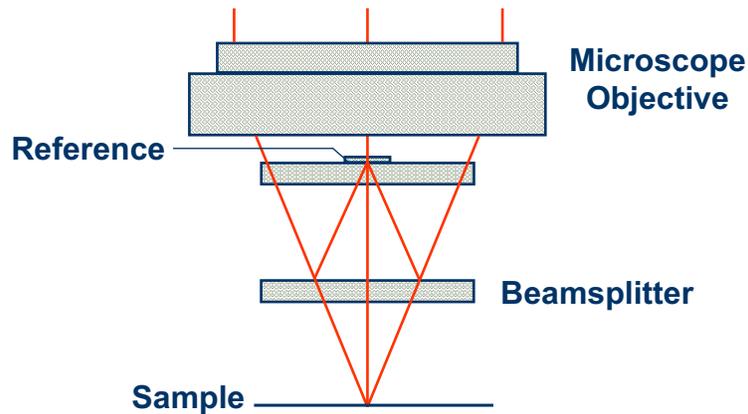


Interference Microscope Diagram



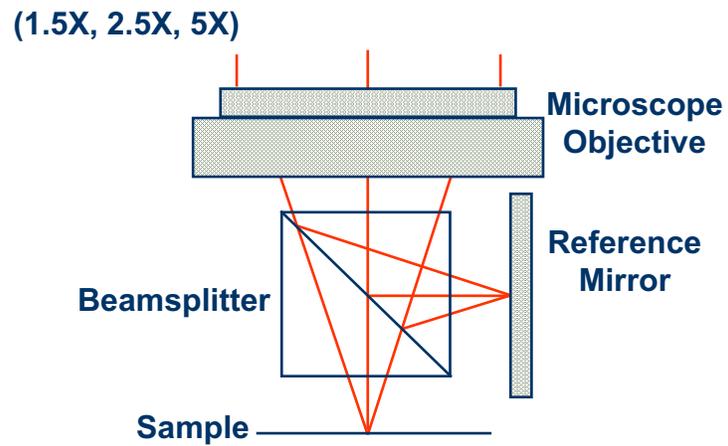
Mirau Interferometer

(10X, 20X, 50X)

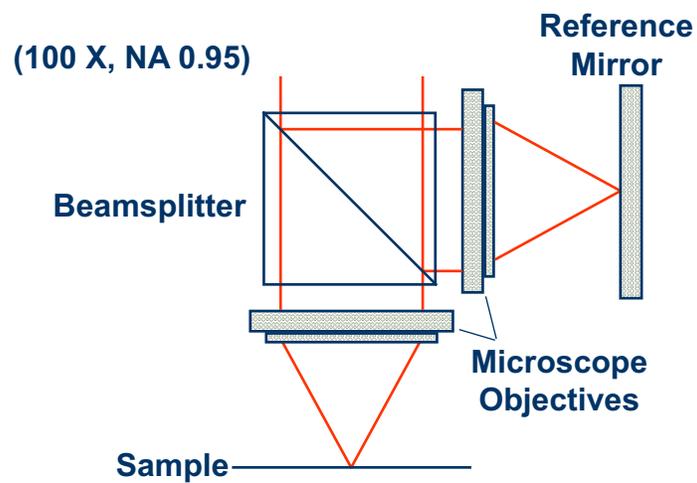




Michelson Interferometer



Linnik Interferometer





Interference Objectives

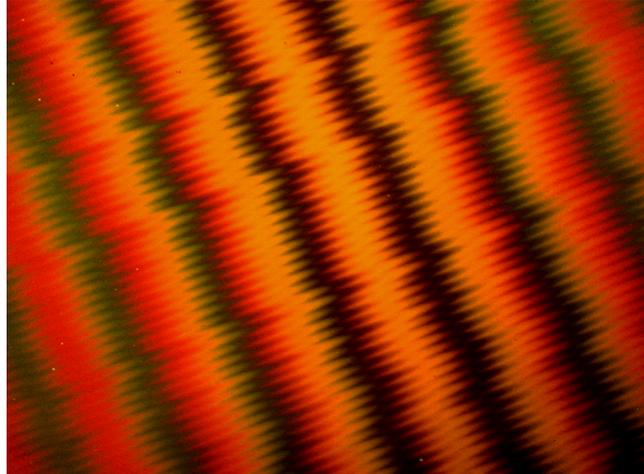
- **Mirau**
 - Medium magnification
 - Central obscuration
 - Limited numerical aperture
- **Michelson**
 - Low magnification, large field-of-view
 - Beamsplitter limits working distance
 - No central obscuration
- **Linnik**
 - Large numerical aperture, large magnification
 - Beamsplitter does not limit working distance
 - Expensive, matched objectives



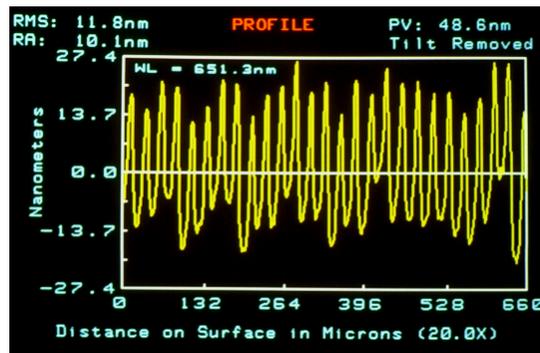
Optical Profiler



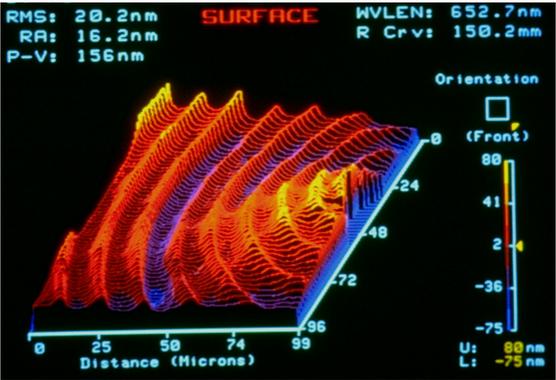
White Light Interferogram



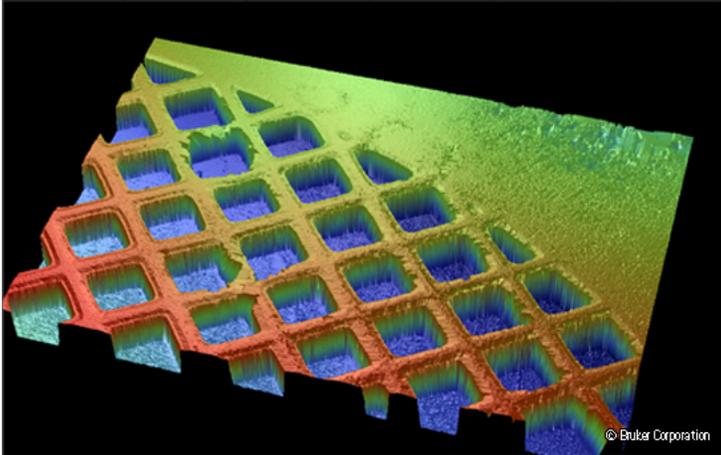
Profile of Diamond Turned Mirror



Diamond Turned Mirror

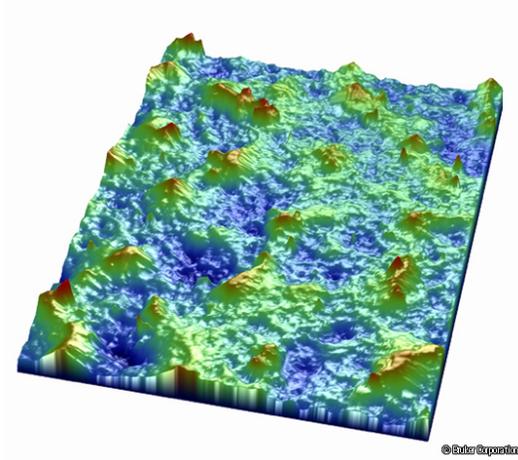


Grating



Ref: Bruker

Diamond Film



© Bruker Corporation

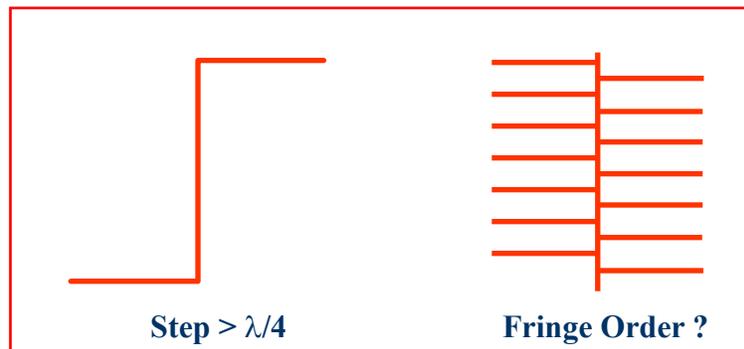
Ref: Bruker

2017 – James C. Wyant

How High is the Step?



Steps $> \lambda/4$ between adjacent detector pixels introduce integer half-wavelength height ambiguities



White Light Interferometry

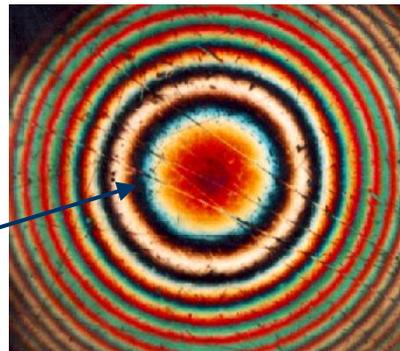


- Eliminates ambiguities in heights present with monochromatic interferometry
- Techniques old, but use of modern electronics and computers enhance capabilities and applications

White Light Interference Fringes



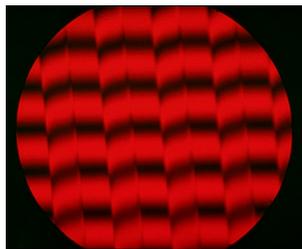
- Fringes form bands of contour of equal height on the surface with respect to the reference surface.
- Fringe contrast will be greatest at point of equal path length or “best focus.”



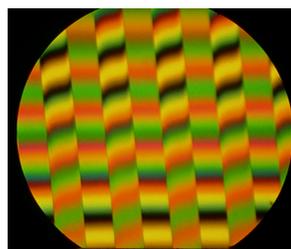
Interferograms of Diffraction Grating



Quasi-Monochromatic Light



White Light



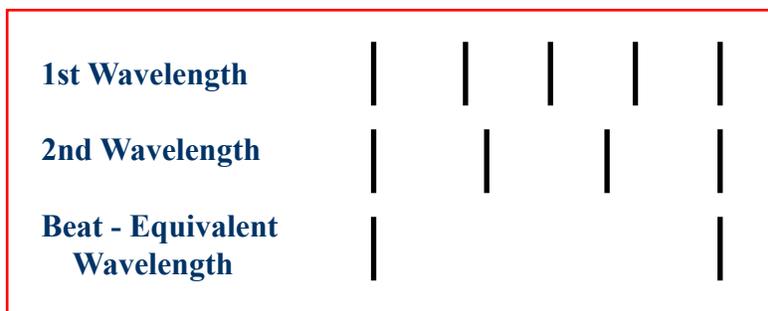
Profile



Two Wavelength Measurement



- Measure Beat Frequency
- Long Effective Wavelength





Two Wavelength Calculation

Equivalent Wavelength $\lambda_{eq} = \frac{\lambda_1 \lambda_2}{|\lambda_1 - \lambda_2|}$

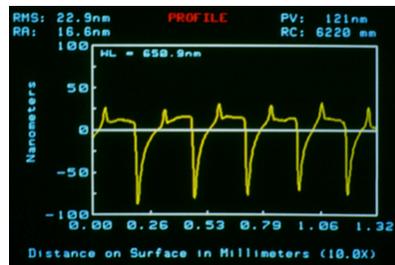
Equivalent Phase $\varphi_{eq} = \varphi_1 - \varphi_2$

No height ambiguities as long as height difference between adjacent detector pixels < equivalent wavelength / 4

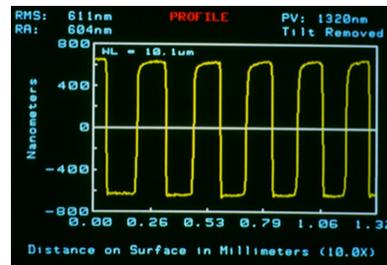


Diffraction Grating Measurement

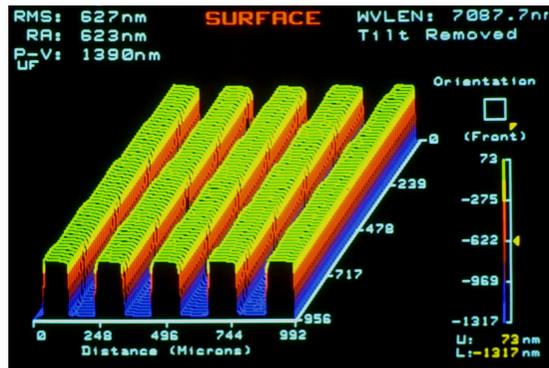
Single wavelength
(650 nm)



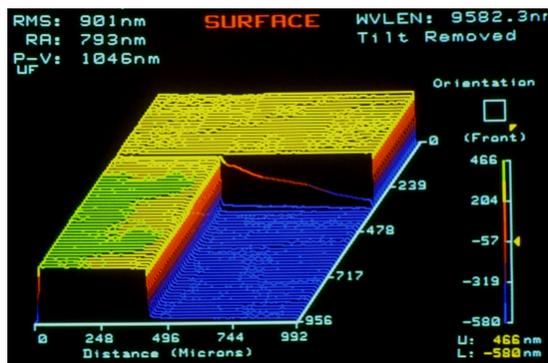
Equivalent wavelength
(10.1 microns)



3-D Two-Wavelength Measurement (Equivalent Wavelength, 7 microns)



Two-Wavelength Measurement of Step

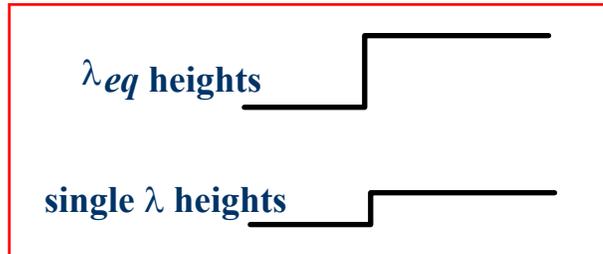


Wavelength Correction



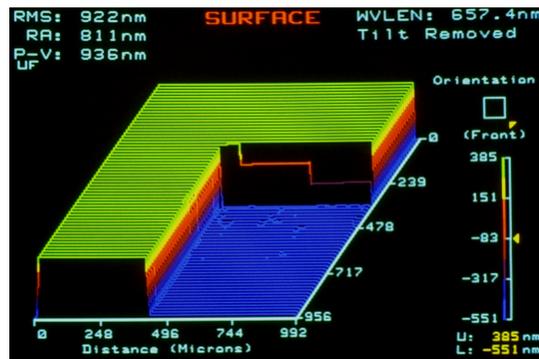
Compare

- Heights calculated using equivalent wavelength
- Heights calculated using single wavelength



Add $N \times \lambda/2$ to heights calculated using single wavelength so difference $< \lambda/4$

Wavelength Correction Measurement of Step

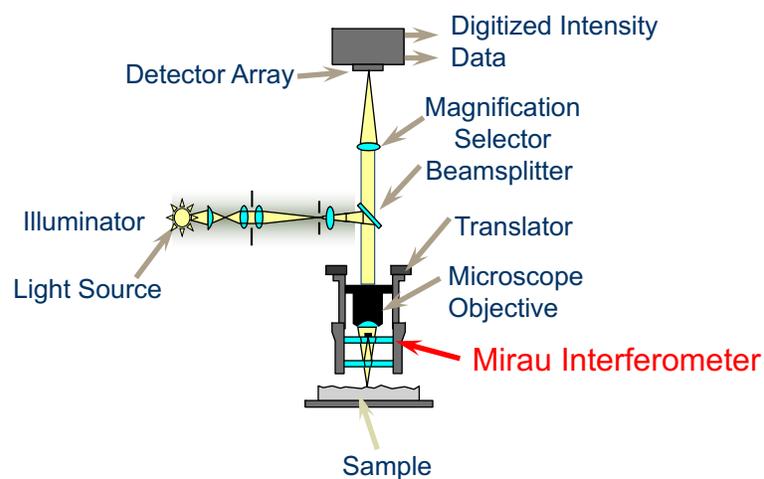


Principles of Vertical Scanning Interferometry



- A difference between the reference and test optical paths causes a difference in phase.
- Best fringe contrast corresponds to zero optical path difference.
- Best focus corresponds to zero optical path difference.

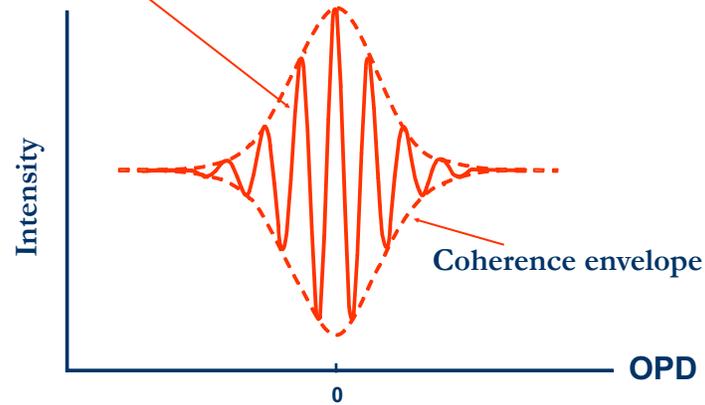
Interference Microscope Diagram



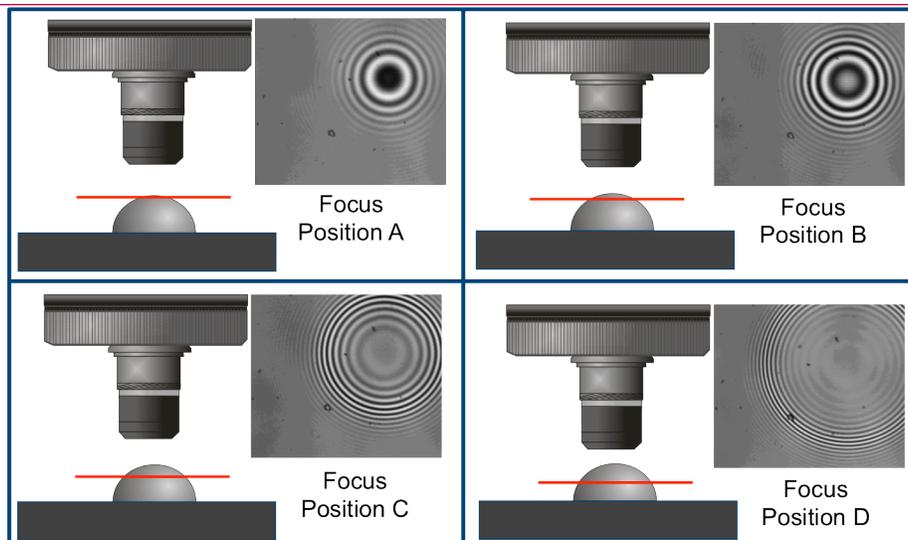


Irradiance Signal Through Focus

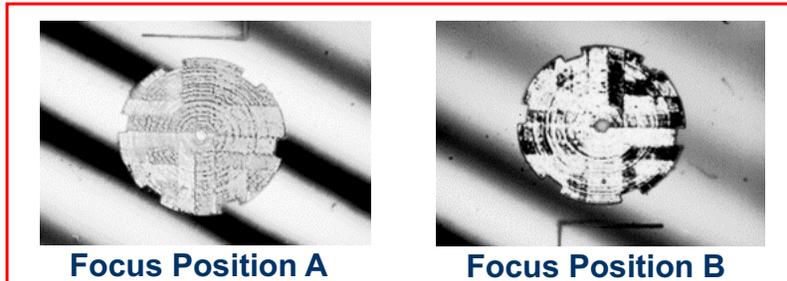
$$I = I_0 [1 + \gamma(OPD) \cos(\phi + \alpha)]$$



Vertical Scanning Interference Microscope



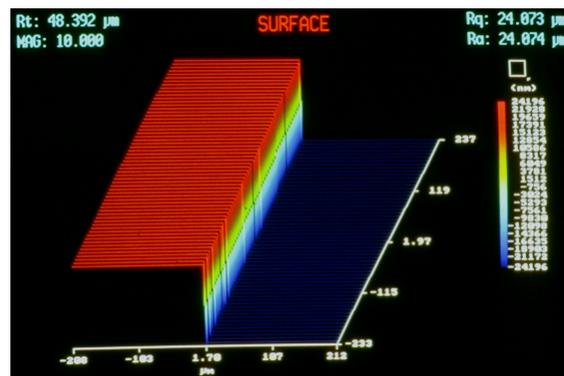
White Light Interferograms



As the scan moves different areas of the part being measured come into focus (have zero OPD or maximum contrast between fringes).

A determination of the point of maximum contrast and knowledge of the scan position allows a reconstruction of the surface shape.

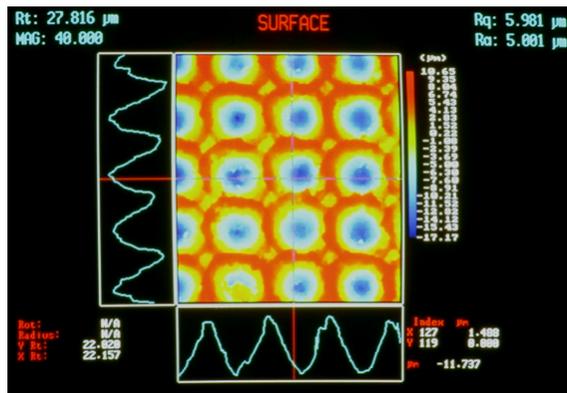
Step Measurement



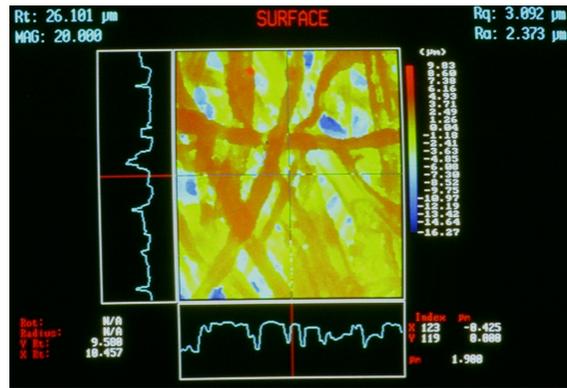
Print Roller



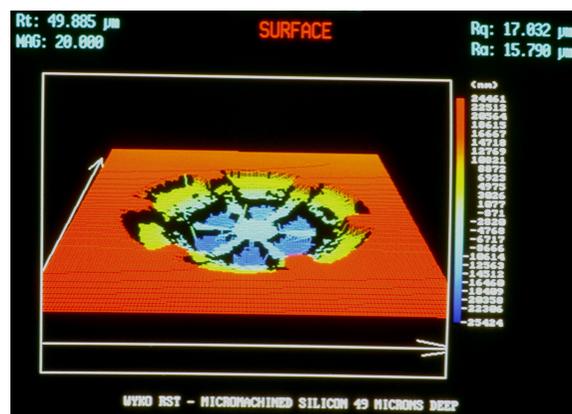
Print Roller Measurement



Paper Measurement



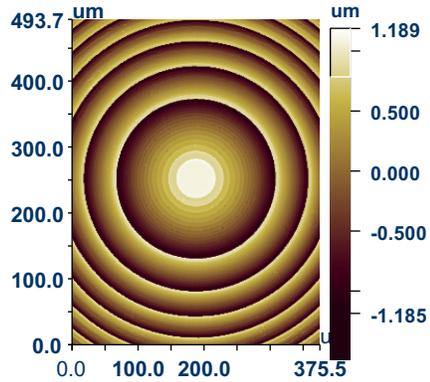
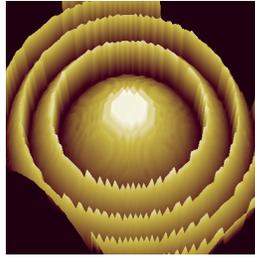
Micromachined Silicon Measurement





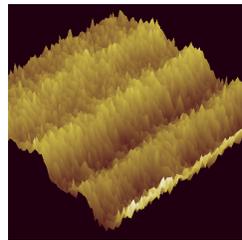
Binary Optic Lens

Surface Stats:
RMS: 561.30 nm
PV: 2.37 μm



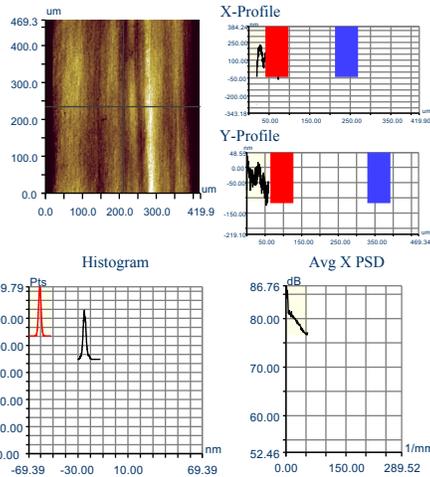
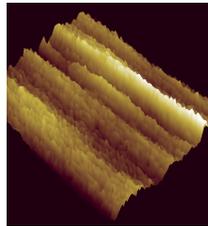
Chatter Seen on Camshaft

Surface Stats:
Rq: 872.06 nm
Ra: 693.90 nm
Rt: 7.47 μm
Terms Removed:
Cylinder & Tilt





Heart Valve



Data Statistics
Rt: 1.419 um
Ra: 87.391 nm
Rq: 113.942 nm

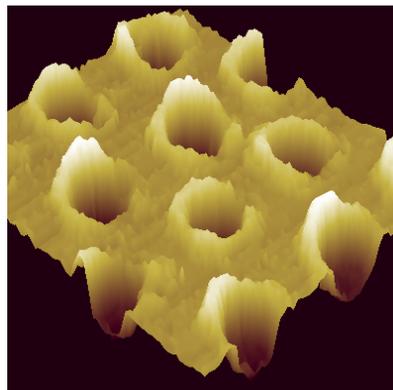


Pits in Metal

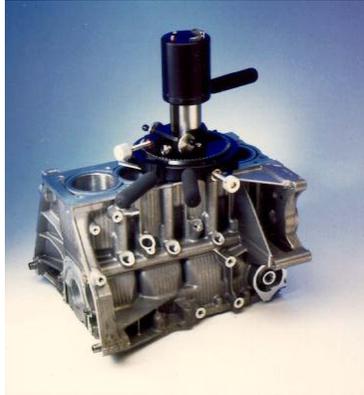
Size: 248 X 239
Sampling: 1.70 um

Surface Stats:
Rq: 5.07 um
Ra: 3.44 um
Rt: 31.05 um

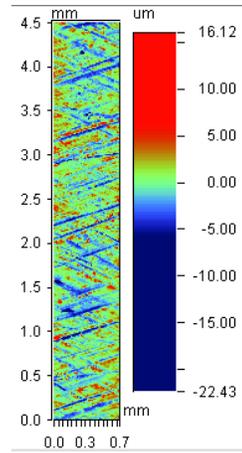
Terms Removed:
Tilt



Six Stitched Data Sets of Inside of Engine Bore

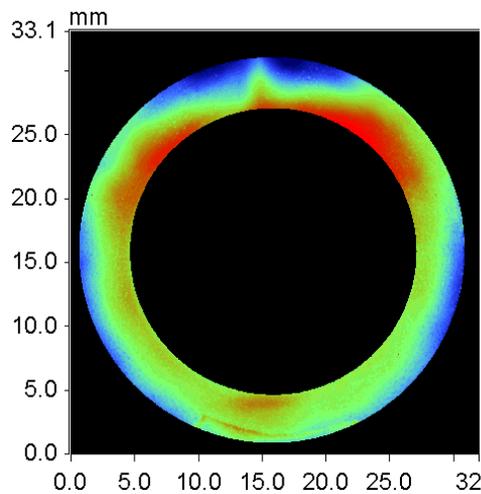


**Insight 2000 measuring
inside of engine bore**



Ra = 1.69 μm , Rz = 27.87 μm , and Rt = 38.54 μm

Stitched Measurement - Fuel Cap

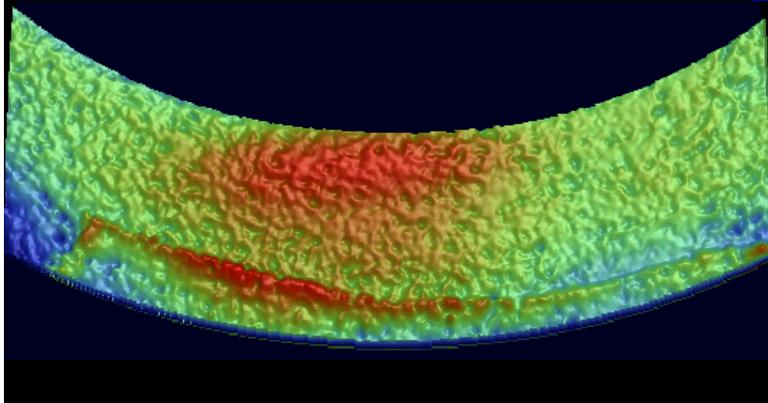


**VSI
mode**

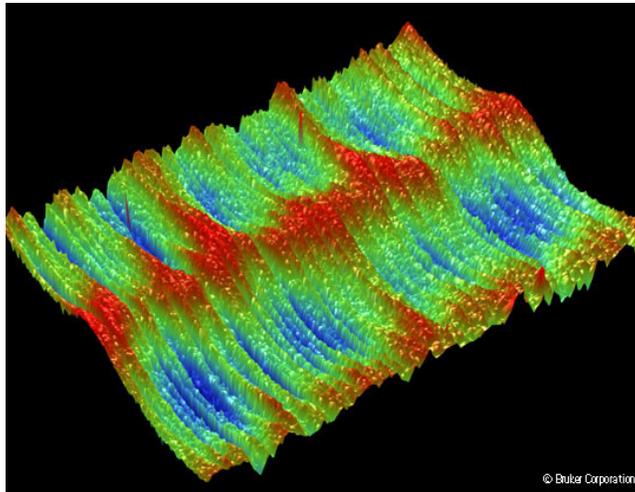
Surface statistic

**Ra=26.32 microns
Rq=32.72 microns
Rt=246.42 microns
array size 1251x1107
sampling 25.5 microns**

Sub-Region of Stitched - Fuel Cap

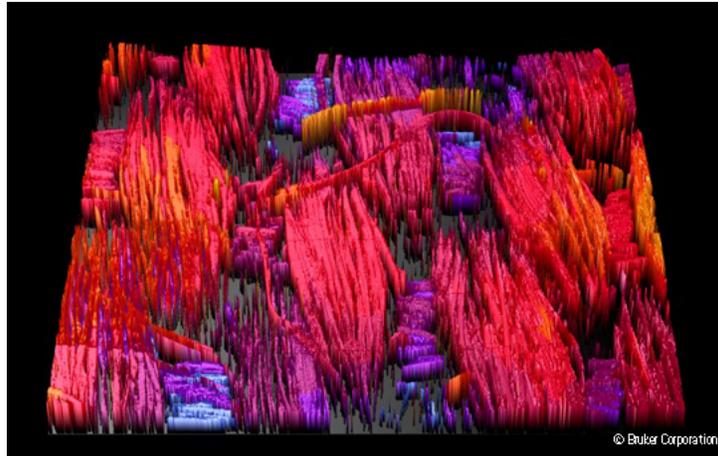


Chatter on Camshaft



© Bruker Corporation

Woven Cloth



Part 7 - Absolute Measurements



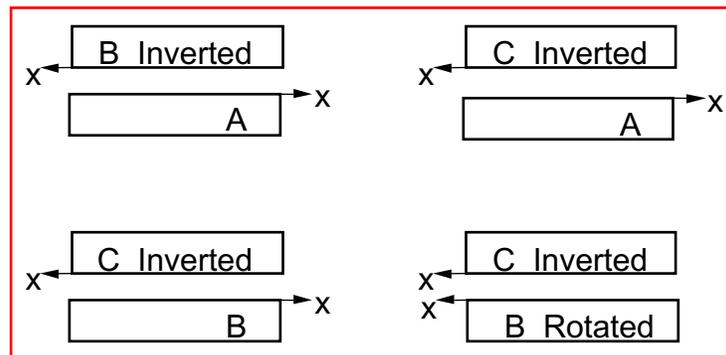
- **Absolute measurement of flats**
- **Absolute measurement of spheres**
- **Absolute measurement of surface roughness**

Absolute Surface Shape Measurement



- Removing system aberrations & reference surface effects
- Improves measurement accuracy
- Tests for
 - Flats
 - Spheres
 - Surface roughness

Measurements Required for Three-Flat Test





Three-Flat Test Equations

Make 4 Measurements

$$G_{AB}(x,y) = f_A(x,y) + f_B(-x,y)$$

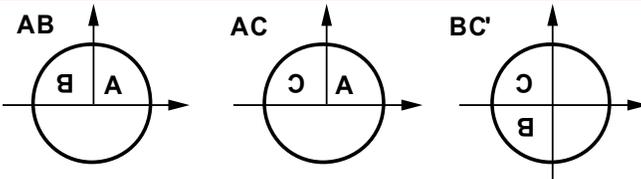
$$G_{AC}(x,y) = f_A(x,y) + f_C(-x,y)$$

$$G_{BC}(x,y) = f_B(x,y) + f_C(-x,y)$$

$$G_{BC'}(x,y) = f_B(-x,-y) + f_C(-x,y)$$



Three-Flat Test - X Line



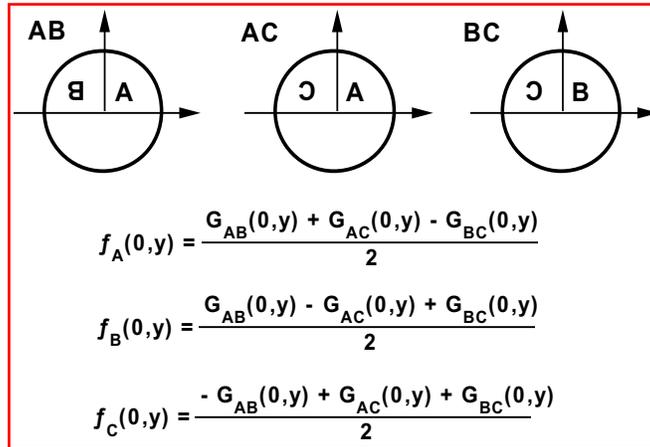
$$f_A(x,0) = \frac{G_{AB}(x,0) + G_{AC}(x,0) - G_{BC'}(x,0)}{2}$$

$$f_B(x,0) = \frac{G_{AB}(x,0) - G_{AC}(x,0) + G_{BC'}(x,0)}{2}$$

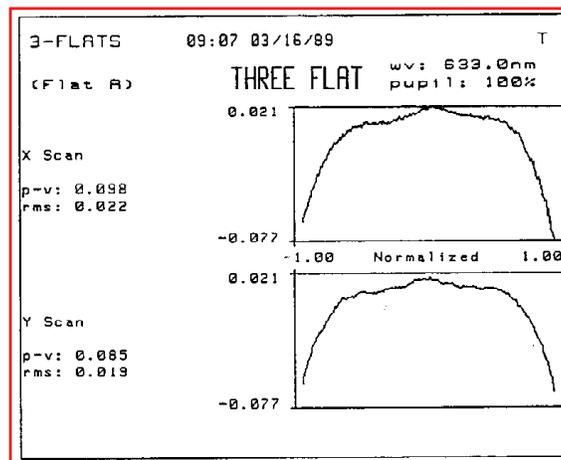
$$f_C(x,0) = \frac{-G_{AB}(x,0) + G_{AC}(x,0) + G_{BC'}(x,0)}{2}$$



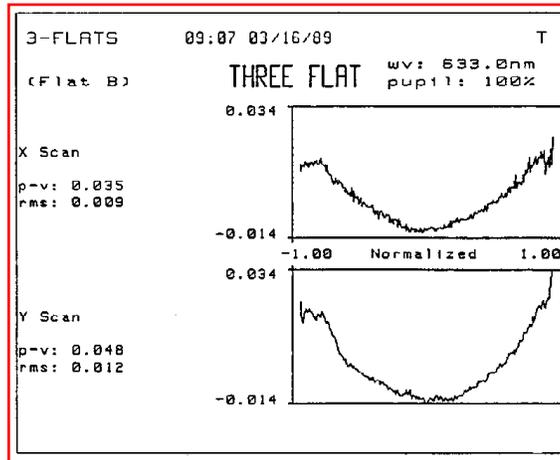
Three-Flat Test - Y Line



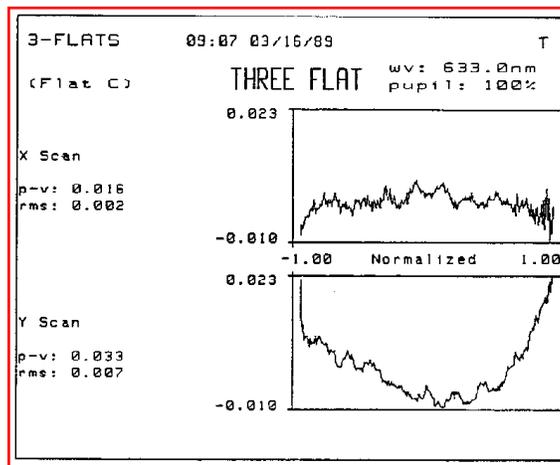
Three-Flat Test - Flat A



Three-Flat Test - Flat B



Three-Flat Test - Flat C

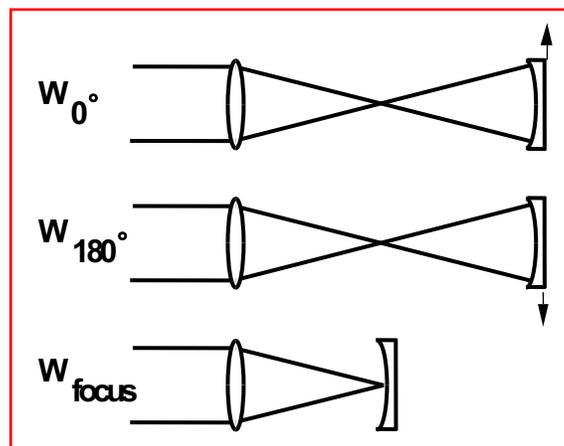


Absolute Sphere Testing



- Separate interferometer errors from errors in spherical mirror being tested.
- Three measurements required.

Absolute Sphere Testing (Measurements Required)





Absolute Sphere Testing (Equations)

$$W_{focus} = W_{ref} + \frac{1}{2} [W_{div} + \bar{W}_{div}]$$

$$W_{0^\circ} = W_{surf} + W_{ref} + W_{div}$$

$$W_{180^\circ} = \bar{W}_{surf} + W_{ref} + W_{div}$$

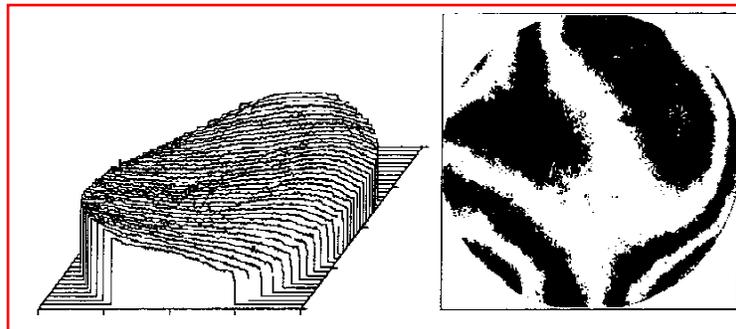
COMBINE 3 MEASUREMENTS

$$W_{surf} = \frac{1}{2} [W_{0^\circ} + \bar{W}_{180^\circ} - W_{focus} - \bar{W}_{focus}]$$



Single Measurement of Sphere

TILT, POWER REMOVED
INTERVAL = 0.025
RMS = 0.014 WAVES
P-V = 0.121 WAVES

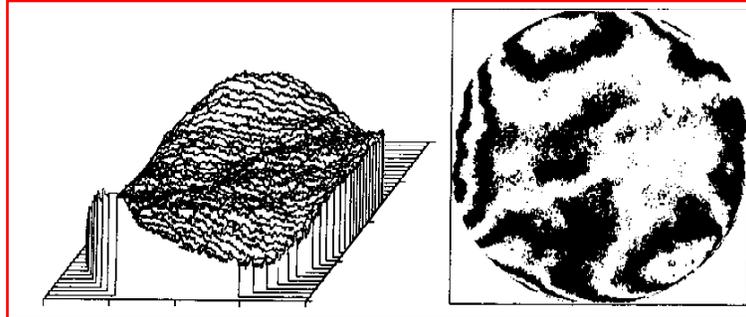


FIZEAU INTERFEROMETER, F/1.1 REF. SPHERE



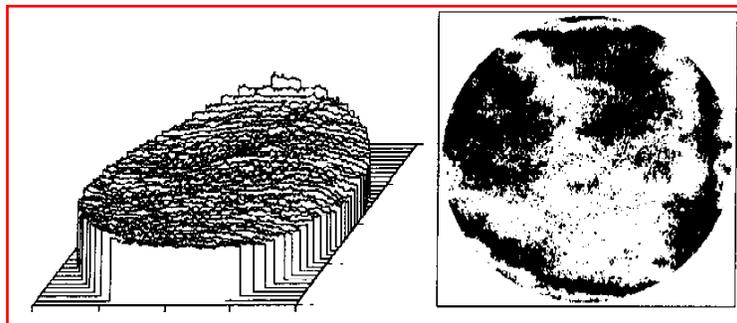
Flat at Focus f/1.1 Diverger

TILT, POWER, COMA REMOVED
INTERVAL = 0.05
RMS = 0.027 WAVES
P-V = 0.243 WAVES



Absolute Reference

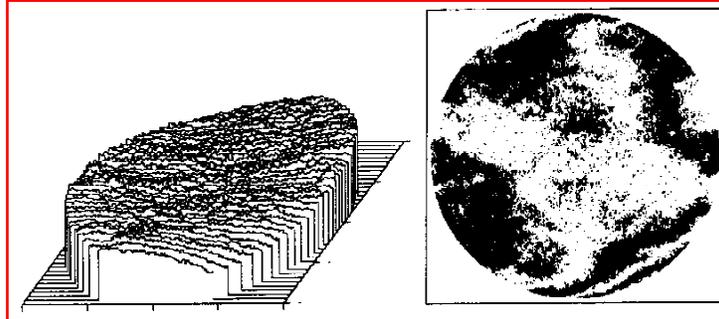
TILT, POWER REMOVED
INTERVAL = 0.025
RMS = 0.010 WAVES
P-V = 0.084 WAVES





Absolute Measurement of Sphere

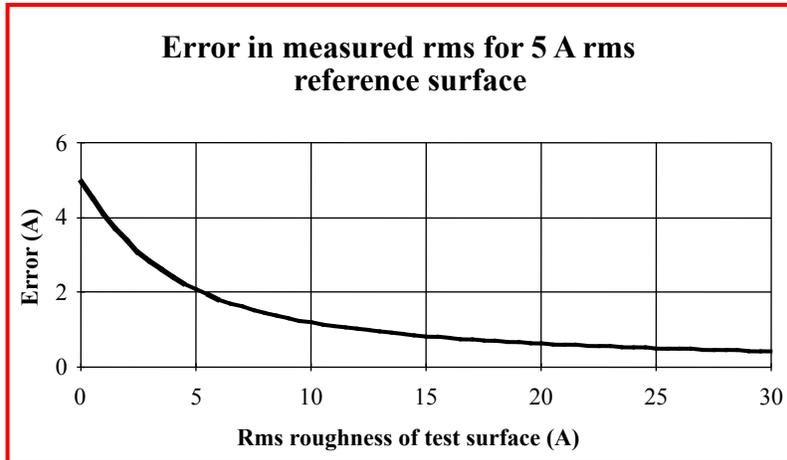
**TILT, POWER REMOVED
INTERVAL = 0.025
RMS = 0.011 WAVES
P-V = 0.081 WAVES**



Absolute Surface Roughness Measurement Assumptions

- Surface height is random
- Statistics do not vary over surface
- Each measurement = Test + Reference
- Test and reference uncorrelated

Effect of Reference Surface on Measurement



Subtraction of Errors due to Reference Surface



- Perfect mirror
- Generate reference
- Absolute rms measurement

Generate Reference

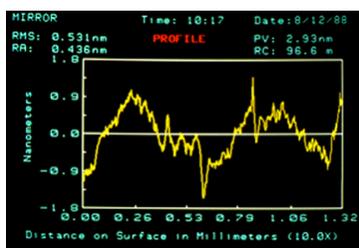


- Average many measurements
- Move random surface > correlation length between measurements
- Effects of random surface reduce as square root of number of measurements

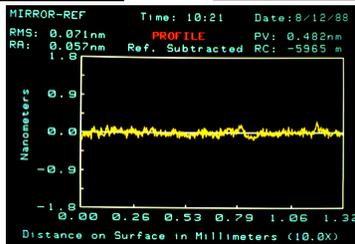
Generate Reference and Subtract



Surface + Reference



Reference



Surface
(0.071 nm)



Absolute RMS Measurement

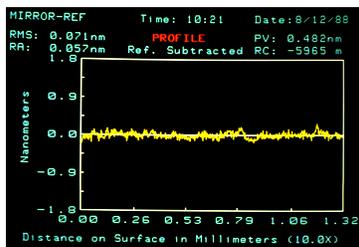
- Make 2 measurements where surface moved > correlation length between measurements
- Subtract measurements and divide by square root of 2
- Reference cancels and obtain
- RMS of test surface

$$Diff = Test_1 + (-Test_2)$$
$$RMS_{Test} = \frac{1}{\sqrt{2}} RMS_{Diff}$$



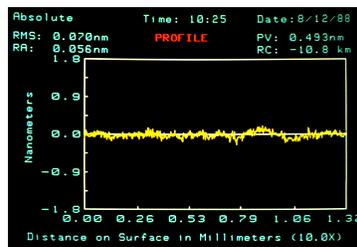
Generate Reference and Absolute RMS Comparison

Generate Reference



RMS = 0.071 nm

Absolute RMS



RMS = 0.070 nm

Part 8 – Concluding Remarks



- **Limitations of Direct Phase Measurement Interferometers**
- **Most Important to Remember**
- **References**

Limitations of Direct Phase Measurement Interferometers



- **Accuracy generally limited by environment**
 - **Vibration**
 - **Turbulence**
- **Measurement of surface roughness less limited by environment because path differences small**
- **Single-shot phase-measurement interferometers greatly reduce the effects of vibration and turbulence effects can be averaged out.**

Remember



- **If you make optics you have to be able to test the optics because you cannot make optics any better than you can test.**
- **If you purchase optics you need to test the optics you buy to make sure the optics meet the specs.**
- **If you let the supplier know you are going to test the optics when you receive them you will get better optics.**

References



D. Malacara, Ed., Optical Shop Testing

W. Smith, Modern Optical Engineering

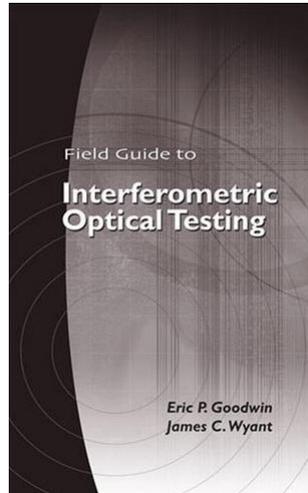
**Kingslake, Thompson, Shannon, and Wyant, Ed. Applied Optics
and Optical Engineering, Vols. 1-11**

Goodwin and Wyant, Field Guide to Interferometric Optical Testing

**Optical Society of America
Optics Infobase**

**SPIE
Digital Library**

Field Guide to Interferometric Optical Testing (Published by SPIE)



Thank you for taking the short course!

