#### We return to our basic scenario:



Einstein: If A & B are separated in space then measurements on A & B can be spacelike separated events 

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## Seems reasonable, given what we know about Special Relativity and Causality

How to think about this in a rigorous, testable way?

### **Thought experiment:** Scheduling a date

1. Alice and Bob share qubits in the entangled state

They agree that if Bob measures  $^{\uparrow}_{2}$  at a specified later date then he will visit Alice.

- 2. Alice travels to a galaxy far, far away
- 3. At the agreed-upon time Alice and Bob measure their qubits

Alice instantly knows about Bob's travel plans. Moreover, this information did not exist prior to their measurements

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#### Let us be clear:

- (1) Alice and Bob have no control over the outcome of their measurements it is equally likely that they both get  $\frac{1}{2}$  or they both get  $\frac{1}{2}$ . Thus they cannot signal each other to say "I am bored, come visit"
- (2) Alice and Bob would be in the same situation if they shared a mixed state,

$$S = \frac{1}{2} \left( | 1_2 1_2 \times 1_2 1_3 | + | 1_2 1_2 \times 1_2 1_4 | \right)$$

Therefore entanglement is not involved!

(3) Alice and Bob would be in the same situation if a machine prepared two boxes with either a green ball in each or a red ball in each, chosen by some fundamentally random process.

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### Did we go too far?

Classical balls | Info was there all along

Entangled spins Info came into existence when the measurement was made

Note: This distinction is meaningless to Alice and Bob

Nevertheless , the quantum and classical physics appears fundamentally different

### **Bells inequalities:**

Guidelines to set up experiments with entangled spins so quantum mechanics and "reasonable classical models" (Hidden Variable Theories) make different and testable predictions

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## **Local Hidden Variable (LHV) Theories**

Measurement is fundamentally deterministic. It appears probabilistic only because the state of a system is described by the quantum state plus a set of hidden variables whose values are not known and cannot be controlled

QM: Preparation  $\Rightarrow$  spin in state  $|\psi_{S}\rangle$ 

LHV: Preparation 

spin state (145>, {λ})

1HV:

**Example:**  $|45\rangle$ , one HV  $05\lambda51$ , uniformly distributed

Measure:  $\sigma_2 \Rightarrow \begin{cases} |\uparrow_2\rangle & \text{for } 0 \le \lambda \le \cos^2 \frac{\Theta}{2} \\ |\downarrow_2\rangle & \text{for } \cos^2 \frac{\Theta}{2} \le \lambda \le 1 \end{cases}$ 

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LHV: Preparation  $\Rightarrow$  spin state  $(14_S)$ ,  $\{\lambda\}$ 

**Example:**  $|4 \rangle$ , one HV  $0 \leqslant \lambda \leqslant 1$ , uniformly distributed

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**Einstein:** There exist a LHV description of a spin-1/2. Thus, once prepared, the outcome of measuring  $\nabla_{\hat{n}} = \vec{\nabla} \cdot \hat{n}$  is completely determined by the LHV state  $( [\psi_s \rangle_i \{ \lambda \} )$ , and we could predict the outcome deterministically if only we knew  $[\psi_s \rangle$  and the values of all the HV's in the set  $\{\lambda \}$ .

HV Theory: This happens because measuring of disturbs the values of the HV's in ways we cannot control and cannot know.

Nevertheless, the original HV state (14),  $(\lambda)$  contains all the info needed to predict the outcome of any pair of measurements  $\sigma_{\vec{n}}$  or  $\sigma_{\vec{n}}$ .

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### **Physical Reality of HV's?**

If QM is always correct and HV theories make no measurably different predictions, then we conclude the [[]] do not represent any element of physical reality (Occams Razor)

### **EPR** experiment with spins:

(1) Prepare 2 spins in state  $|\psi\rangle = \frac{1}{\sqrt{2}} \left( |\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle \right)$ 

Note: Total spin 
$$\vec{j} = \vec{S}_1 + \vec{S}_2$$
,  $| \vec{\Phi}_2 \rangle = | \vec{j} = 0, M = 0 \rangle$   
(Singlet state, rotationally invariant)

(2) Separate and measure আ (A) and আ (B) as spacelike separated events ⇒

Local descriptions 
$$\begin{cases} S_{A} = Tr_{B}(| \nabla X \nabla L|) \\ S_{B} = Tr_{A}(| \nabla X \nabla L|) \end{cases}$$

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- (2) Separate and measure জু(A) and জু (৫) as spacelike separated events ♠

Local descriptions 
$$\begin{cases} S_{A} = Tr_{B} (| \nabla_{x} \nabla_{x} |) \\ S_{B} = Tr_{A} (| \nabla_{x} \nabla_{x} |) \end{cases}$$

SA, SB no info about correlations, in QM no local description is possible

- (3) Is a LHV description possible?

  To test, assign a LHV state (𝒢; , ἐλἐ), ; = Α, ß

  where complete knowledge of the HVs

  allows deterministic predictions regarding

  measurements of ση (Α), σμ (β) and their

  correlations.
- \* Experiments we know measurements of  $\sigma_{\vec{n}}(A), \sigma_{\vec{n}}(B)$  are always perfectly correlated source must build in correlations between  $\{\lambda\}_A, \{\lambda\}_B$  to make this happen
- \* Even so, we still cannot predict if outcomes will be  ${}^{\uparrow}_{\vec{n}}, \downarrow_{\vec{n}}$  or  ${}^{\downarrow}_{\vec{n}}, {}^{\uparrow}_{\vec{n}}$
- (4) Spacelike interval Dobs measurement cannot alter the LHV state (\$\sigma\_A, \{\lambda\ceig\_A, \{\lambda\ceig\_A\ceig\_A\ceig\_A\ceig}\)
- \* Bob measures ﷺ (B) we know result if

  Alice were to measure ♂ਜ਼(A)
- \* Instead Alice we have effectively measured complementary observables  $\sigma_{\mathcal{A}}(A)$ ,  $\sigma_{\widetilde{\mathbf{m}}}(A)$ ,  $\sigma_{\widetilde{\mathbf{m}}}(A)$ ,  $\sigma_{\widetilde{\mathbf{m}}}(A)$

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(5) In a LHV description complete info about the measurement outcomes and correlations must reside in the HV state ( $\mathcal{Q}_{A_1} \{\lambda\}_A$ )

John Bell: The LHV description above forces us to make certain predictions about the outcomes of joint measurements that are In conflict with those of Quantum Mechanics

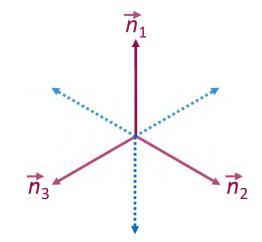
Setup: Alice and Bob choose at random between measurement axes. For example, we can use this (not unique) configuration

Alice chooses among

$$\vec{n}_1 = (0,0,1)$$

$$\overrightarrow{N}_{2} = \left(\frac{\sqrt{3}}{2}, 0, -\frac{1}{2}\right)$$

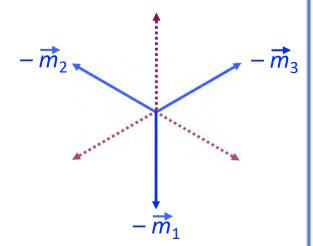
$$\vec{n}_3 = \left(-\frac{\sqrt{3}}{2}, 0, -\frac{1}{2}\right)$$



Bob chooses among

$$\vec{m}_2 = -\vec{n}_2$$

$$\vec{m}_2 = -\vec{n}_2$$



Repeat many times, keep those runs where  $\vec{m} \neq -\vec{n}$ .

Our measurement outcomes will not be perfectly correlated, but we can estimate the probabilities  $\mathcal{C}_{\text{Same}}(i,j)$  that the outcomes are  $\uparrow_{\vec{n}_i} \downarrow_{\vec{n}_j}$  and  $\downarrow_{\vec{n}_i} \uparrow_{\vec{n}_j}$  for any pair (i,j),  $i \neq j$ .

Accept LHV description  $\implies$  we must have complete info about 3 combinations (i,j) = (1,2),(1,3),(2,3) at the same time, all encoded in Alice's LHV state.

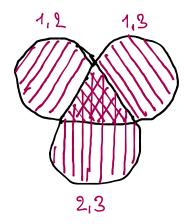
#### **Equivalent Scenario:**

Imagine we flip 3 coins repeatedly, and each time pick two at random and look at those only. The coin flip process builds in correlations between the coins (HV values) that we can observe through measurements. This allows us to estimate  $\Pr(i,j) \forall (i,j)$ 

Note: If we flip 3 coins (heads or tails) then at least 2 of them must have the same value. This gives us the following Bell's inequality:

$$P_{\text{same}}(1,2) + P_{\text{same}}(1,3) + P_{\text{same}}(2,3) \ge 1$$

We can show this graphically by considering the overlap of the 3 sets  $P(1,2 \vee 1,3 \vee 2,3) = 1$ 



(It does not matter if the coins are fair)

Note: This conclusion rests on one thing only – that the head-ness or tail-ness is a settled property of the coins before we look at them.

This is exactly what a LVH description says about the spin measurements in an EPR experiment.

But It turns out to be in conflict with the predictions of Quantum Mechanics!!

#### **Quantum Mechanics:** (From Preskill)

The prob. of an outcome is the expectation value of the corresponding projector. We have

$$E(\vec{n},+) = |\hat{n}_{\vec{n}} \times \hat{n}_{\vec{n}}| = \frac{1}{2} (\mathbf{1} + \vec{n} \cdot \vec{\sigma}) = \frac{1}{2} (\mathbf{1} + \hat{n}_{\vec{n}})$$

$$E(\vec{n},-) = |\hat{j}_{\vec{n}} \times \hat{j}_{\vec{n}}| = \frac{1}{2} (\mathbf{1} - \vec{n} \cdot \vec{\sigma}) = \frac{1}{2} (\mathbf{1} - \hat{n}_{\vec{n}})$$
projectors for outcomes up/down along  $\vec{n}$ 

#### **Probability of identical outcomes**

$$P(\pm,\pm) = \langle \mathcal{D}_{-} [E^{(A)}(\vec{N},\pm) E^{(B)}(m,\pm) | \mathcal{D}_{-} \rangle^{1})$$

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$$= \frac{1}{4} (1 + \langle \mathcal{D}_{-} [\mathcal{D}_{-}^{(A)} \mathcal{D}_{-}^{(B)} ] \mathcal{D}_{-} \rangle^{2})$$

#### Next we use

$$\begin{split} &\left(\overrightarrow{\sigma}^{(A)} + \overrightarrow{\sigma}^{(B)}\right) | \psi_{-} \rangle = 0 \Rightarrow \overrightarrow{\sigma}^{(B)} | \psi_{-} \rangle = -\overrightarrow{\sigma}^{(A)} | \psi_{-} \rangle \Rightarrow \\ &\left\langle \psi_{-} | \sigma_{R}^{(A)} \sigma_{\widetilde{M}}^{(B)} | \psi_{-} \rangle = -\langle \psi_{-} | \sigma_{\widetilde{M}}^{(A)} \sigma_{\widetilde{M}}^{(A)} | \psi_{-} \rangle \\ &= \text{Tr} \left[ \mathcal{G}_{A} \sigma_{\widetilde{M}}^{(A)} \sigma_{\widetilde{M}}^{(A)} \right] = \frac{1}{2} \text{Tr} \left[ (\vec{n} \cdot \overrightarrow{\sigma}) (\vec{m} \cdot \overrightarrow{\sigma}) \right] \qquad \text{(using } \mathcal{G}_{A} = \frac{1}{2} \cancel{A} \text{)} \\ &= -\frac{1}{2} \sum_{i,j} n_{i} m_{j} \text{Tr} \left[ \sigma_{i}^{(A)} \sigma_{j}^{(A)} \right] = -\frac{1}{2} \sum_{i,j} n_{i} m_{j} \delta_{i,j} \quad \text{(using } \text{Tr} \left[ \sigma_{i} \sigma_{j} \right] = \delta_{i,j} \text{)} \\ &= -\vec{n} \cdot \vec{m} = -\cos \theta, \quad \Theta = \text{angle between } \vec{n}, \vec{m} \end{split}$$

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$$| \nabla \rangle = \frac{1}{\sqrt{2}} \left( | \hat{T}_{\vec{n}}^{(A)} \rangle | \hat{J}_{\vec{n}}^{(B)} \rangle - | \hat{J}_{\vec{n}}^{(A)} \rangle | \hat{T}_{\vec{n}}^{(B)} \rangle \right),$$
 2)  $\langle \hat{T}_{\vec{n}}^{(A)} \rangle = \langle \hat{T}_{\vec{n}}^{(A)} \rangle = 0$ 

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$$1) \left| \mathcal{T}_{n} \right\rangle = \frac{1}{\sqrt{2}} \left( \left| \mathcal{T}_{n}^{(A)} \right\rangle \left| \mathcal{I}_{n}^{(B)} \right\rangle - \left| \mathcal{I}_{n}^{(A)} \right\rangle \left| \mathcal{T}_{n}^{(B)} \right\rangle \right), \qquad 2) \left\langle \mathcal{T}_{n}^{(A)} \right\rangle = \langle \mathcal{T}_{n}^{(B)} \rangle = 0$$

Note:  $\nabla_i$  are the Pauli operators i=1,2,3, and  $\nabla_n$  is the component of the Pauli vector along  $\vec{n}$ 

This gives us

$$P(t,t) = \frac{1}{4}(1-\cos\theta)$$
  
 $P(t,\tau) = \frac{1}{4}(1+\cos\theta)$ 

In John Bell's version of the EPR experiment the angles between the  $\vec{n}_i$  and the  $\vec{m}_{ij}$  are all  $60^{\circ}$ ,  $\cos 60^{\circ} = \frac{1}{2}$ .



#### **Whereas**

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This is in conflict with the LHV model of the experiment !! Actual experiments agree with QM, rules out LHV's by many standard deviations.

David Mermin: Is reality really real? (Physics Today)

### **Possible Resolutions**

- \* New physics beyond QM no sign so far
- \* Complementarity Alice did not measure  $\sigma_{\widetilde{n}_{i}}^{(n)}$   $\sigma_{\widetilde{n}_{i}}^{(n)}$  and it is meaningless to assign probs to measurements that were not done.
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- \* Alternative: Take QM at face value.

Nature does not allow us to assign LHV descriptions to Alice and Bob's qubits if they are entangled. Only the Global State Has objective Physical Reality

This is not hard to accept if we embrace the viewpoint of Quantum Information Science

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Quantum States are States of Knowledge. Thus, in the EPR experiment a global observer is permitted by Nature to have only as much information as can be encoded in the global state vector. This allows to predict correlations and nothing else. Nature does not allow local observers with access to only one spin to have any information about it.

### **Real EPR Experiments:**

- \* Tend to use photons with entangled polarization states
- \* Earliest experiments used photons produced in atomic cascades (Aspect); modern experiments use photon pairs from spontaneous parametric downconversion.
- \* Photon experiments use polarization states <a href="https://www.ncorresponding">x>, ly></a>
  corresponding to linear polarizations forming a

  90° angle



Relevant formulae contains angles that are half of those for spins

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### <u>Loopholes – some examples</u>

- \* Locality (space-like separated measurements)
- \* Fair Sampling (detection efficiency)
- \* Freedom of choice (truly random meas. settings)
- \* Coincidence time (locally defined detection windows)
- \* Memory (trials not identical and independent)

See selection of papers on the EPR paradox under the "Reading" tab on the OPTI 646 website.

- \* First good experiments Aspect et al. (3 papers)
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Hensen et al., Giustina et al., Shalm et al.

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## From Preskill's notes, chapter 4.1

Bell's logic seemed compelling but something went wrong, so we are forced to reconsider his tacit assumptions. First, Bell assumed that there is a joint probability distribution that governs the possible outcomes of all measurements that Alice and Bob might perform. This is the hidden-variable hypothesis. He imagines that if the values of the hidden variables are exactly known, then the outcome of any measurement can be predicted with certainty — measurement outcomes are described probabilistically because the values of the hidden variables are drawn from an ensemble of possible values. Second, Bell assumed that Bob's decision about what to measure in Chicago has no effect on the hidden variables that govern Alice's measurement in Pasadena. This is the assumption that the hidden variables are local. If we accept these two assumptions, there is no escaping Bell's conclusion. We have found that the correlations predicted by quantum theory are incompatible with theses assumptions.

What are the implications? Perhaps the moral of the story is that it can be dangerous to reason about what might have happened, but didn't actually happen — what are sometimes called *counterfactuals*. Of course, we do this all the time in our everyday lives, and we usually get away with it; reasoning about counterfactuals seems to be acceptable in the classical world, but sometimes it gets us into trouble in the quantum world. We claimed that Alice knew what would happen when she measured along  $\hat{a}_1$ , because Bob measured along  $-\hat{a}_1$ , and every time we have ever checked, their measurement outcomes are always perfectly correlated. But Alice did not measure along  $\hat{a}_1$ ; she measured along  $\hat{a}_2$  instead. We got into trouble by trying to assign probabilities to the outcomes of measurements along  $\hat{a}_1, \hat{a}_2$ , and  $\hat{a}_3$ , even though Alice can perform just one of those measurements. In quantum theory, assuming that there is a probability distribution that governs the outcomes of all three measurements that Alice might have made, even though she was able to carry out only one of these measurements, leads to mathematical inconsistencies, so we had better not do it. We have affirmed Bohr's principle of complementary we are forbidden to consider simultaneously the possible outcomes of two mutually exclusive experiments.

## <u>Clauser-Horne-Shimony-Holt</u> (C.H.S.H.) Inequality

(Different version of Bell's inequality)

Alice: 2 settings 
$$\Rightarrow$$
 measure 
$$\begin{cases} A & w/outcome \pm 1 \\ A' & w/outcome \pm 1 \end{cases}$$

Bob: 2 settings 
$$\Rightarrow$$
 measure 
$$\begin{cases} & \frac{\text{w/outcome}}{\text{t1}} \\ & \frac{\text{w/outcome}}{\text{t1}} \end{cases}$$

Note: 
$$a_i a^i = \pm 1 \Rightarrow \begin{cases} a+a^i = 0 & a-a^i = \pm 1 \\ a-a^i = 0 & a+a^i = \pm 2 \end{cases}$$

Combine 
$$w/b$$
,  $b^r = \pm 1$ 

$$C = (a + a^r)b + (a - a^r)b^r = \pm 2$$

HV assumption: Values  $\pm 1$  can be assigned simultaneously to all 4 observables  $\alpha_{i}\alpha_{i}^{i}$   $\beta_{i}\beta_{i}^{i}$ 

It follows that  $|\langle c \rangle| \le \langle |c| \rangle = 2$ 

(C.H.S.H. inequality)

Quantum 
$$Q = \mathcal{F}(A) \cdot \vec{Q}$$
  $\mathcal{E} = \mathcal{F}(B) \cdot \vec{\mathcal{E}}$ 

Mechanics  $Q = \mathcal{F}(A) \cdot \vec{Q}$   $\mathcal{E}' = \mathcal{F}(B) \cdot \vec{\mathcal{E}}'$ 

$$\begin{cases} \langle ab \rangle = \langle a'b \rangle = \langle ab' \rangle = -\cos \theta = -\frac{1}{\sqrt{2}} \\ \langle a'b' \rangle = -\cos(\theta + \frac{1}{2}) = \frac{1}{\sqrt{2}} \end{cases}$$
For  $\theta = 45^{\circ}$ 



 $|\langle ab \rangle + \langle a'b \rangle + \langle ab' \rangle - \langle a'b' \rangle| = \frac{4}{\sqrt{2}} = 2\sqrt{2} > 2$ 

(max violation)

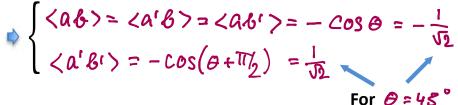
It follows that  $|\langle c \rangle| \le \langle |c| \rangle = 2 \Rightarrow$ 

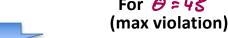
(C.H.S.H. inequality)

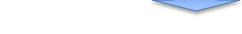
Quantum **Mechanics** 

$$\alpha = \sigma^{(\alpha)} \cdot \vec{\alpha}$$
  $\beta = \sigma^{(\alpha)} \cdot \vec{\beta}$ 

$$\alpha' = \nabla^{(A)} \cdot \overline{\alpha}^{(B)} \cdot \overline{b}^{(B)}$$







$$|\langle ab \rangle + \langle a'b \rangle + \langle ab' \rangle - \langle a'b' \rangle| = \frac{4}{\sqrt{2}} = 2\sqrt{2} > 2$$

- violates C.H.S.H. inequality

### **Laboratory Experiment (Aspect, many others)**

