

# OPTI 646

## Introduction to Quantum Information and Computation

This course covers the Foundations of Quantum Information Science and selected topics in Quantum Communication and Quantum Computation, including physical implementations.

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**Text:** "Quantum Information and Computation", lecture notes by John Preskill, Caltech 1998.

Send me an email after the first lecture to ensure I get you in my mailing list, and I will respond by sending you a PDF copy.

**Course Website:** <https://wp.optics.arizona.edu/opti646/>

**Lectures:** Meinel 305, Tuesdays and Thursdays 2-3:30pm

**Office Hours:** Meinel 604, Wednesdays 2-3:30pm  
If you give me a heads-up beforehand, I can usually find time for a chat outside office hours.

**Note:** OPTI 646 is taught in a live, in-person format. Video and slides from the lectures will be posted on the course website, but these recordings are not meant to substitute for live attendance.

**Grading:** Homework (30%), Student Presentation or Term Paper (40%), and class participation (30%).

In place of exams, each student is required to give a Lecture or submit a Term Paper on a topic related to Quantum Information Science.

**Prerequisites:** A solid knowledge and understanding of graduate level quantum mechanics is essential, as developed in, for example, OPTI/PHYS 570A "Quantum Mechanics", or equivalent. The course uses the notation and conceptual language of the "Cohen-Tannoudji school of quantum mechanics", adapted in the OPTI 570/544/646 series of graduate level courses.

# Topics

## **Introduction and overview**

Physics of Information, Quantum Computation  
Quantum parallelism, Deutsch's problem  
Quantum Error Correction  
Quantum Hardware: Ions, atoms, Superconductors, Photons and more

## **Review of quantum mechanics I - basics**

State vectors, Linear operators, Observables, Unitary Operators  
Postulates of Quantum Mechanics

## **Review of quantum mechanics II – bipartite systems**

Tensor Product of State Spaces and Operators  
Measurements on one Part of a System  
Density operator, Separate Description of part of a System, Partial trace  
Bayes Rule and the Updating of Probabilities, Collapse of the Wavefunction

## **Qubits, Spin-1/2 and other 2-Level Systems**

Spin State Space, Entangled States, Observables, Pauli Matrices  
Pure states, Density operator, Bloch picture.

## **Entanglement**

2 Spins, EPR States, Local Measurements and Correlations  
Sending Non-Orthogonal States, Significance of Ensemble Decomposition, Local Hidden Variable Theories, Bell Inequalities, Clauser-Horne-Shimony-Holt Inequality

## **Quantum Communication**

Information in entangled pairs, Dense Coding  
Quantum key distribution, Security against eavesdroppers, No cloning theorem, Quantum teleportation

## **General Theory of Measurement**

Von Neumanns Theory of Orthogonal Measurement, System-Meter Model,  
Non-orthogonal Measurements, POVM's  
Implementation as Orthogonal Measurement in Extended State Space

## **Open Quantum Systems**

Evolution and Decoherence, Operator-sum representation, Kraus operators, Super-Operators, Decohering Quantum Channels, Depolarizing, Phase & Amplitude Damping

## **Classical & Quantum Information Theory**

Shannon for Dummies. Shannon Entropy, Data Compression. Channel Capacity,  
Joint and Conditional Entropy, Mutual Information. Quantum Data Compression.

## **Quantum Computation**

Classical Circuits, Universal Gates, Circuit Complexity.  
Quantum Circuits, Universal Quantum Gates. Quantum Circuit Complexity,  
Complexity Hierarchy.

# **Student Lectures and Term Papers 2002 - 2023**

## **Student Lecture/Term Paper Topics 2002 (7)**

EPR and GHZ, loopholes

Quantum teleportation

Quantum communication and quantum cryptography Neutral atom quantum computation – optical lattices Slow light and quantum data storage

Quantum games

Quantum measurement – QND and POVM

## **Student Lecture/Term Paper Topics 2005 (6)**

Quantum Computing with Ion Traps Quantum Data Storage in Ensembles Quantum Algorithms

Quantum Key Distribution

Solid State Implementations of Quantum Computation Classical Wave Simulations of QM

## **Student Lecture/Term Paper Topics 2008 (14)**

EPR experiments

Quantum Non-Demolition Measurements

Quantum State Reconstruction

Public Key Cryptography and the RSA cryptosystem

Slow light and quantum data storage

Quantum teleportation

Ion trap quantum computation

Linear optics quantum computation

Solid state implementations of quantum computation

Robust quantum control of qubits

Quantum simulation of model Hamiltonians

Shor's algorithm for factoring

Topological quantum computing

Quantum Information Theory - Holevo Information, Accessible Information

## **Student Lecture/Term Paper Topics 2010 (9)**

EPR experiments

Quantum Non-Demolition measurements

Quantum State Reconstruction

Quantum Metrology

Public Key Cryptography and the RSA cryptosystem

Slow Light and Quantum Data Storage

Ion Trap Quantum Computation

Grovers Algorithm for Data Base Search

Quantum Trajectories and Quantum Monte Carlo Simulation

## **Student Lecture/Term Paper Topics 2012 (7)**

Quantum Non-Demolition measurements Spin Squeezing

Weak Values in Quantum Measurement Quantum Cryptography

Grovers Algorithm

Adiabatic Quantum Computing Quantum Simulation in Chemistry

### **Student Lecture/Term Paper Topics 2015 (4)**

Quantum non-demolition measurements, Superoperators and decoherence  
Dynamical decoupling and composite pulses Measurement based one-way quantum computation

### **Student Lecture/Term Paper Topics 2018 (5)**

Quantum Repeaters  
Surface Code Quantum Computing Grovers Algorithm  
Quantum Tomography  
Squeezed States

### **Student Lecture/Term Paper Topics 2020 (13)**

Frequency Combs and Quantum Computation  
Overview of Quantum Gates for Ion Trap Quantum Computers  
Quantum Non-Demolition Measurements in Quantum Optomechanics  
GHZ States and Tests of LVH Theories  
Quantum Neural Networks  
Continuous Measurement and Quantum Control  
Analog vs Digital Simulation and the Effects of Trotterization  
Variational Quantum Eigensolver (VQE)  
Quantum Metrology: Quantum Fisher Information and Estimation Strategies Quantum Memory:  
A Review  
Shor's Algorithm  
A Review of Quantum Error Correction of a Qubit Encoded in Grid States Quantum Error  
Correction Codes

### **Student Lecture/Term Paper Topics 2022 (15) Quantum Annealing**

Blind Quantum Computation  
Measurement Based and Delegated QC Topological QC  
Optical Computing with CV Cluster States Semiconductor Spin Qubits  
Qubits in Harmonic Oscillators  
Quantum Fisher Information and Cramer Rao Bounds Quantum Neural Networks  
Optical Coherent State Discrimination  
Quantum Causality  
Gaussian Boson Sampling  
Survey of Optical Quantum Computing  
Quantum Acoustics and Quantum Control  
Quantum Key Distribution

### **Student Lecture/Term Paper Topics 2024 (15)**

Quantum Annealing Error Correction  
Quantum Communication Networks  
Superconducting Implementations of QC  
Semiconductor Spin Qubits  
QKD with 3-Outcome POVM  
Nanomechanical Systems in QIS  
Quantum Decoherence  
Quantum Gates in Ion Traps