John von Neumann

Physics of Information: Alan Turing

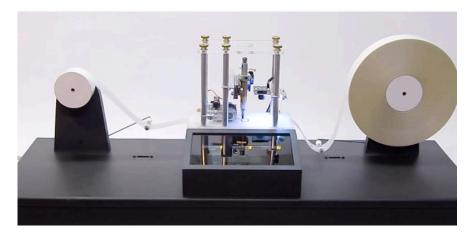
Notions: What is a computation?

What is computable

Formulation of Computer Science that is Device Independent



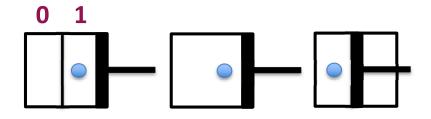
1937 Turing Machine:



https://www.youtube.com/watch?v=E3keLeMwfHY

Landaur: Information is Physical!

Example: Erasure = Dissipation



Entropy: $\triangle S_{gas} = - \log \ln 2$

Work: $W = kT \ln 2 = 0.96 \times 10^{-23} \frac{J}{K} \cdot 300 K$ $\sim 3 \times 10^{-21} J \sim 0.02 eV$

Is there a way around it?

Reversible Computation!

But we need a different gate set!

John von Neumann Alan Turing

Wikipedia:

A Turing Machine (TM) is a mathematical model of computation describing an abstract machine that manipulates symbols on a strip of paper according to a table of rules.

The TM operates on an infinite tape divided into cells, each of which can hold a symbol drawn from a finite set.

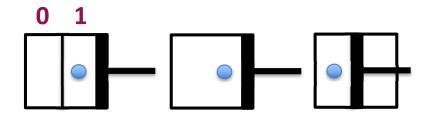
At each step the head reads the symbol in the cell. Then, based on the symbol and the TM's present state, the machine writes a symbol in the cell, and moves the head one step to the left or the right, or halts the computation.

Church – Turing Thesis:

Everything that is computable can be computed on a Turing Machine with at most polynomial overhead.

Landaur: Information is Physical!

Example: Erasure = Dissipation



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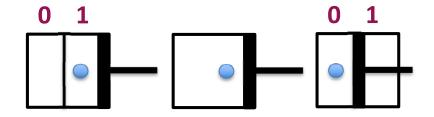
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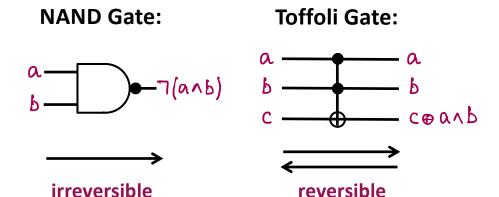
Work:
$$W = \&T \ln 2 = 0.96 \times 10^{-13} \frac{J}{K} \cdot 300 K$$

 $\sim 3 \times 10^{-21} J \sim 0.09 \text{ eV}$

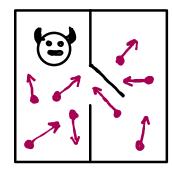
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Maxwells Demon:

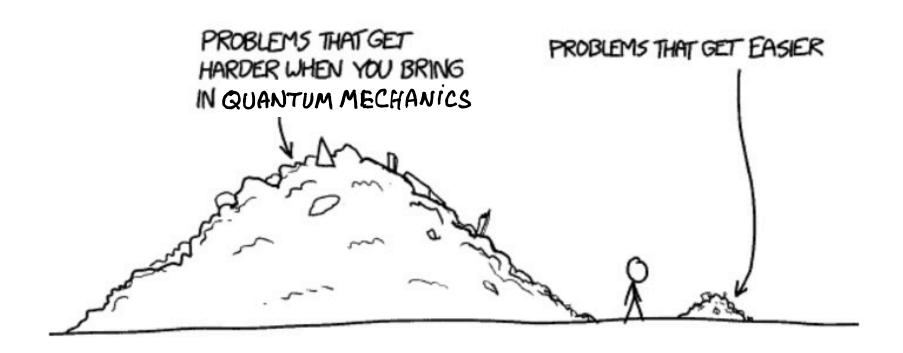


Information is Physical!

Quantum Information

Carl Caves: Quantum States are states of knowledge

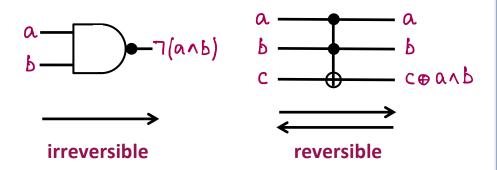
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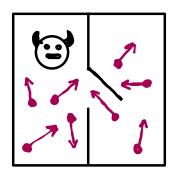
Source: xkcd.com

NAND Gate:

Toffoli Gate:



Maxwells Demon:



Information is Physical!

Quantum Information

Carl Caves:

Quantum States are states of knowledge

Physics is Information!

New properties of QM

Measurement:



Acquire Info | Disturb system

Randomness:

Outcome fundamentally unpredictable

"Collapse" of wavefunction

Cannot determine state of a quantum system if initially unknown

Cannot Copy No cloning theorem

pure state, entangled

Entanglement:

 $|70\rangle = \frac{1}{\sqrt{2}} (|100\rangle + |11\rangle)$

Non-local correlations

 $g = \frac{1}{2} \left(\left[\cos X \cos \right] + \left[11 \times 11 \right] \right)$

mixed state, not entangled

Quantum Computing

Does QM impact Computation?

Peter Shor (1994): YES! Quantum
Fourier
Transform

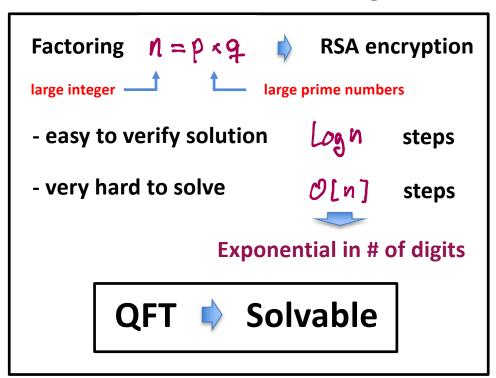


Factoring!

DFT on N bits $\mathcal{O}[(2^N)^2]$ steps

FFT on u $\mathcal{O}[N2^N]$ uQFT on u $\mathcal{O}[NLogN]$ u

Efficient Factoring



Preskill Ch. 1, p. 5-6 $T \propto e^{1.9 (\log n)^{1/3}} e^{(\log \log n)^{2/3}}$ Best Classical Algorithm

Quantum Computing

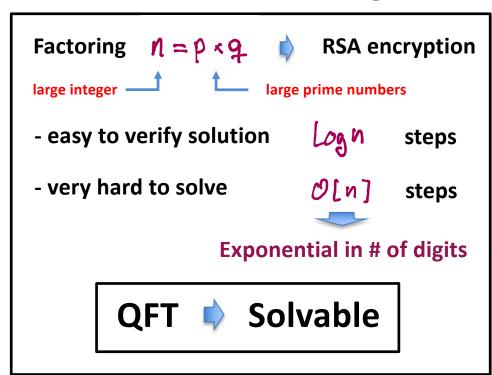
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Preskill Ch. 1, p. 5-6 $T \propto e^{1.9 ((\log n)^{1/3}} e^{((\log \log n)^{2/3}}$ (1998) 130 digits in 1 month 400 digits in 10¹⁰ years (2022) 24 yrs = 16 Moores Law doublings $2^{16} = 65,536 \implies 400 \text{ digits} \approx 150 \text{kYrs}$

Quantum Computing

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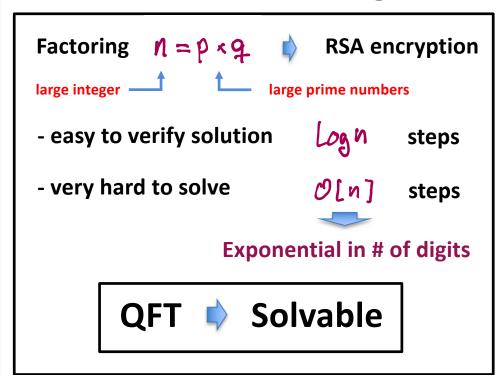


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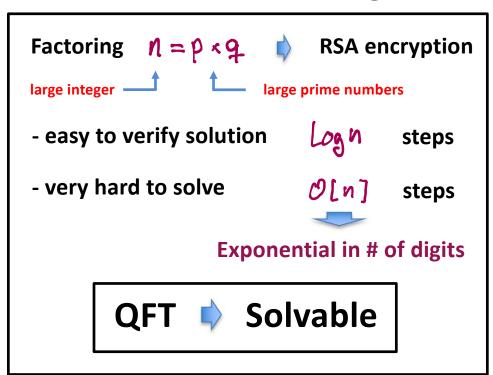
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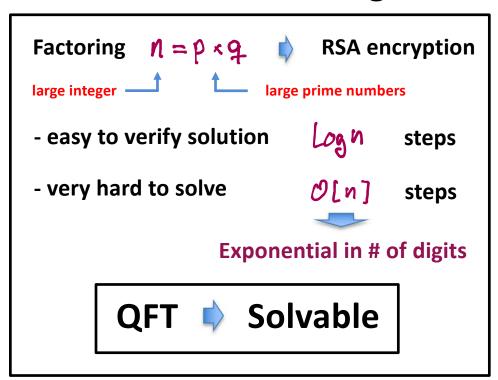
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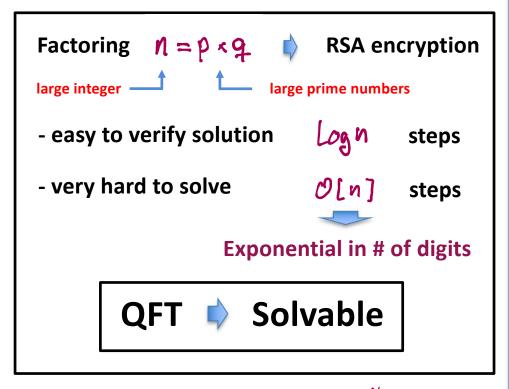


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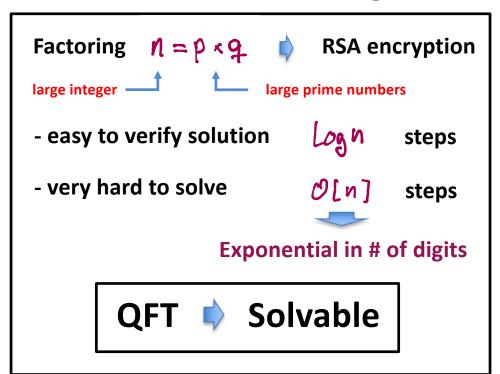
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Quantum Complexity

Efficient Factoring

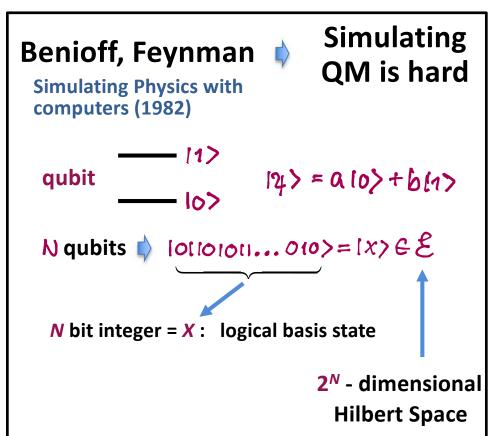


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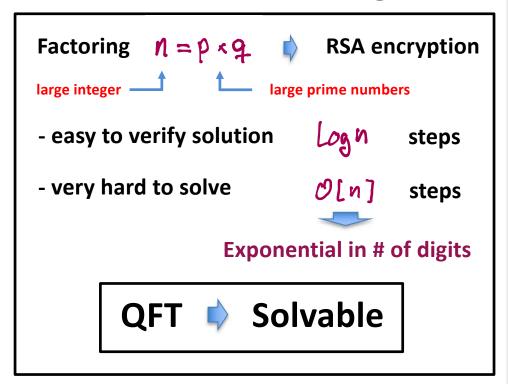
Quantum Complexity



General State:

$$|z\rangle = \frac{1}{2^{N/2}} \sum_{x=0}^{2^{N-1}} a_x |x\rangle$$

Efficient Factoring



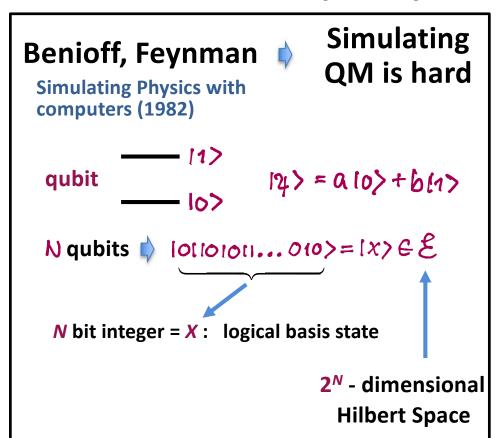
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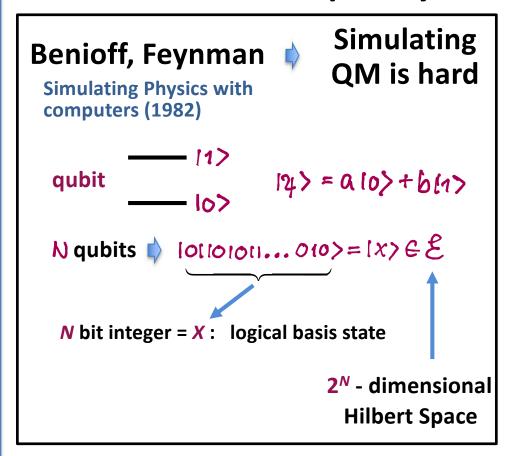
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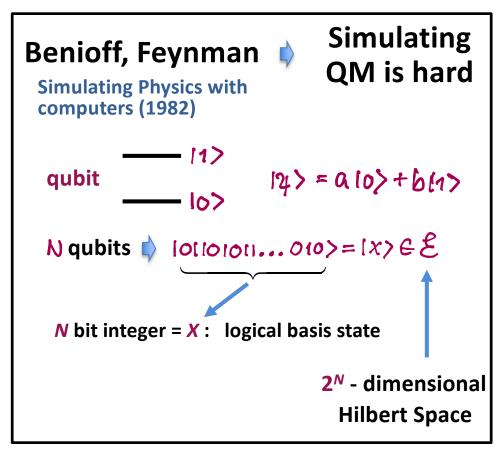
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Quantum Complexity



General State:

$$|7\rangle = \frac{1}{2^{N/2}} \sum_{x=0}^{2^{N-1}} a_x |x\rangle$$

Simulating Physics with Computers

Richard P. Feynman

Department of Physics, California Institute of Technology, Pasadena, California 91107

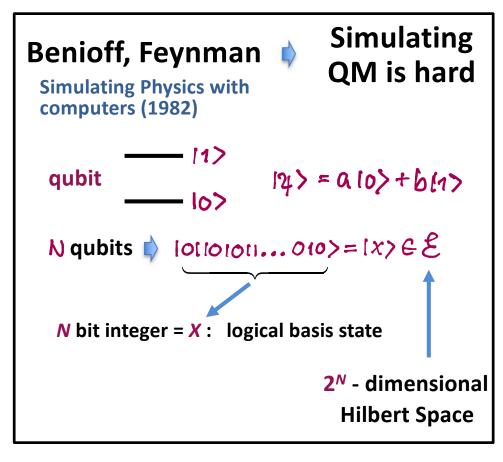
Received May 7, 1981

1. INTRODUCTION

On the program it says this is a keynote speech—and I don't know what a keynote speech is. I do not intend in any way to suggest what should be in this meeting as a keynote of the subjects or anything like that. I have my own things to say and to talk about and there's no implication that anybody needs to talk about the same thing or anything like it. So what I want to talk about is what Mike Dertouzos suggested that nobody would talk about. I want to talk about the problem of simulating physics with computers and I mean that in a specific way which I am going to explain. The reason for doing this is something that I learned about from Ed Fredkin, and my entire interest in the subject has been inspired by him. It has to do with learning something about the possibilities of computers, and also something about possibilities in physics. If we suppose that we know all the physical laws perfectly, of course we don't have to pay any attention to computers. It's interesting anyway to entertain oneself with the idea that we've got something to learn about physical laws; and if I take a relaxed view here (after all I'm here and not at home) I'll admit that we don't understand everything.

The first question is, What kind of computer are we going to use to simulate physics? Computer theory has been developed to a point where it realizes that it doesn't make any difference; when you get to a *universal computer*, it doesn't matter how it's manufactured, how it's actually made. Therefore my question is, Can physics be simulated by a universal computer? I would like to have the elements of this computer *locally interconnected*, and therefore sort of think about cellular automata as an example (but I don't want to force it). But I do want something involved with the

Quantum Complexity



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1st Reading Assignment

Read as much as you feel like, but don't get bogged down in the details.

Focus on Chapters 4 & 5 and summarize margins

in a few bullet points, no more than a half page, 12pt font, single line spacing, 1 inch

The first question is, What kind of computer are we going to use to simulate physics? Computer theory has been developed to a point where it realizes that it doesn't make any difference; when you get to a universal computer, it doesn't matter how it's manufactured, how it's actually made. Therefore my question is, Can physics be simulated by a universal computer? I would like to have the elements of this computer locally interconnected, and therefore sort of think about cellular automata as an example (but I don't want to force it). But I do want something involved with the

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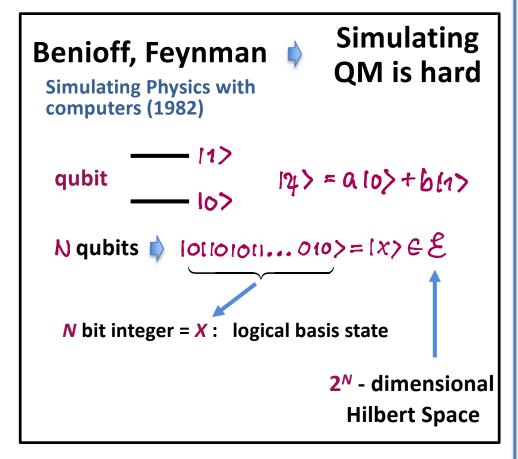
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Quantum Complexity



Quantum Computation

Computation is a map

Schrödinger Evolution

$$i \pi \frac{dU}{dt} = HU$$
 given enough memory & time we can find U

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Quantum Computation

- * A classical computer can simulate a QC
- * Notion of computability unchanged

Simulation is <u>hard</u>:

$$N = 100 \rightarrow 2^{100} \sim 10^{30}$$
 p.a.'s

$$N = 300 \Rightarrow 2^{900} \sim 10^{90}$$
 p.a.'s

10⁹⁰ >> # of particles in the visible universe

Jeff Kimble: Hilbert Space is a mighty big place

Quantum Computation

- * A classical computer can simulate a QC
- Notion of computability unchanged

Simulation is hard:

N qubits 2^N prob. amp.'s

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10⁹⁰ >> # of particles in the visible universe

Jeff Kimble: Hilbert Space is a mighty big place

- * Is it possible for a classical computer to efficiently simulate QM?
- * Use probabilistic local algorithm (the most general kind)

John Bell

Bell's Theorem:

No local probabilistic theory can reproduce all of QM

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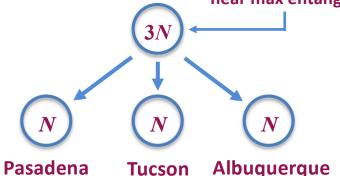
No local probabilistic theory can reproduce all of QM

Non-Local Correlations

Key to Quantum Information

Thought experiment:

Generic Pure State in 2^{3N} dimensional space near max entangled



Local state close to random

Shannon Info
$$S = -\sum_{i=1}^{2^{N}} \rho_{i} \log \rho_{i}$$
Von Neuman Info
$$S = -\text{Tr} \left[\Im \log \Im \right]$$

$$\text{entropy}$$

$$\text{max value of } S$$

$$\sim N - 2^{-(N+l)}$$

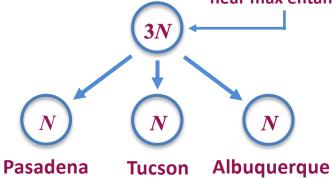
Almost all info in *N* - body state in Non-Local correlations

Non-Local Correlations

Key to Quantum Information

Thought experiment:

Random Pure State in 2^{3N} dimensional space near max entangled



Local state close to random

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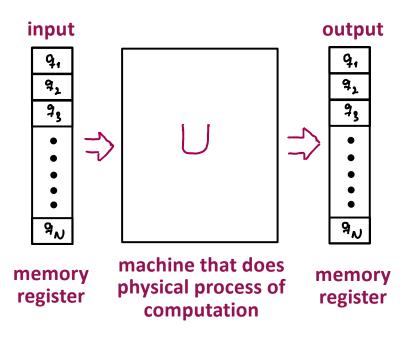
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Almost all info in N - body state in Non-Local correlations

OK – Plausible QM can do more Where does the QC's power come from?

Visualization of Computation

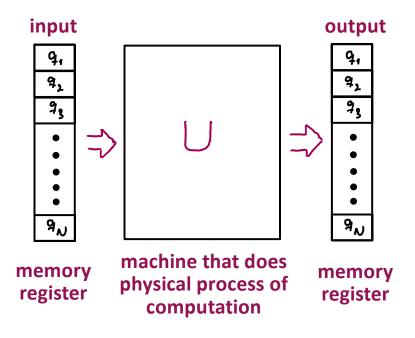


Classical: Register is in one of the logical states

Reversible transformation

OK – Plausible QM can do more Where does the QC's power come from?

Visualization of Computation



Classical: Register is in one of the logical states

Reversible transformation

Quantum: Register can be in any coherent superposition of logical states [x>

Unitary transformation U: I×>→ ly>

Maps basis to basis $U: \{1\times\} \rightarrow \{1y\}$

Quantum Parallelism

$$|2i_{in}\rangle \rightarrow \sum_{x} a_{x}|_{x}\rangle \rightarrow |$$

$$\rightarrow |2i_{out}\rangle = \bigcup |2i_{in}\rangle = \sum_{x} a_{x}|_{3}\rangle = \sum_{x} b_{x}|_{x}\rangle$$

Machine processes 2^N inputs "in parallel"!

Beware: measurement collapses Q. Register into a single basis state at random

We get one random result out of 2^N

Quantum: Register can be in any coherent superposition of logical states (x>

Unitary transformation U: <a>!५> <a>!५>

Maps basis to basis $U: \{l \times \} \rightarrow \{l \neq \}$

Quantum Parallelism

Quantum Sampling

Problem

$$|\mathcal{V}_{in}\rangle \rightarrow \sum_{x} a_{x}|_{x}\rangle \rightarrow |\mathcal{V}_{in}\rangle = \sum_{x} a_{x}|_{\eta}\rangle = \sum_{x} b_{x}|_{x}\rangle$$

Machine processes 2^N inputs "in parallel"!

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Quantum Algorithms look for global properties of functions — symmetry, periodicity, etc.

- * Classical -> requires many function evaluations
- Quantum -> design U so measurement gives answer with high probability
- * \exists classes of problems (sampling problems)

 which are classically hard but quantum "easy"

 Google "Quantum Supremacy"

Expert insight into current research

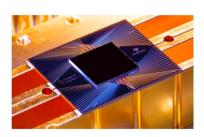
News & views

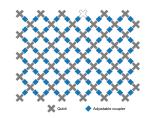
Quantum information

Quantum computing takes flight

William D. Oliver

A programmable quantum computer has been reported to outperform the most powerful conventional computers in a specific task – a milestone in computing comparable in importance to the Wright brothers' first flights. See p.505





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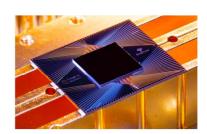
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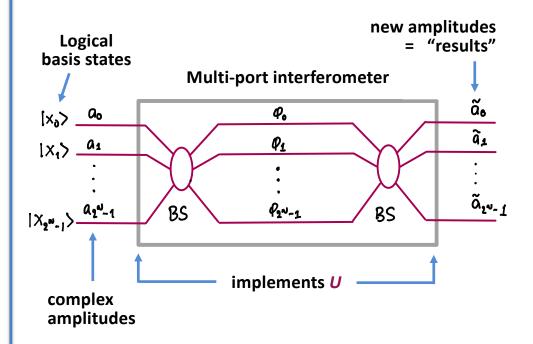
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What might be inside the machine?

Wave interference w/classical fields?



Note: N - qubit register | → 2^N "paths"

Beware of Resource Scaling!

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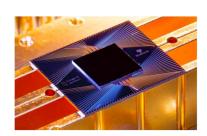
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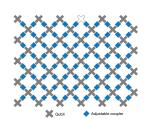
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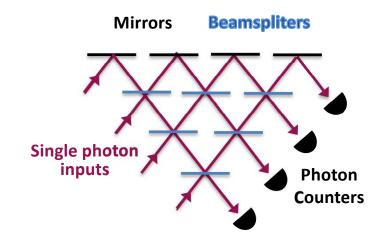
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Boson Sampling

An example from Optics/Photonics
Setup



Beware: Boson behavior at Beamsplitters hard to predict photon statistics across outputs.

Exponential in #'s of Beamsplitters

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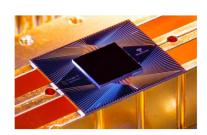
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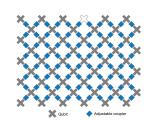
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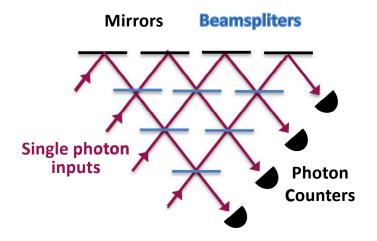
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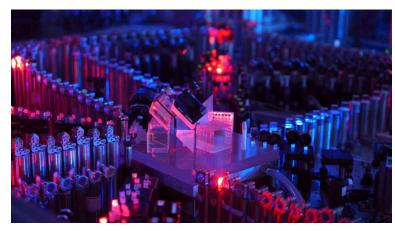




Boson Sampling

An example from Optics/Photonics Setup





An optical quantum computer developed by a team of Chinese researchers including those from the University of Science and Technology of China. (courtesy of Han-Sen Zhong of the research group)

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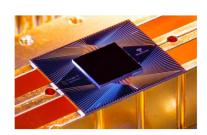
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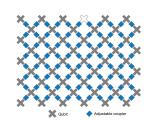
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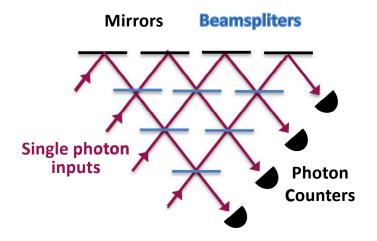
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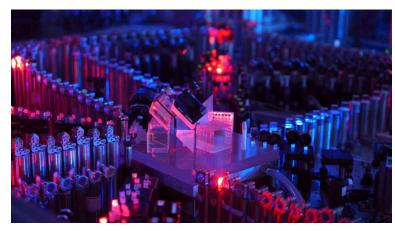




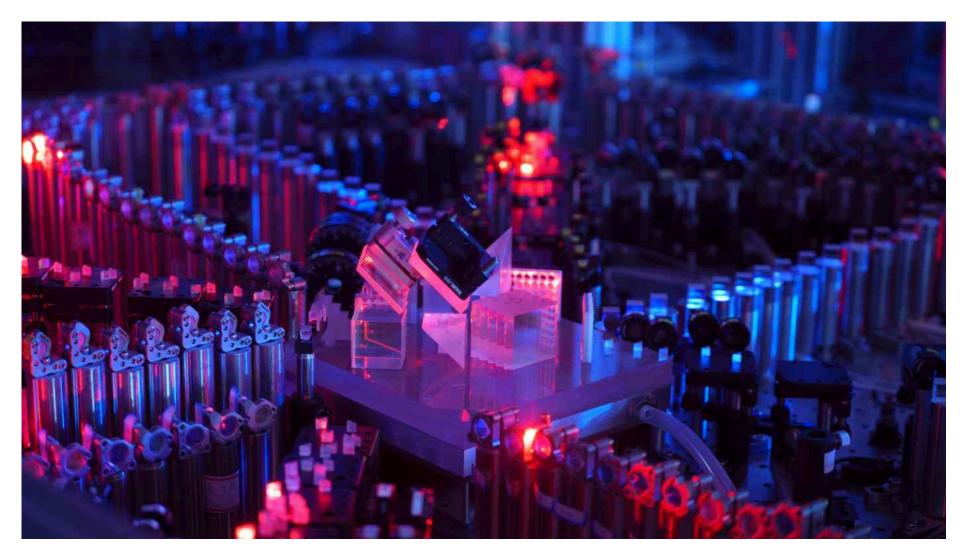
Boson Sampling

An example from Optics/Photonics Setup

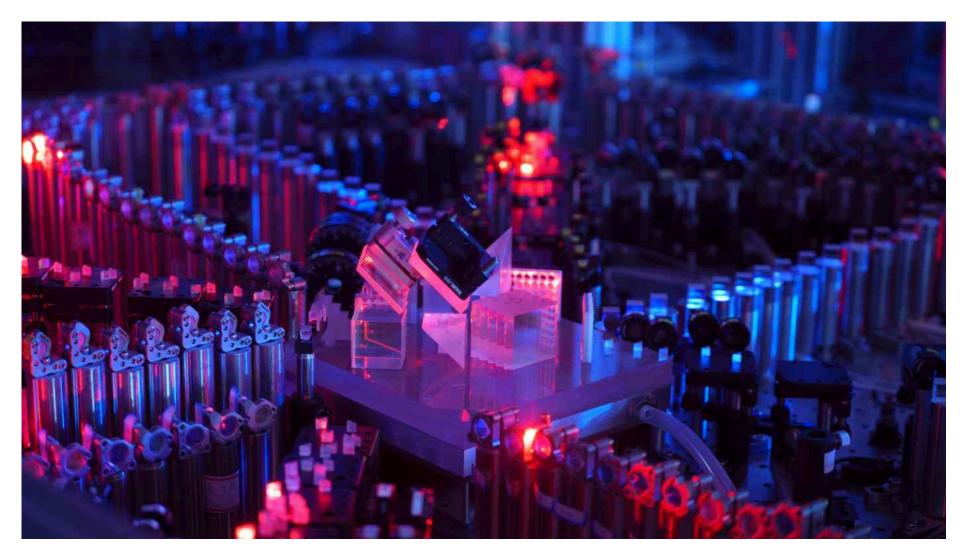




An optical quantum computer developed by a team of Chinese researchers including those from the University of Science and Technology of China. (courtesy of Han-Sen Zhong of the research group)



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Quantum Algorithms look for global properties of functions — symmetry, periodicity, etc.

- * Classical prequires many function evaluations
- ★ Quantum design U so measurement gives answer with high probability
- * declasses of problems (sampling problems)

 which are classically hard but quantum "easy"

 Google "Quantum Supremacy"

Expert insight into current research

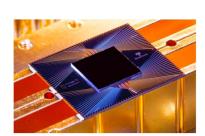
News & views

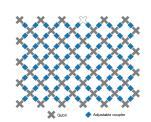
Quantum information

Quantum computing takes flight

William D. Oliver

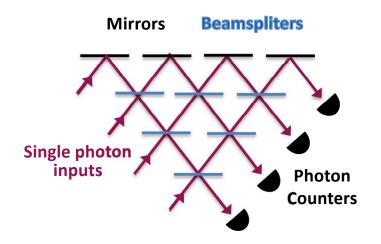
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Boson Sampling

An example from Optics/Photonics
Setup



Imagine aligning that thing...!