Overview of Aberrations

Lens Design OPTI 517

Aberration

From the **Latin**, aberrare, to wander from; **Latin**, ab, away, errare, to wander.

Symmetry properties

Overview of Aberrations (Departures from ideal behavior)

- Basic reasoning
- Wave aberration function
- Aberration coefficients
- Comments
- Aspheric contributions
- Stop shift
- Bending a lens

Wavefront

• Ideally wavefronts and rays converge to Gaussian image points. This implies that ideally wavefronts must be spherical and rays must be homocentric.

- • Actual image degradation by an optical system implies that the collinear transformation can not model accurately imaging. In the wave picture for light propagation we notice that wavefronts must be deformed from the ideal spherical shape.
- • Wavefront deformation is determined by the use of a reference sphere with center at the Gaussian image point and passing by the exit pupil on-axis point.

 \bullet An axially symmetric system can only have an axially symmetric wavefront deformation for an object point on-axis. In its simplest form this deformation can be quadratic or quartic with respect to the aperture. If the reference sphere is centered in the Gaussian image point then the quadratic deformation can not be present for the design wavelength.

 \bullet For an object point that is off-axis the axial symmetry of the beam is lost and is reduced to plane symmetry. Therefore for that off-axis beam the wavefront deformation can have axial, plane, or double plane symmetry.

- • The simplest plane symmetric wavefront deformation shapes represent the primary aberrations. These are:
- •Spherical aberration Axially symmetric
- \bullet
- •
- •
- •
- •
- •chromatic
- •
- •chromatic

Coma Plane symmetric Astigmatism Double plane symmetric Field curvature **Axially symmetric** Distortion **Plane symmetric** Longitudinal **Axially symmetric**

Lateral **Exercise Example 2** Plane symmetric

Aberration forms: symmetry considerations

Distortion

Field curvatureFocus

Astigmatism

Coma

Spherical aberration

Focus

Spherical

aberration

On-axis

Wave aberration function

 \bullet The wave aberration function is a function of the field H and aperture ρ vectors. Because this function represents a scalar, which is the wavefront deformation at the exit pupil, it depends on the dot product of the field and aperture vectors. The assumed axial symmetry leads to a select set of terms.

$$
W\{H,\rho\} = \sum_{j,m,n} W_{k,l,m} H^k \rho^l \cos^m \theta
$$

$$
W(H, \rho, \theta) = W_{200}H^2 + W_{020}\rho^2 + W_{111}H\rho\cos\theta + W_{040}\rho^4 + W_{131}H\rho^3\cos\theta + W_{222}H^2\rho^2\cos^2\theta + W_{220}H^2\rho^2 + W_{311}H^3\rho\cos\theta + W_{400}H^4 + \dots
$$

Wave aberration function

 \bullet The field vector has its foot at the center of the image plane and the aperture vector has its foot at the center of the exit pupil. Both are normalized

Wave aberration function

• Note that defocus W020 and the change of scale W111 terms are not needed because Gaussian optics accurately predict the location and size of the image. The piston terms W200 and W400 represent a constant phase change that does not degrade the image.

Summary of primary aberrations

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$$
\delta \lambda W_{020} = \frac{1}{2} C_L \qquad \delta \lambda W_{111} = C_T
$$

$$
C_L = \sum A y \Delta \left(\frac{\delta n}{n}\right) \qquad C_T = \sum \overline{A} y \Delta \left(\frac{\delta n}{n}\right)
$$

$$
A = nu + nyc = ni
$$

\n
$$
\overline{A} = n\overline{u} + n\overline{y}c = n\overline{i}
$$

\n
$$
K = n\overline{u}y - nu\overline{y} \qquad c = \frac{1}{r} \qquad P = c\Delta(1/n)
$$

\n
$$
\Delta\left(\frac{\delta n}{n}\right) = \frac{n-1}{n\nu} \qquad \nu = \frac{n_d - 1}{n_F - n_C}
$$

 \cancel{K} is the Lagrange invariant.

- c is the surface curvature, v is the v number or reciprocal dispersive power.
- All with the marginal and chief ray paraxial ray traces !!!
- Lens optimization started!!!

Comments on aberrations

- •Third-order or fourth-order ?
- • A well corrected system has its third-order aberrations almost zero
- • Aberration cancellation is the main mechanism for image correction
- • Presenting to the optimization routine a system with its third-order aberrations corrected is a good starting point
- • Some simple systems are designed by formulas that relate third-order aberrations
- •Note symmetry in third-order aberration coefficients
- \bullet Wave aberrations seem to be simpler to understand than transverse ray aberrations

Example

Example

Summary of aberrations

Aspheric surfaces

$$
Z(S) = \frac{cS^2}{1 + \sqrt{1 - (K + 1)c^2 S^2}} + A_4 S^4 + A_6 S^6 + A_8 S^8 + A_{10} S^{10} + \dots
$$

$$
S^2 = x^2 + y^2
$$

C is 1/r where r is the radius of curvature; K is the conic constant; A's are aspheric coefficients

Aspheric contribution can be thought of as a cap to the spherical part

Aspheric contributions I

- \equiv $\delta C_{L}^{}=0$
- $\delta C_{T}^{}=0$

$$
= \left(\frac{b}{y}\right) a \qquad a = -\varepsilon^2 c^3 y^4 \Delta n
$$

$$
a = 8A_4 y^4 \Delta n
$$

Aspheric contributions II

The surface sag is: $Z = A_4 y^4$ and the wavefront deformation is: $W_{040} = (n'-n) \cdot A_4 y^4$

For off-axis beams y becomes $y + \Delta \overline{y}$ or $y + \overline{y}$ and therefore:

 y^4 becomes $(y+\bar{y})^4 = (y^2 + 2y\bar{y} + y^2) \cdot (y^2 + 2y\bar{y} + \bar{y}^2) =$

$$
= y^4 \left\{ 1 + 4\frac{\overline{y}}{y} + 4\left(\frac{\overline{y}}{y}\right)^2 + 2\left(\frac{\overline{y}}{y}\right)^2 + 4\left(\frac{\overline{y}}{y}\right)^3 + \left(\frac{\overline{y}}{y}\right)^4 \right\}
$$

The terms in the brackets represent spherical, coma, astigmatism, field curvature, distortion, and piston.

Aspheric contributions III

•When the stop is at the aspheric surface only spherical aberration is contributed given that all the beams see the same portion of the surface •When the stop is away from the surface, different field beams pass through different parts of the aspheric surface and other aberrations are contributed Prof. Jose Sasian **College of Optical Sciences**

Stop Shifting

•Stop shift is a change in the location of the aperture stop along the axis

- •Stop shift does not change the f/#
- •Stop shift select a different portion of the wavefront fro off-axis beams

Stop shifting

Stop Shift

Wave coefficients in terms of Seidel sums

I $W_{040} = -S$ 1 040 Ξ *II* $W_{131} = -S$ 1 131 \equiv *III* $W_{222} = -\frac{1}{2}S$ 1 222 Ξ $\sum_{220} = \frac{1}{4} (S_{III} + S_{IV})$ 1 4 $W_{220} = -\frac{1}{4}(S_{III} + S_{IV})$ *V* $W_{311} = -S$ 1 311 \equiv

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The ratio
$$
\frac{\delta \bar{y}}{y}
$$

Can be calculated at any plane in the optical system

$$
\overline{S} = \frac{\overline{u}_{new} - \overline{u}_{old}}{u} = \frac{\overline{y}_{new} - \overline{y}_{old}}{y} = \frac{\overline{A}_{new} - \overline{A}_{old}}{A}
$$

 S is the stop shifting parameter

Structural coefficients σ

$$
S_{I} = \frac{1}{4} y_{p}^{4} \phi^{3} \sigma_{I}
$$

$$
S_{II} = \frac{1}{2} \mathcal{K} y_{p}^{2} \phi^{2} \sigma_{II}
$$

$$
S_{III} = \mathcal{K}^{2} \phi \sigma_{III}
$$

$$
S_{IV} = \mathcal{K}^{2} \phi \sigma_{IV}
$$

$$
S_V = \frac{2 \mathcal{K}^3}{y_p^2} \sigma_V
$$

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$$
C_T = 2 \, \mathcal{K} \sigma_T
$$

 $C_L = y_p^2 \phi \sigma_L$

 y_p

Marginal ray height at the principal planes

Structural coefficients: Thin lens (stop at lens)

$$
S_{I} = \frac{1}{4} y^{4} \phi^{3} [AX^{2} - BXY + CY^{2} + D]
$$
\n
$$
S_{II} = \frac{1}{2} \mathcal{K} y^{2} \phi^{2} [EX - FY]
$$
\n
$$
S_{II} = \mathcal{K}^{2} \phi
$$
\n
$$
S_{IV} = \mathcal{K}^{2} \phi
$$
\n
$$
S_{IV} = \mathcal{K}^{2} \phi \frac{1}{n}
$$
\n
$$
S_{V} = 0
$$
\n
$$
S_{V} = 0
$$
\n
$$
S_{V} = \frac{1 + m}{1 - m} = \frac{u' + u}{u' - u}
$$
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S_{V} = 0
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S_{V} = 0
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S_{V} = \frac{1 + m}{1 - m} = \frac{u' + u}{u' - u}
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$$
S_{V} = \frac{1 + m}{1 - m} = \frac{u' + u}{u' - u}
$$
\n
$$
S_{V} = \frac{n^{2}}{n}
$$
\n
$$
S_{V} = \frac{n^{2}}{n}
$$
\n
$$
S_{V} = \frac{1 + m}{1 - m} = \frac{u' + u}{u' - u}
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$$
S_{V} = \frac{n^{2}}{n}
$$
\n
$$
S_{V} = \frac{n^{2}}{n}
$$
\n
$$
S_{V} = \frac{3n + 2}{n}
$$
\n
$$
S_{V} = \frac{3n + 2
$$

Surface optical power φ

Bending a lens

- Maintains the optical power
- Changes the optical shape
- Meniscus, planoconvex, doubleconvex, etc.
- Shape factor

$$
X = \frac{c_1 + c_2}{c_1 - c_2} = \frac{r_2 + r_1}{r_2 - r_1}
$$

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Using a lens design program

- • Must be able to interpret correctly the information displayed by the program
- • In some instances the program is right but we think it is wrong. So we must carefully review our assumptions
- • When there is disagreement between you an the program, there is an opportunity to learn
- •Verify that the program is modeling what you want
- •Check and double check
- •You must feel comfortable when using a program.
- •Read the manual
- • Play with the program to verify that it does what you think it does
- Prof. Jose Sasian • Must reach the point when it is actually fun to use the program

Summary

- Review of aberrations
- Aspheric surfaces
- Stop shifting
- Aberration coefficients
- Using a lens design program
- Next class derivation of coefficients

Mode matching concept

- Same mode diameter
- Same amplitude distribution
- Same phase distribution
- Same polarization
- Same x,y,z position
- Same angular position

Fiber coupling efficiency

"overlap integral"

 $\bar{m}(x)$ $\Psi_m^*(x)dx$ $+\infty$ \ast $-\infty$

Herwig Kogelnik

