Coma aberration

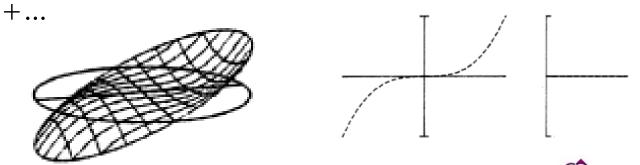
Lens Design OPTI 517



Coma

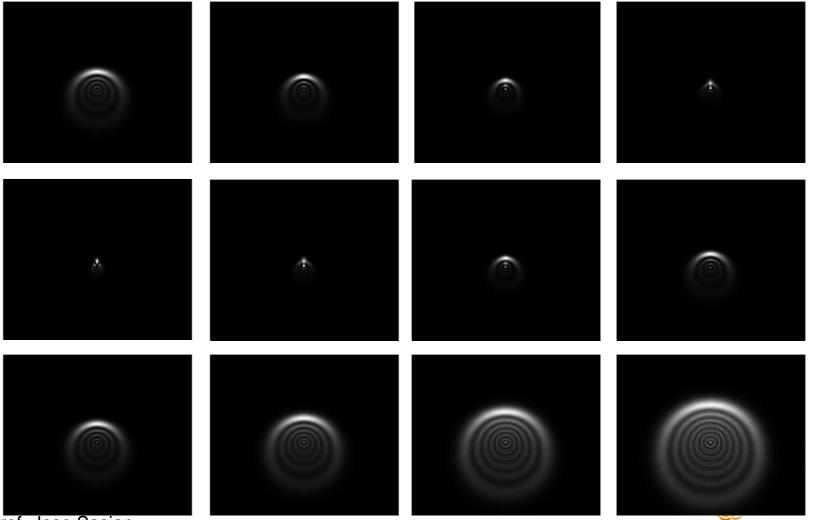
0.25 wave	1.0 wave	2.0 waves	4.0 waves	Spot diagram
•	•	*		

 $W(H, \rho, \theta) = W_{200}H^{2} + W_{020}\rho^{2} + W_{111}H\rho\cos\theta + W_{040}\rho^{4} + W_{131}H\rho^{3}\cos\theta + W_{222}H^{2}\rho^{2}\cos^{2}\theta + W_{220}H^{2}\rho^{2} + W_{311}H^{3}\rho\cos\theta + W_{400}H^{4} + W_{220}H^{2}\rho^{2} + W_{311}H^{3}\rho\cos\theta + W_{400}H^{4} + W_{40}H^{4} + W_{40}H^{4}$



College of Optical Sciences

Coma though focus



College of Optical Sciences

Cases of zero coma

$$W_{131} = -\frac{1}{2}A\overline{A}\Delta\left\{\frac{u}{n}\right\}y$$

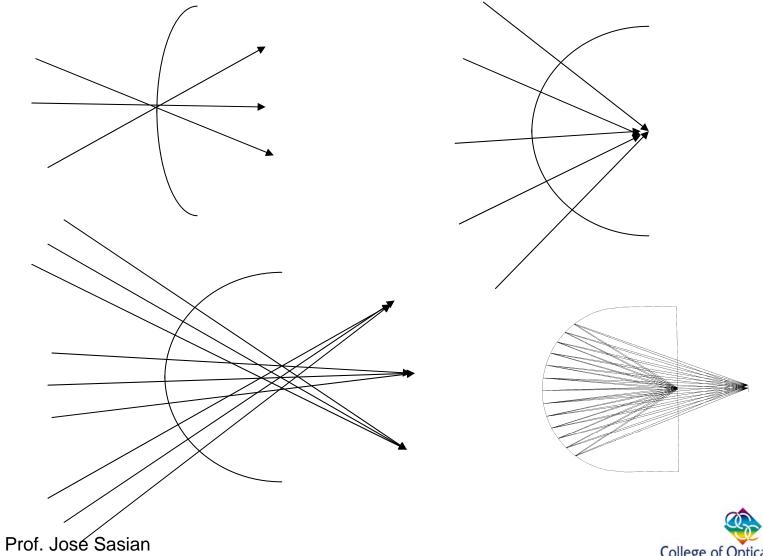
•At y=0, surface is at an image

•A=0, On axis beam concentric with center of curvature

A-bar=0, Off-axis beam concentric, chief ray goes through the center of curvature
Aplanatic points

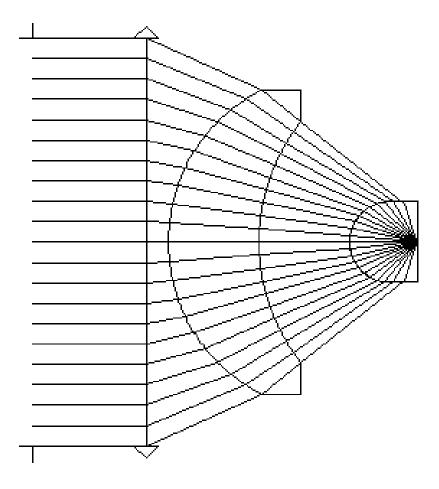


Cases of zero coma



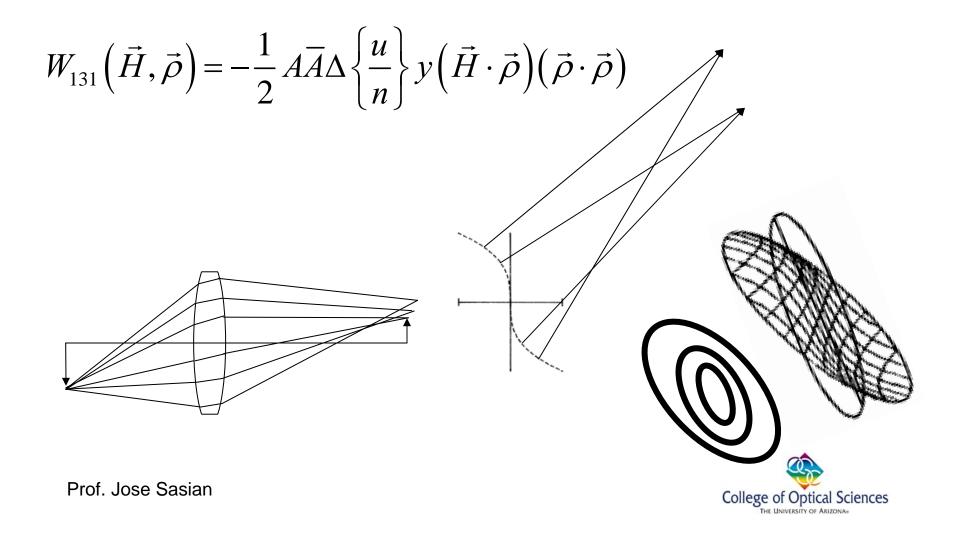


Aplanatic-concentric

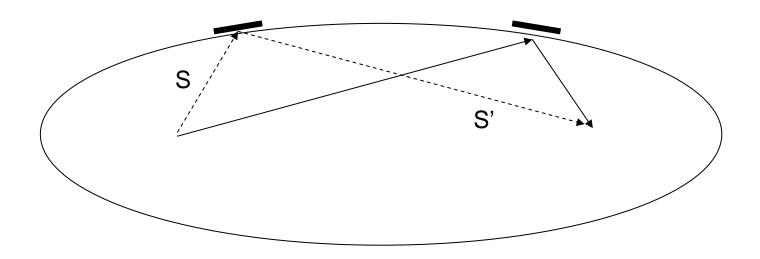




Coma as a variation of magnification with aperture I



Coma as a variation of magnification with aperture II



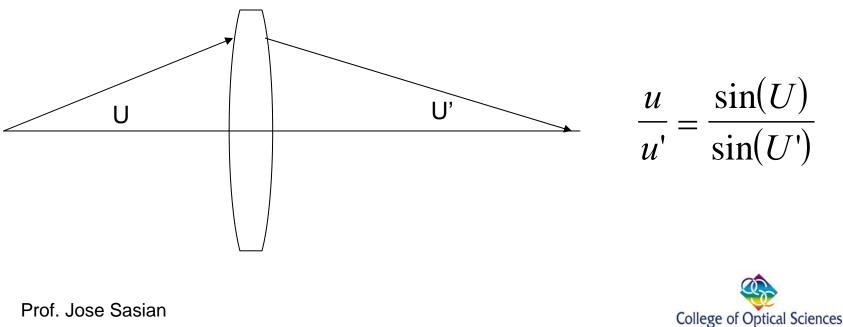
m=s'/s



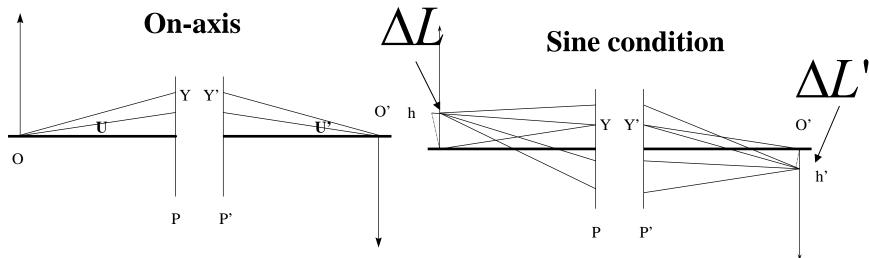
Sine condition

Coma aberration can be considered as a variation of magnification with respect to the aperture. If the paraxial magnification is equal to the real ray marginal magnification, then an optical system would be free of coma. Spherical aberration can be considered as a variation

of the focal length with the aperture.



Sine condition



Optical path length between O and O' is L_{axis} and does not depend on Y or Y'

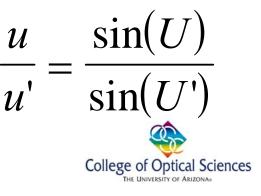
 $\Delta L = h \sin(U) \qquad \Delta L' = h' \sin(U)$

 $L_{off-axis} = L_{axis} + \Delta L' - \Delta L$

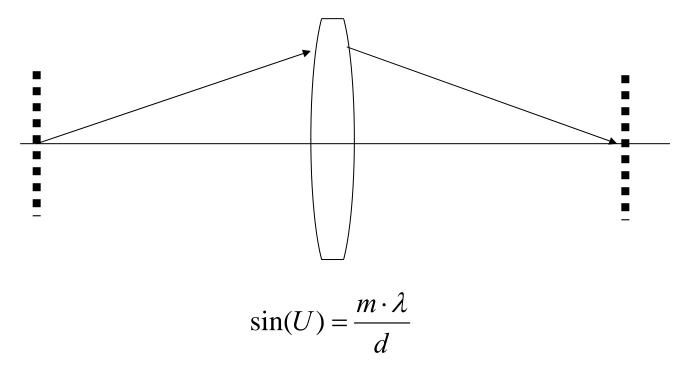
$$L_{off-axis} = L_{axis} + h' n' sin(U') - h n sin(U)$$

 $h'n'\sin(U') = hn\sin(U)$

That is: OPD has no linear phase errors as a function



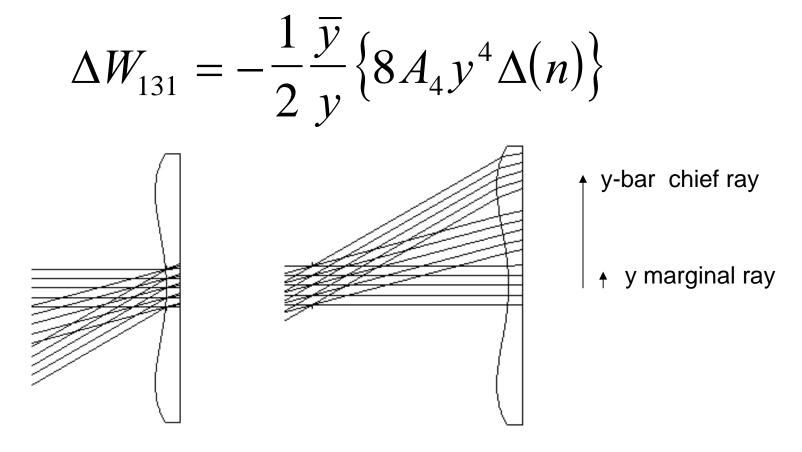
Imaging a grating



$$d \cdot \sin(U) = m \cdot \lambda = d' \sin(U')$$



Contribution from an aspheric surface



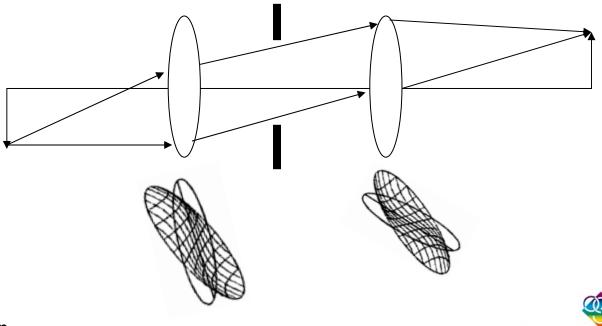


Aberrations and symmetry

$$W(H,\rho,\theta) = W_{200}H^{2} + W_{020}\rho^{2} + W_{111}H\rho\cos\theta + W_{040}\rho^{4} + W_{131}H\rho^{3}\cos\theta + W_{222}H^{2}\rho^{2}\cos^{2}\theta + W_{220}H^{2}\rho^{2} + W_{311}H^{3}\rho\cos\theta + W_{400}H^{4} + W_{220}H^{2}\rho^{2} + W_{311}H^{3}\rho\cos\theta + W_{400}H^{4} + W_{220}H^{2}\rho^{2} + W_{311}H^{3}\rho\cos\theta + W_{400}H^{4} + W_{40}H^{4} + W$$

+...

Coma is an odd aberration with respect to the stopNatural stop position to cancel coma by symmetry

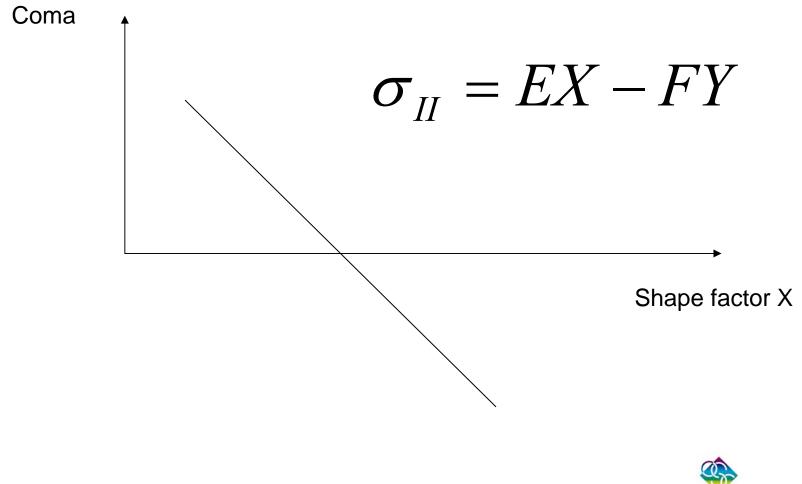




Structural coefficients: Thin lens (stop at lens) $A = \frac{n+2}{n(n-1)^2}$ $S_{I} = \frac{1}{4} y^{4} \phi^{3} \Big[A X^{2} - B X Y + C Y^{2} + D \Big]$ $S_{II} = \frac{1}{2} \mathcal{K} y^2 \varphi^2 \left[EX - FY \right]$ $B = \frac{4(n+1)}{n(n-1)}$ $S_{III} = \mathcal{K}^2 \varphi$ $C = \frac{3n+2}{n}$ $S_{IV} = \mathcal{K}^2 \varphi^{-1}$ $X = \frac{c_1 + c_2}{1 - c_2} = \frac{r_2 + r_1}{1 - c_2}$ $c_1 - c_2 = r_2 - r_1$ $D = \frac{n^2}{(n-1)^2}$ $S_{V} = 0$ $Y = \frac{1+m}{1-m} = \frac{u'+u}{u'-u}$ $C_L = y^2 \phi \frac{1}{v}$ $E = \frac{n+1}{n(n-1)}$ $\phi = \Delta n \Delta c = (n-1)(c_1 - c_r)$ $C_{\tau} = 0$ $F = \frac{2n+1}{n}$

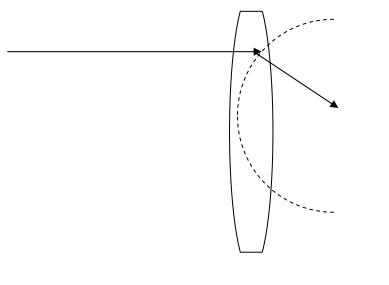


Coma vs Bending

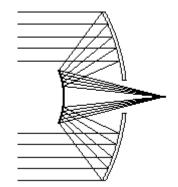


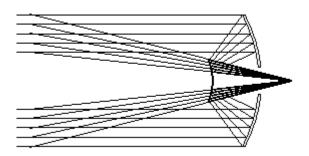
College of Optical Sciences

Principal surface



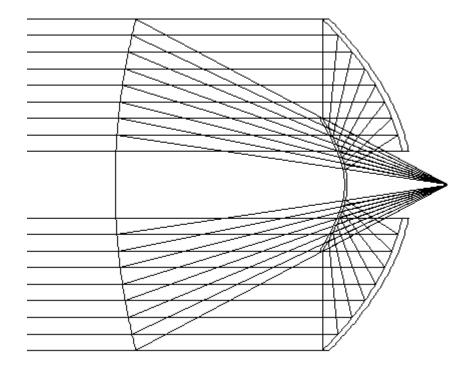
In an aplanat working at m=0 the equivalent refracting surface is a hemisphere







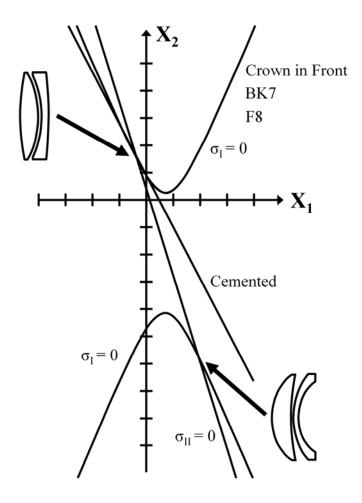
Cassegrain's principal surface

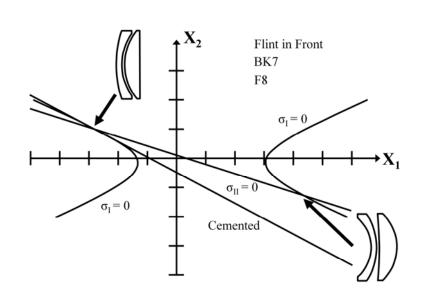


Since the equivalent refracting surface in a Cassegrain telescope is a paraboloid then the coma of that Cassegrain is the same of a paraboloid mirror with the same focal length.



Aplanat doublets







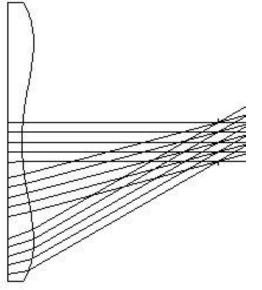
Kingslake's cemented aplanat

Chromatic correction Spherical aberration correction Coma correction Still cemented

C=1/r	d	Glass	n _D	VD
0.1509				
	0.32	SK-11	1.56376	60.75
-0.2246				
	0.15	SF-19	1.66662	33.08
052351				



Control of coma in the presence of an aspheric mirror near a pupil

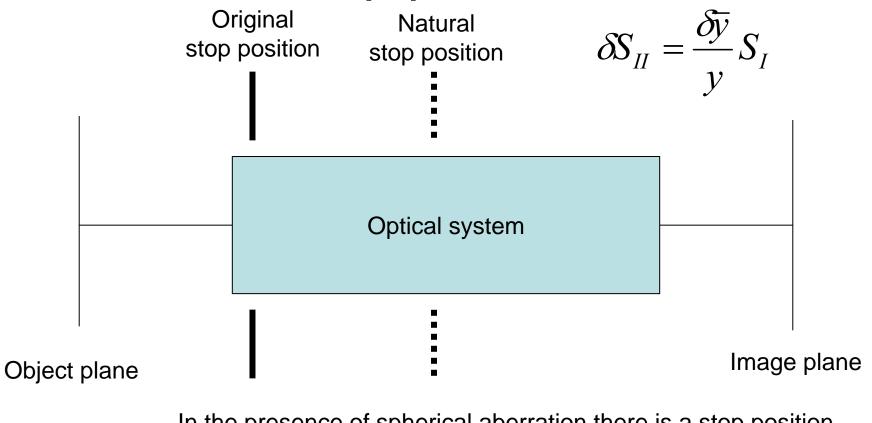


In the presence of a strong aspheric surface near the stop or pupil, coma aberration can be corrected by moving the surface

$$\Delta W_{131} = -\frac{1}{2} \frac{\overline{y}}{\overline{y}} \left\{ 8A_4 y^4 \Delta(n) \right\}$$



Coma correction by natural stop position



In the presence of spherical aberration there is a stop position for which coma is zero. At that stop position spherical aberration might be corrected. Then the system becomes aplanatic and the stop can be shifted back to its original position.

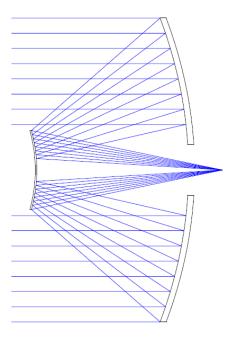
The aplanatic member(s) in a family of solutions

Doublet

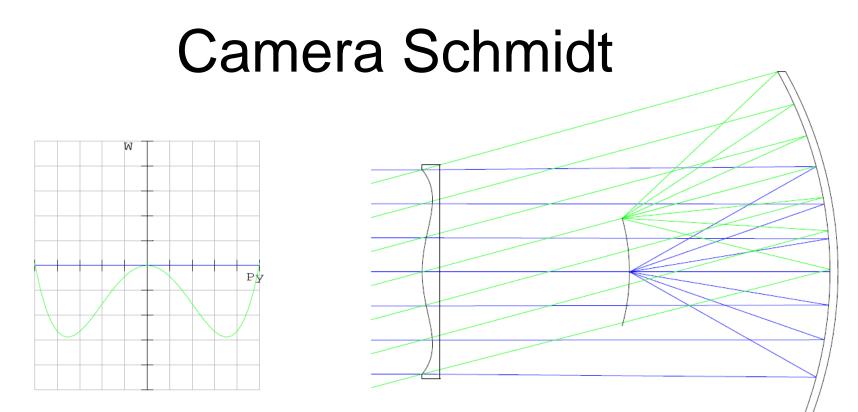




Ritchey-Chretien







Aspheric plate at mirror center of curvature A-bar=0 Stop aperture at aspheric plate Note symmetry about mirror CC No spherical aberration No coma No astigmatism. Anastigmatic over a wide field of view! Satisfies Conrady's D-d sum



Notes

- Need to make aplanatic zero-field systems (that are fast). The alignment becomes easier.
- Lenses for lasers diodes/optical fibers
- Microscope objectives



Summary

- Coma aberration
- Coma as an odd aberration
- Sine condition
- Natural stop position
- Aplanatic doublets
- Zero-field systems

